

Semper in Motu: Transforming Mobility Through Learning and Control

Karl H. Johansson
Digital Futures & EECS
KTH Royal Institute of Technology
Sweden



Bode Lecture
IEEE CDC, Milan
December 16-19, 2024

1

First Bode Lecture: Gunter Stein 1989



Respect the Unstable

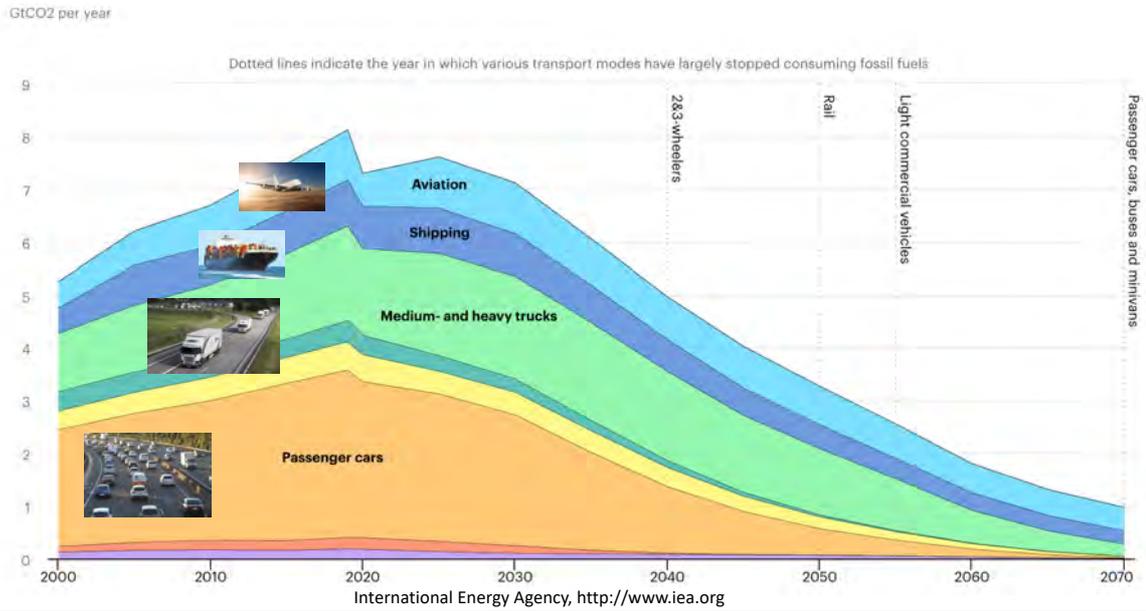
Karl Johan Åström Anders Rantzer



Acknowledgements : Matthieu Barreau, Mladen Čičić, Frank Jiang, Ting Bai, Yuchao Li, Truls Nyberg, Vandana Narri, Miguel Aguiar, Jonas Mårtensson, Henrik Sandberg, Dimos Dimarogonas, Dan Work, Carlos Canudas-de-Wit

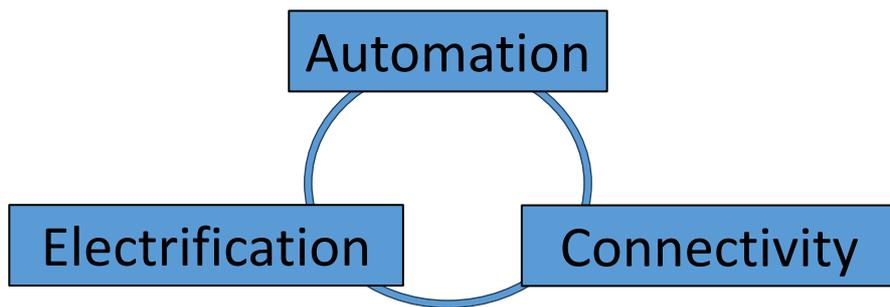
2

Transport CO2 Emissions in the Sustainable Development Scenario



3

The Transformation of the Transport Sector



4

4

The Transformation of the Transport Sector



Volvo



Automation



Einride



Electrification

Connectivity



Scania



Ma et al., 2024



Jiang et al., 2020

Self-driving Vehicles?

Society of Automotive Engineers
Levels of Driving Automation (2014)



Waymo

Sergey Brin, Google, 2012

Google's Sergey Brin: You'll ride in robot cars within 5 years

Ordinary folks will have access to self-driving cars in the next few years, the Google cofounder said at a California bill signing today.



Elon Musk, Tesla, 2016

"I really consider autonomous driving a solved problem," he said. "I think we are probably less than two years away."



Stockholm Public Transport



Volvo Group



Self-driving Vehicles? Not Yet!



Steven Shladover, UC Berkeley, 2018

"I usually tell today's students that they can work with this for the whole of their career. In my opinion, the technology will be fully developed around 2075 - perhaps a little earlier, or perhaps a little later."



Feds Say Self-Driving Uber SUV Did Not Recognize Jaywalking Pedestrian in Fatal Crash



Driverless Car Gets Stuck in Wet Concrete in San Francisco



Tesla FSD Keeps Trying To Drive Into A Train: Video



Waymo Recalls Robotaxis to Give Telephone Poles a Higher 'Damage Score'



Why is transportation hard to automate?

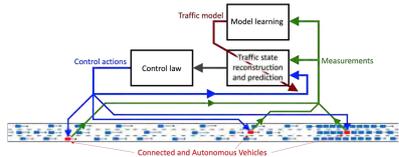
UNCERTAINTY

Control is the science of uncertainty

Network optimization



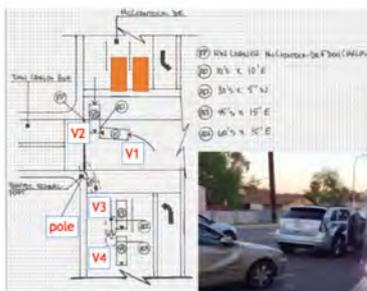
Traffic control



Vehicle autonomy



Uber Automated Vehicle Accident in 2017



Grembek et al., UC-ITS-2018-13, 2018



a) Left-turning Honda and Uber's AV Volvo are on the collision course
 b) Left-turning Honda does not see Uber's AV Volvo
 c) Uber's AV Volvo does not see left-turning Honda

Automated vehicle and human drivers had insufficient information to resolve the situation

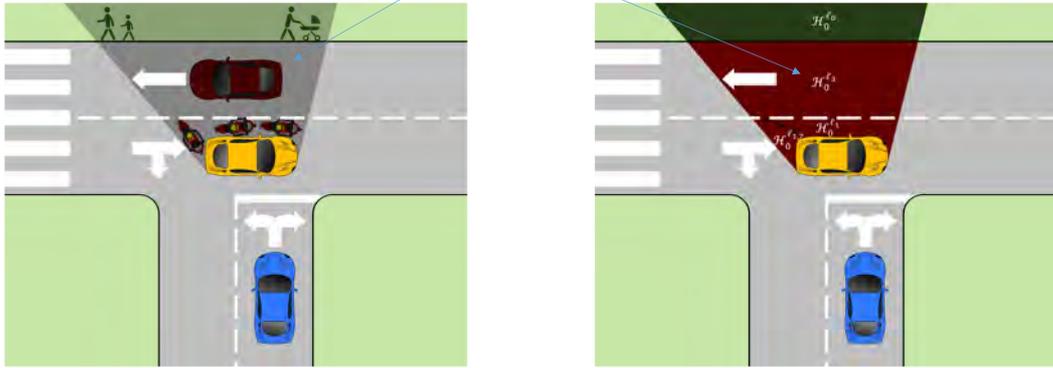
- How should automated vehicles handle **occlusions**?
- How should they **reason** about potential vehicles or other road users in occluded areas?



