

Cyber-Security of Networked Control Systems

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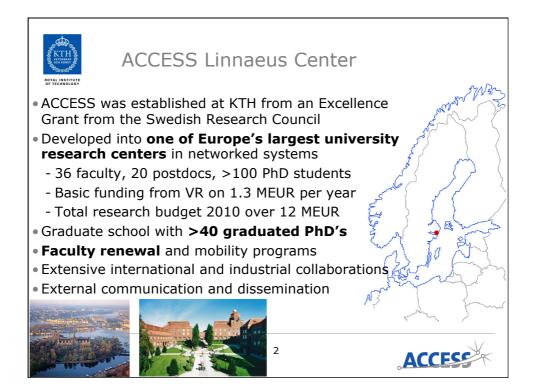