Pravin Varaiya

Occlusion

Areas not seen from the blue ego vehicle



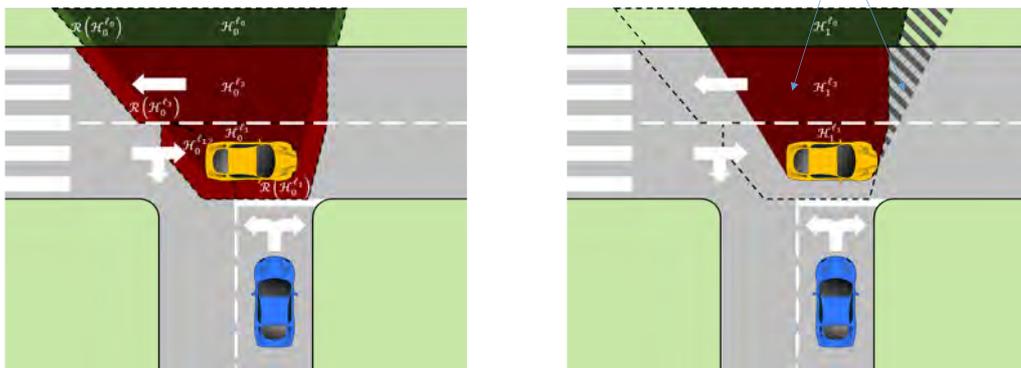
Nyberg, Gaspar Sanchez, Narri et al., 2024

11

11

Foresee the unseen

Propagate sets in occluded regions based on lane properties



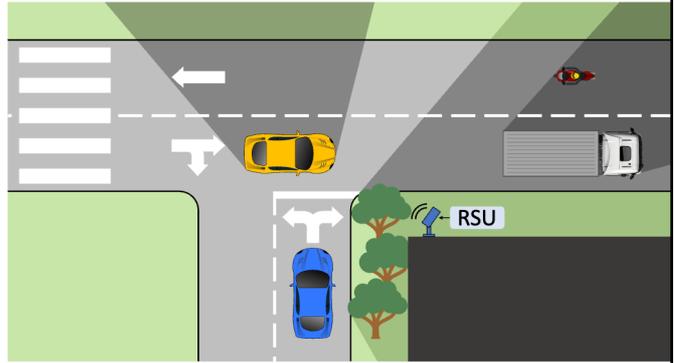
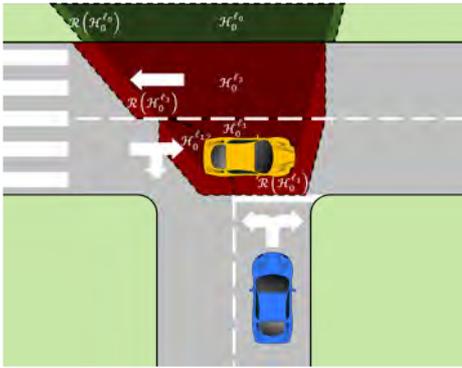
Nyberg, Gaspar Sanchez, Narri et al., 2024

12

12

Share the unseen

Ego vehicle situational awareness can be enhanced by roadside unit (RSU) sharing information about occluded areas



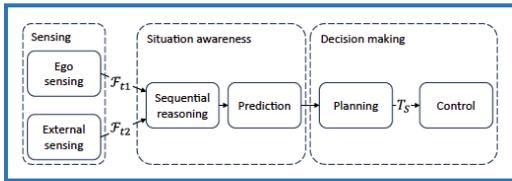
Supported by ETSI standard ITS-G5 for V2X communication with Collaborative Perception Messages sent at 10 Hz

Nyberg, Gaspar Sanchez, Narri et al., 2024

13

13

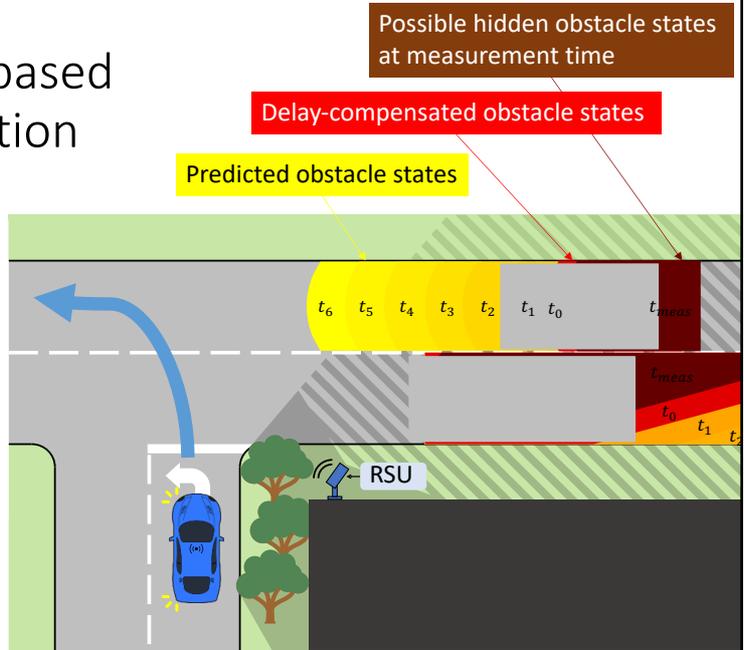
Sequential reasoning based on shared set information



- Set of possible hidden obstacles computed based on reachability analysis using RSU and other sensors information together with traffic rules
- Ego vehicle plans its motion under guarantee to stay in the safe set:

```

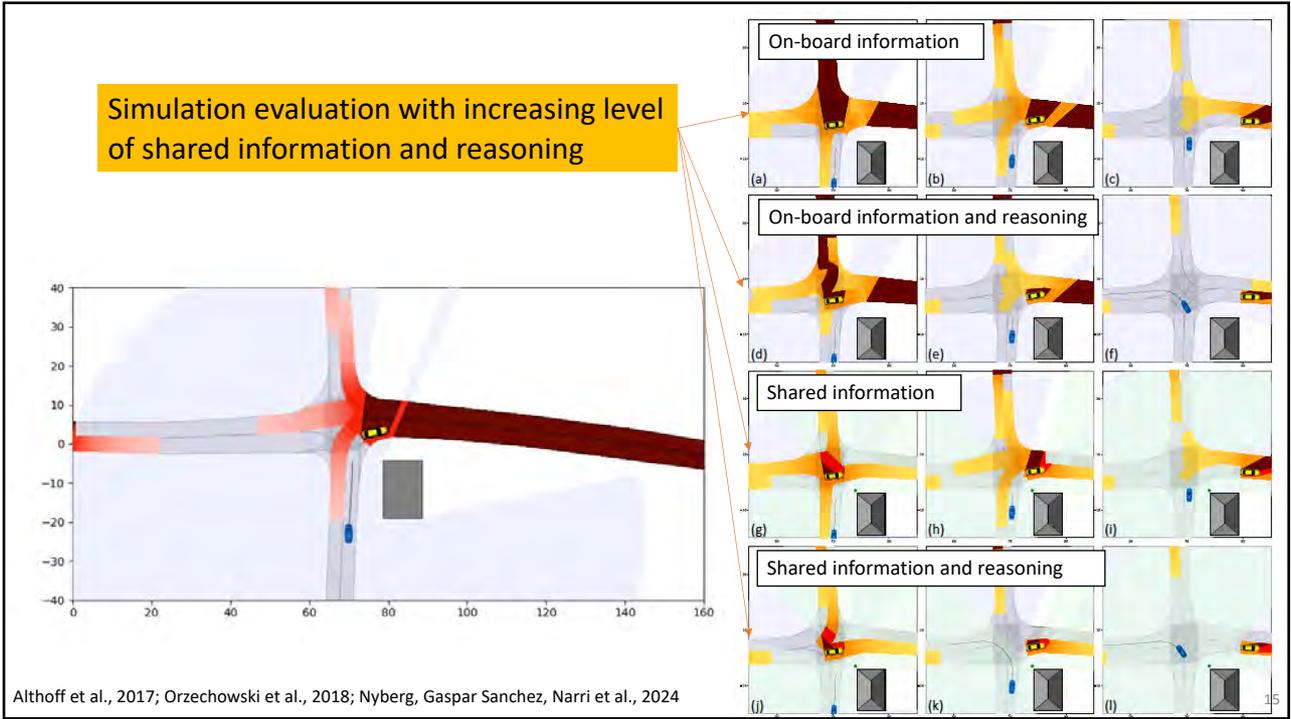
foreach  $\mathcal{H}_{[t_a, t_b]}^c \in \mathcal{H}_{[t_a, t_b]}^c$ 
  foreach  $i \in 1$  to  $N$ 
     $t_a \leftarrow t_{[last, t_a]} + (i - 1)\Delta t$ 
     $t_b \leftarrow t_{[last, t_b]} + i\Delta t$ 
     $\mathcal{O}_{[t_a, t_b]}^c \leftarrow occ(\mathcal{R}(\mathcal{H}_{[t_a, t_b]}^c, M^c, [t_a, t_b]), 0)$ 
     $\mathcal{O}_{[t_a, t_b]}^c \leftarrow \mathcal{O}_{[t_a, t_b]}^c \cup \mathcal{O}_{[t_a, t_b]}^{[c]}$ 
 $T \leftarrow generateTrajectories(x_{ego}^{[0]}, \mathcal{O}_{[t_a, t_b]}^c)$ 
 $J_s \leftarrow getSafeTrajectories(T, (\mathcal{O}_{[t_{last}, t_{last} + \Delta t]}^c, \dots, \mathcal{O}_{[t_a, t_b]}^c))$ 
 $T \leftarrow getBestTrajectory(J_s)$ 
return  $T$ 
    
```



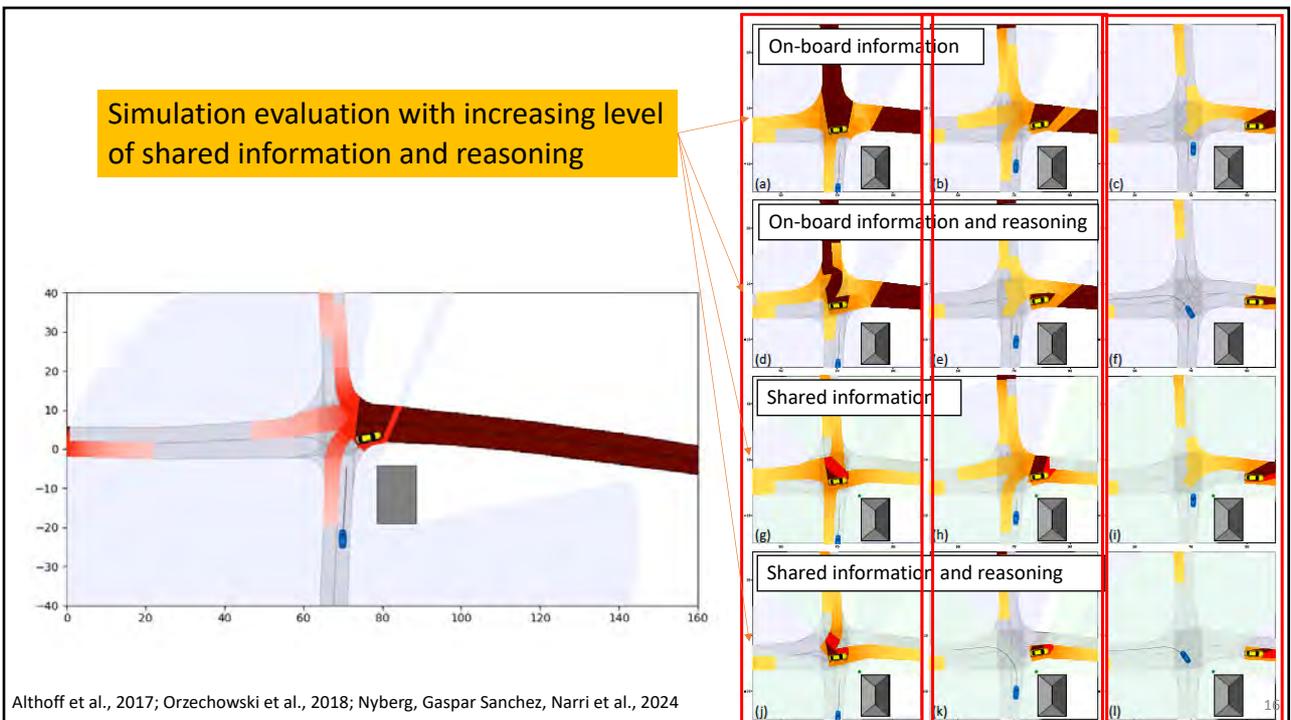
Nyberg, Gaspar Sanchez, Narri et al., 2024

14

14



15



16

Experimental evaluation on Scania test track



17

A 2x2 grid of images illustrating vehicle perception and communication. The top-left image shows a truck on the test track. The top-right image shows a truck at the intersection. The bottom-left image shows a sensor visualization with green and blue lines representing the field of view of the ego vehicle and other vehicles. The bottom-right image shows a similar sensor visualization with a text box. A central text box with a white background and black text reads: "Ego vehicle can reason about if the occluded area is occupied or not". A text box at the bottom of the grid reads: "Roadside Unit share information about area occluded for the ego vehicle". The number '18' is in the bottom right corner of the grid.

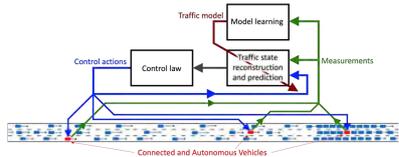
Nyberg, Gaspar Sanchez, Narri et al., 2024

18

Network optimization

Traffic control

Vehicle autonomy


Use automated truck platoons to regulate car traffic



- Trucks are slower than cars and act as moving bottlenecks in traffic
- **Idea:** Regulate cars moving into congested area by controlling platoon velocity

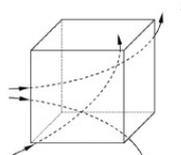


Flows according to Euler and Lagrange



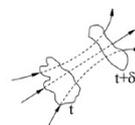
Leonhard Euler (1707-1783)

Euler was looking at fluid motion focused on specific locations in the space through which the fluid flows as time passes.



Joseph-Louis Lagrange (1736-1813)

Lagrange was looking at fluid motion where the observer follows an individual fluid parcel as it moves through space and time



21

21

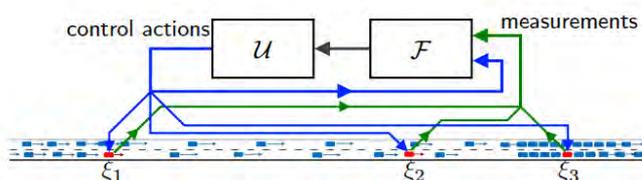
From Eulerian to Lagrangian traffic control



Leonhard Euler (1707-1783)
 Stationary observer of the flow
 Traffic control based on fixed infrastructure
 High deployment costs and limited flexibility



Joseph-Louis Lagrange (1736-1813)
 Observers moves with the flow
 Traffic control based on mobile sensors and actuators
 Need for a new system theoretic foundation

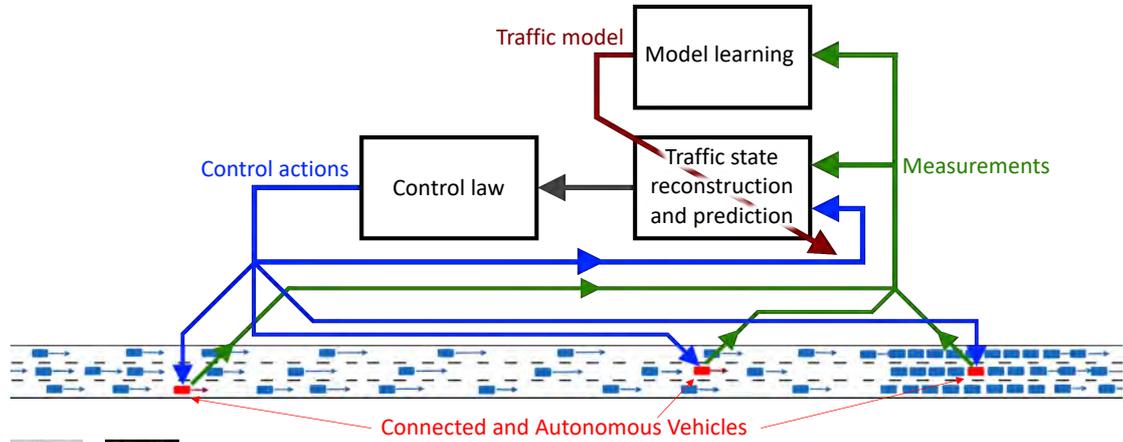


Edie, 1963; Papageorgiou et al., 1991; Hegyi et al., 2005; Ferrara et al., 2018; Yu & Krstić, 2019; Gloudemans et al., 2023

Work et al., 2008; Delle Monache et al., 2019; Barreau et al., 2021
 Čičić & J, 2018; Piacentini et al., 2018²

22

Lagrangian traffic control system



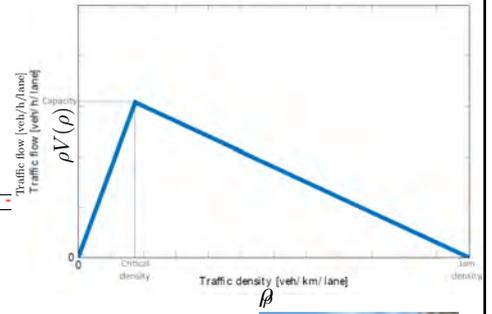
Čičić et al., 2021; Barreau, Aguiar, J, 2021

Wu et al., 2021; Lee et al. 2024 23

23

Fundamental diagram of traffic flow

Microscopic traffic model with 329 vehicles $\dot{x}_i(t) = V(\rho(t, x_i(t)))$



Macroscopic traffic model with density function $\rho : \mathbb{R}^+ \times [0, L] \mapsto [0, 1]$



$$\frac{\partial \rho}{\partial t} + \frac{\partial V(\rho)\rho}{\partial x} = 0$$



24

24



Connected and Autonomous Vehicles

Traffic model with N probing vehicles

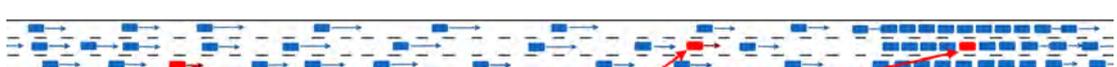
$$\frac{\partial \rho}{\partial t} + \frac{\partial V(\rho)\rho}{\partial x} = \gamma^2 \frac{\partial^2 \rho}{\partial x^2}, \quad (t, x) \in [0, T] \times [0, L]$$

$$\dot{x}_i(t) = V(\rho(t, x_i(t))), \quad t \in [0, T], i = 1, \dots, N$$

Control of a coupled PDE-ODE system

Lebacque et al., 1998; Delle Monache & Goatin, 2014; Barreau, Selivanov, J, 2020; Barreau, Aguiar et al., 2021

25



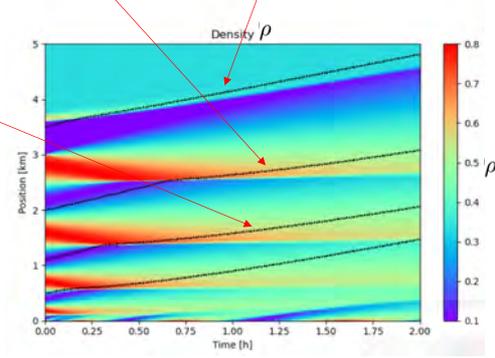
Connected and Autonomous Vehicles

Traffic model with N probing vehicles

$$\frac{\partial \rho}{\partial t} + \frac{\partial V(\rho)\rho}{\partial x} = \gamma^2 \frac{\partial^2 \rho}{\partial x^2}, \quad (t, x) \in [0, T] \times [0, L]$$

$$\dot{x}_i(t) = V(\rho(t, x_i(t))), \quad t \in [0, T], i = 1, \dots, N$$

Control of a coupled PDE-ODE system



Lebacque et al., 1998; Delle Monache & Goatin, 2014; Barreau, Selivanov, J, 2020; Barreau, Aguiar et al., 2021

26

Learning-based traffic state reconstruction

How can we out of noisy measurements from **probe vehicles**

$$\{x_i(t), \underbrace{\rho(t, x_i(t))}_{\rho_i(t)}, \underbrace{V(\rho_i(t))}_{V_i(t)}\}_{i \in [1, N]}$$

reconstruct the density $\hat{\rho}^* = \arg \min_{\hat{\rho}} \int_0^T \|\rho(t, \cdot) - \hat{\rho}(t, \cdot)\|^2 dt$?



27

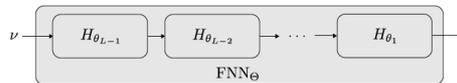
27

Neural network model

Model density and velocity as feedforward neural networks



with each layer having a set of parameters to be trained:



$$\min_{\Theta_\rho} \frac{1}{N} \sum_{i=1}^N \int_0^T |\hat{\rho}_{\Theta_\rho}(t, x_i(t)) - \rho_i(t)|^2 dt$$

$$\min_{\Theta_V} \frac{1}{N} \sum_{i=1}^N \int_0^T |\hat{V}_{\Theta_V}(\rho_i(t)) - V_i(t)|^2 dt$$

Barreau, Selivanov, J, 2020; Barreau, Aguiar, J, 2021

28

28

Physics-informed neural network model

Model density and velocity as feedforward neural networks



with each layer having a set of parameters to be trained:

$$\min_{\Theta_\rho} \frac{1}{N} \sum_{i=1}^N \int_0^T |\hat{\rho}_{\Theta_\rho}(t, x_i(t)) - \rho_i(t)|^2 dt \quad \min_{\Theta_V} \frac{1}{N} \sum_{i=1}^N \int_0^T |\hat{V}_{\Theta_V}(\rho_i(t)) - V_i(t)|^2 dt$$

under **physical constraints**

$$\frac{\partial \hat{\rho}_{\Theta_\rho}}{\partial t} + \frac{\partial \hat{V}_{\Theta_V}(\hat{\rho}_{\Theta_\rho}) \hat{\rho}_{\Theta_\rho}}{\partial x} = \gamma^2 \frac{\partial^2 \hat{\rho}_{\Theta_\rho}}{\partial x^2} \quad \left| \frac{\partial \hat{V}_{\Theta_V}}{\partial \rho} \right|_+ = 0$$

- Physics-informed neural networks [Raissi, Perdikaris, Karniadakis, 2019]
- Application to traffic modeling [Barreau, Selivanov, J, 2020; Barreau, Aguiar, J, 2021]

29

29

Training physics-informed neural network

$$\begin{aligned} \operatorname{argmin}_{\Theta_\rho, \Theta_V} \quad & \frac{1}{N} \sum_{i=1}^N \left\{ \int_0^T |\hat{\rho}_{\Theta_\rho}(t, x_i(t)) - \rho_i(t)|^2 dt + \int_0^T |\hat{V}_{\Theta_V}(\rho_i(t)) - V_i(t)|^2 dt \right\} \\ \text{s. t.} \quad & \frac{\partial \hat{\rho}_{\Theta_\rho}}{\partial t} + \frac{\partial \hat{V}_{\Theta_V}(\hat{\rho}_{\Theta_\rho}) \hat{\rho}_{\Theta_\rho}}{\partial x} = \gamma^2 \frac{\partial^2 \hat{\rho}_{\Theta_\rho}}{\partial x^2} \\ & \left| \frac{\partial \hat{V}_{\Theta_V}}{\partial \rho} \right|_+ = 0 \end{aligned}$$

with Lagrangian relaxation

$$\begin{aligned} \operatorname{argmin}_{\Theta_\rho, \Theta_V} \max_{\lambda_\rho, \lambda_V} \quad & \frac{1}{N} \sum_{i=1}^N \int_0^T \left\{ |\hat{\rho}_{\Theta_\rho}(t, x_i(t)) - \rho_i(t)|^2 + |\hat{V}_{\Theta_V}(\rho_i(t)) - V_i(t)|^2 \right\} dt \\ & + \lambda_\rho \iint_{[0, T] \times [0, L]} \left| \frac{\partial \hat{\rho}_{\Theta_\rho}}{\partial t}(\nu) + \frac{\partial \hat{V}_{\Theta_V}(\hat{\rho}_{\Theta_\rho}) \hat{\rho}_{\Theta_\rho}}{\partial x}(\nu) - \gamma^2 \frac{\partial^2 \hat{\rho}_{\Theta_\rho}}{\partial x^2}(\nu) \right|^2 d\nu + \lambda_V \int_0^1 \left| \frac{\partial \hat{V}_{\Theta_V}}{\partial \rho}(\rho) \right|^2 d\rho \\ =: \operatorname{argmin}_{\Theta_\rho, \Theta_V} \max_{\lambda_\rho, \lambda_V} \quad & \mathcal{L}_{\lambda_\rho, \lambda_V}(\Theta_\rho, \Theta_V) \end{aligned}$$

Barreau, Selivanov, J, 2020; Barreau, Aguiar, J, 2021; Barreau, 2024 30

30

Training physics-informed neural network

$$\arg \min_{\Theta_\rho, \Theta_V} \max_{\lambda_\rho, \lambda_V} \frac{1}{N} \sum_{i=1}^N \int_0^T \left\{ |\hat{\rho}_{\Theta_\rho}(t, x_i(t)) - \rho_i(t)|^2 + |\hat{V}_{\Theta_V}(\rho_i(t)) - V_i(t)|^2 \right\} dt$$

$$+ \lambda_\rho \iint_{[0,T] \times [0,L]} \left| \frac{\partial \hat{\rho}_{\Theta_\rho}}{\partial t}(\nu) + \frac{\partial \hat{V}_{\Theta_V}(\hat{\rho}_{\Theta_\rho}) \hat{\rho}_{\Theta_\rho}}{\partial x}(\nu) - \gamma^2 \frac{\partial^2 \hat{\rho}_{\Theta_\rho}}{\partial x^2}(\nu) \right|^2 d\nu + \lambda_V \int_0^1 \left| \frac{\partial \hat{V}_{\Theta_V}}{\partial \rho}(\rho) \right|^2 d\rho$$

$$=: \arg \min_{\Theta_\rho, \Theta_V} \max_{\lambda_\rho, \lambda_V} \mathcal{L}_{\lambda_\rho, \lambda_V}(\Theta_\rho, \Theta_V)$$

Primal problem

$$\Theta_\rho^*(\lambda_\rho), \Theta_V^*(\lambda_V) = \arg \min_{\Theta_\rho, \Theta_V} \mathcal{L}_{\lambda_\rho, \lambda_V}(\Theta_\rho, \Theta_V)$$

Dual problem

$$\lambda_\rho^*(\Theta_\rho), \lambda_V^*(\Theta_V) = \arg \max_{\lambda_\rho, \lambda_V} \mathcal{L}_{\lambda_\rho, \lambda_V}(\Theta_\rho, \Theta_V)$$

Primal-dual gradient descent iterations

Primal step

$$\Theta_\rho^{k+1} = \Theta_\rho^k - \alpha_\Theta^k \nabla_{\Theta_\rho} \mathcal{L}_{\lambda_\rho, \lambda_V}(\Theta_\rho, \Theta_V)$$

$$\Theta_V^{k+1} = \Theta_V^k - \alpha_\Theta^k \nabla_{\Theta_V} \mathcal{L}_{\lambda_\rho, \lambda_V}(\Theta_\rho, \Theta_V)$$

Dual step

$$\lambda_\rho^{k+1} = \lambda_\rho^k - \alpha_\lambda^k \nabla_{\lambda_\rho} \mathcal{L}_{\lambda_\rho, \lambda_V}(\Theta_\rho, \Theta_V)$$

$$\lambda_V^{k+1} = \lambda_V^k - \alpha_\lambda^k \nabla_{\lambda_V} \mathcal{L}_{\lambda_\rho, \lambda_V}(\Theta_\rho, \Theta_V)$$

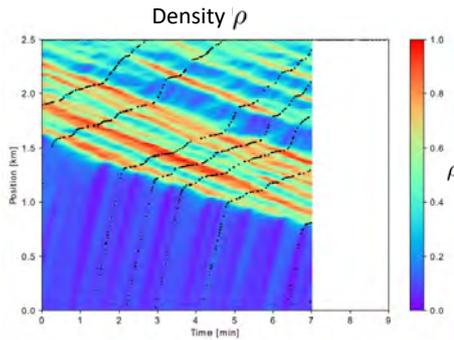
- Multiple dual steps for each primal
- Uniform and importance sampling of the integrals

Barreau, Aguiar, J, 2021; Barreau, 2024

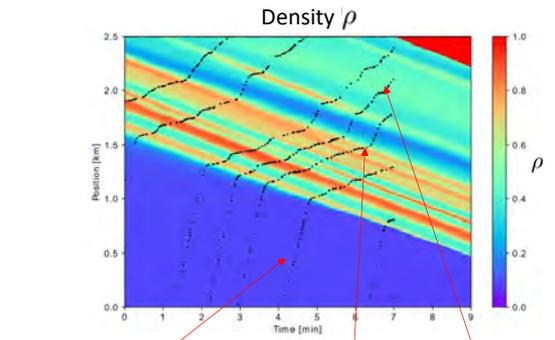
31

31

Micro (vehicle) simulated density over time interval [0,7] min



Reconstructed and predicted density over [0,9] min using PINN model



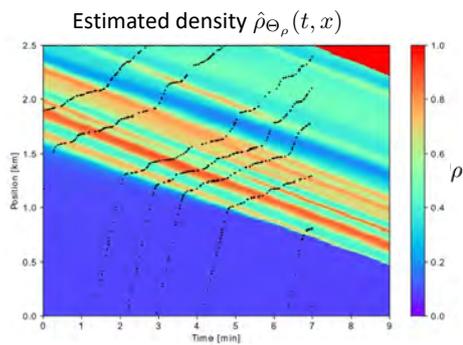
Trained model captures traffic dynamics despite sparse sampling

Liu et al., 2021; Delle Monache et al., 2022

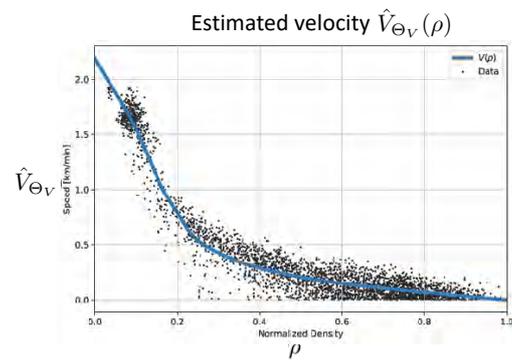
32

32

Trained PDE model captures density evolution observed in real data



Trained NN velocity model captures relationship observed in real data

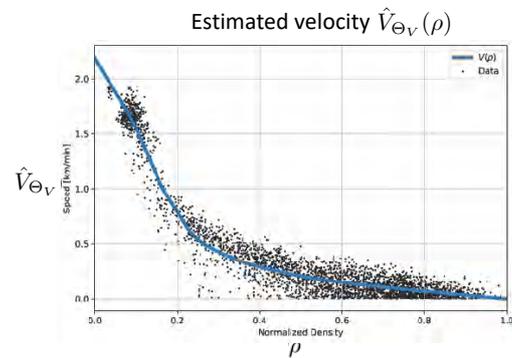
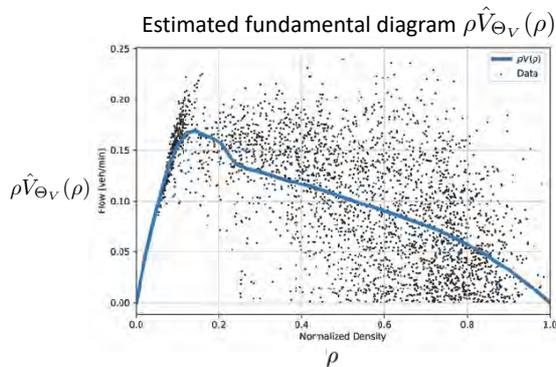


Liu et al., 2021; Delle Monache et al., 2022

33

33

Trained NN velocity model captures relationship observed in real data

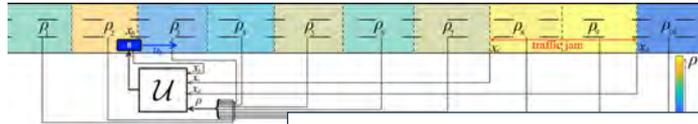


Liu et al., 2021; Delle Monache et al., 2022

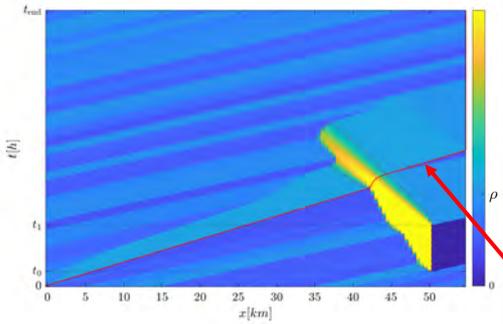
34

34

Control truck platoon velocity to dissipate traffic congestion



Without truck platoon control



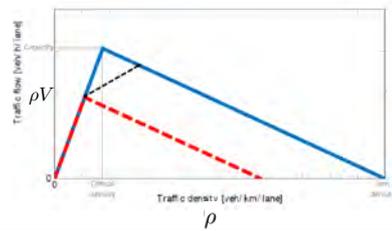
Truck platoon velocity control

Controlled platoon velocity

$$\dot{x}_i(t) = \min(V(\rho(t, x_i(t))), u(t))$$

reduces road capacity

$$V(\rho(t, x_i(t))) \leq V_{con}(\rho(t, x_i(t)), u(t))$$



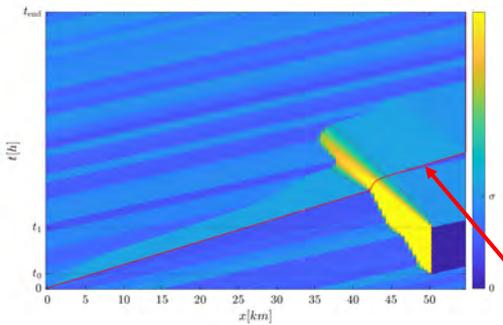
Giorgio, 2002; Delle Monache & Goatin, 2014; Cacic and J, 2018; Liu et al., 2021

35

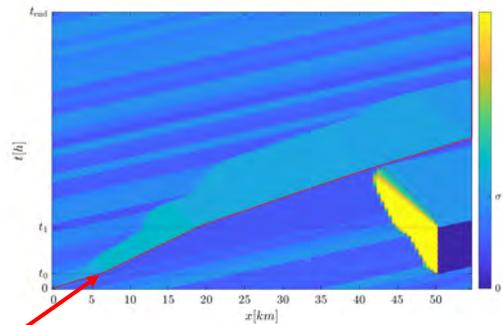
Control truck platoon velocity to dissipate traffic congestion



Without truck platoon control



With truck platoon control

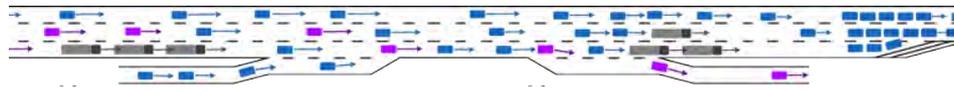


Truck platoon trajectory

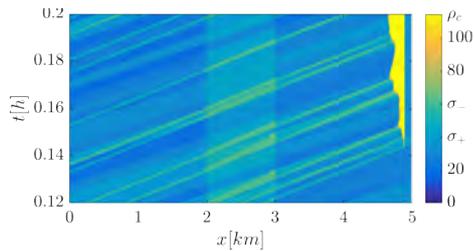
Cacic and J, 2018

36

Truck platoon control reduces total travel time for all vehicles



Without truck platoon control



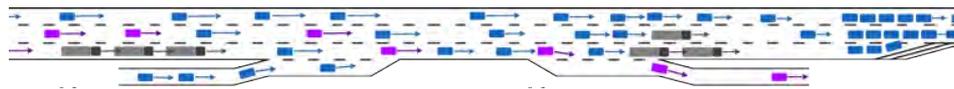
38% total travel time increase due to traffic congestion

Cicic, Jin and J, 2019

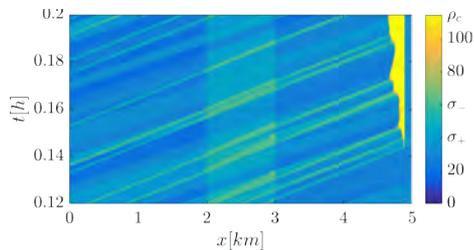
37

37

Truck platoon control reduces total travel time for all vehicles

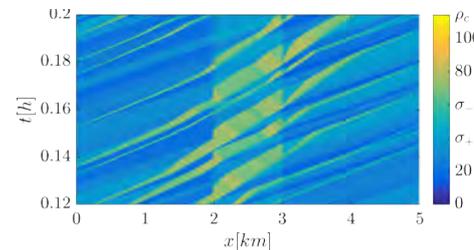


Without truck platoon control



38% total travel time increase due to traffic congestion

With truck platoon control



8% total travel time increase due to traffic congestion

Cicic, Jin and J, 2019

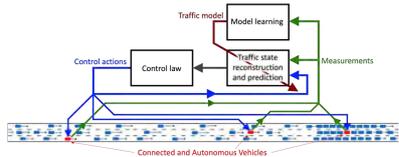
38

38

Network optimization



Traffic control



Vehicle autonomy



39

39

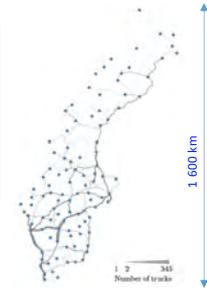
Distributed Charging Coordination of Electric Trucks

Consider 1 000 electric trucks travel over Swedish road network daily

Problem: How can the trucks decide **where** and **when** to charge with

- Pre-planned routes
- Limited charging capacity
- Uncertain travel times and energy consumptions





Solution: Trucks update their charging plans supported by forecasts provided by the charging stations

- **Scalability:** Each truck computes its **own charging plan**, with no central coordination
- **Privacy:** Stations provide **aggregated** forecast information, and trucks never reveal their plans to others



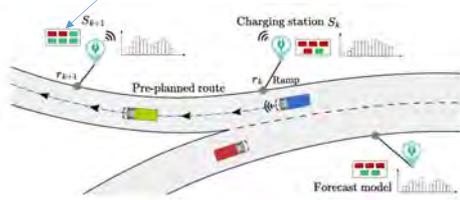
Bai, Li et al., 2024 40

40

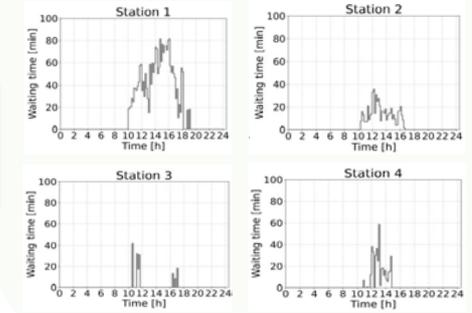
Rollout-based Truck Planning with Uncertain Charging Capacity

Charging stations

- a) Charge **waiting time forecast model** based on historical data
- b) Assign charging spots as trucks arrive to charging station



Waiting time forecast models for charging stations



Distributed rollout-based solution for truck planning

- a) Truck talks to stations S_k, S_{k+1}, \dots to obtain **estimated waiting times**
- b) Truck simulates the worst case if or if not charging at station S_k : Each simulated scenario leads to a linear program, fast to solve
- c) Repeat the procedure when approaching next station S_{k+1}

Guaranteed feasible plans for all trucks

Consistently improving plans

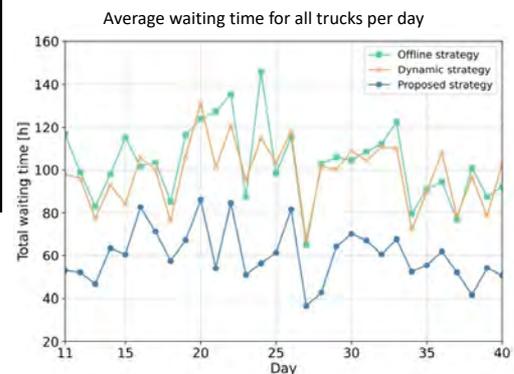
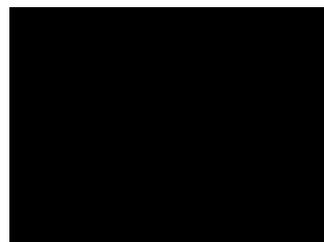
Bai, Li et al., 2024 ⁴¹

41

Evaluation over the Swedish road network



- **Reduced time for charging** is important for electric heavy vehicle adoption
- Evaluated on realistic freight transport missions and models for 1 000 electric trucks
- Our distributed charge plans give **50% lower waiting times**

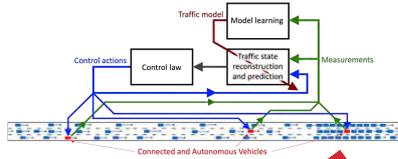


Bai, Li et al., 2024 ⁴²

42

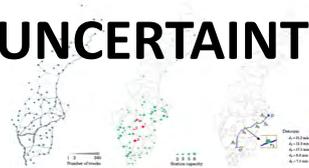
Control community develops the tools to mitigate uncertainty

Physics-data-driven modeling



Stochastic forecasting

UNCERTAINTY



Safety-first set computing



Festina lente
Proceed quickly, but cautiously

Slides and papers available at people.kth.se/~kallej

Main references for presented results

- Jiang, F.J., Gao, Y., Xie, L., Johansson, K.H. (2020). Human-centered design for safe teleoperation of connected vehicles. *IFAC-PapersOnLine*, 53(5), 224-231.
- Nyberg, T., Sánchez, J.M.G., Narri, V., et al. (2024). Share the unseen: Sequential reasoning about occlusions using V2X technology. *IEEE Transactions on Control Systems Technology*.
- Jin, L., Čičić, M., Amin, S., Johansson, K.H. (2018). Modeling the impact of vehicle platooning on highway congestion: A fluid queuing approach. *Hybrid Systems Conference Proceedings*.
- Barreau, M., Aguiar, M., Liu, J., Johansson, K.H. (2021). Physics-informed learning for identification and state reconstruction of traffic density. *IEEE Conference on Decision and Control (CDC)*.
- Čičić, M., Xiong, X., Jin, L., Johansson, K.H. (2021). Coordinating Vehicle Platoons for Highway Bottleneck Decongestion and Throughput Improvement. *IEEE Transactions on Intelligent Transportation Systems*, 1-13.
- Barreau, M., Selivanov, A., Johansson, K.H. (2020). Dynamic traffic reconstruction using probe vehicles. *IEEE Conference on Decision and Control (CDC)*, 233-238.
- Liu, J., Barreau, M., Čičić, M., Johansson, K.H. (2021). Learning-based traffic state reconstruction using probe vehicles. Elsevier.
- Liang, K.Y., Mårtensson, J., Johansson, K.H. (2016). Heavy-duty vehicle platoon formation for fuel efficiency. *IEEE Transactions on Intelligent Transportation Systems*.
- Besselink, B., Turri, V., Van De Hoef, S.H., et al. (2016). Cyber-physical control of road freight transport. *Proceedings of the IEEE*, 104(5), 1128-1141.
- Keimer, A., Laurent-Brouty, N., Farokhi, F., et al. (2018). Information patterns in the modeling and design of mobility management services. *Proceedings of the IEEE*, 106(4), 554-576.
- Li, Y., Johansson, K.H., Mårtensson, J. (2019). A hierarchical control system for smart parking lots with automated vehicles: Improve efficiency by leveraging prediction of human drivers. *18th European Control Conference (ECC)*, 2675-2681.
- Emanuelsson, W., Riveiros, A.P., Li, Y., Johansson, K.H., Mårtensson, J. (2023). Multiagent rollout with reshuffling for warehouse robots path planning. *IFAC-PapersOnLine*, 56(2), 3027-3032.
- Al Alam, A., Gattami, A., Johansson, K.H. (2010). An experimental study on the fuel reduction potential of heavy duty vehicle platooning. *13th International IEEE Conference on Intelligent Transportation Systems*.
- Turri, V., Besselink, B., Johansson, K.H. (2017). Cooperative look-ahead control for fuel-efficient and safe heavy-duty vehicle platooning. *IEEE Transactions on Control Systems Technology*.
- Bai, T., Li, Y., Johansson, K.H., Mårtensson, J. (2024). Rollout-based charging strategy for electric trucks with hours-of-service regulations. *IEEE Control Systems Letters*, 7, 2167-2172.
- Bai, T., Li, Y., Johansson, K.H., Mårtensson, J. (2024). Distributed charging coordination of electric trucks with limited charging resources. *22nd European Control Conference (ECC)*, 2897-2902.
- Bai, T., Li, Y., Johansson, K.H., Mårtensson, J. (2024). Distributed charging coordination for electric trucks under limited facilities and travel uncertainties. *arXiv preprint arXiv:2407.10207*.

45

References for some related work mentioned

- Grembek, O., Kurzhanskiy, A., Medury, A., Varaiya, P., Yu, M., & Siddiqui, A. (2018). Safe Operation of Automated Vehicles in Intersections. <https://escholarship.org/uc/item/4dm0q8tp>
- Althoff, M., Koschi, M., Manzi, S. (2017). CommonRoad: Composible benchmarks for motion planning on roads. *IEEE Intelligent Vehicles Symposium*, 719-726.
- Orzechowski, P.F., Meyer, A., Lauer, M. (2018). Tackling occlusions & limited sensor range with set-based safety verification. *21st International Conference on Intelligent Transportation Systems*.
- Wu, T., Zhang, J., & Lee, J. (2021). Congestion boundary approach for phase transitions in traffic flow. *Transportmetrica B: Transport Dynamics*.
- Lebacque, J.P., Lesort, J.B., Giorgi, F. (1998). Introducing buses into first-order macroscopic traffic flow models. *Transportation Research Record*, 1644(1), 70-79.
- Delle Monache, M.L., Goatin, P. (2014). A front tracking method for a strongly coupled PDE-ODE system with moving density constraints in traffic flow. *Discrete and Continuous Dynamical Systems*.
- Ferrara, A., Saccone, S., Siri, S. (2018). *Freeway traffic modelling and control*. Springer.
- Yu, H., Krstic, M. (2019). Traffic congestion control for Aw-Rasclé-Zhang model. *Automatica*, 100, 38-51.
- Gludemans, D., Wang, Y., Ji, J., Zachar, G., et al. (2023). I-24 MOTION: An instrument for freeway traffic science. *Transportation Research Part C*.
- Hoh, B., Gruteser, M., Herring, R., et al. (2006). Virtual trip lines for distributed privacy-preserving traffic monitoring. *6th International Conference on Mobile Systems*.
- Delle Monache, M.L., Liard, T., Rat, A., et al. (2019). Feedback control algorithms for the dissipation of traffic waves with autonomous vehicles. *Computational Intelligence and Optimization Methods for Control Engineering*.
- Stern, R.E., Cui, S., Monache, M.L.D., et al. (2018). Dissipation of stop-and-go waves via control of autonomous vehicles: Field experiments. *Transportation Research Part C*, 89, 205-221.
- Edie, L.C. (1963). *Discussion of Traffic Stream Measurements and Definitions*. Port of New York.
- Papageorgiou, M., Hadj-Salem, H., Blosseville, J.M. (1991). ALINEA: A local feedback control law for on-ramp metering. *Transportation Research Record*, 1320(1), 58-67.
- Hegyi, A., De Schutter, B., Hellendoorn, H. (2005). Model predictive control for optimal coordination of ramp metering and variable speed limits. *Transportation Research Part C*.
- Piacentini, G., Goatin, P., Ferrara, A. (2018). Traffic control via moving bottleneck of coordinated vehicles. *IFAC-PapersOnLine*.
- Delle Monache, M.L., Pasquale, C., Barreau, M., Stern, R. (2022). New frontiers of freeway traffic control and estimation. *IEEE Conference on Decision and Control (CDC)*, 6910-6925.
- Bertsekas, D.P. (2024). *Lessons from AlphaZero for optimal, model predictive, and adaptive control*. Athena Scientific

46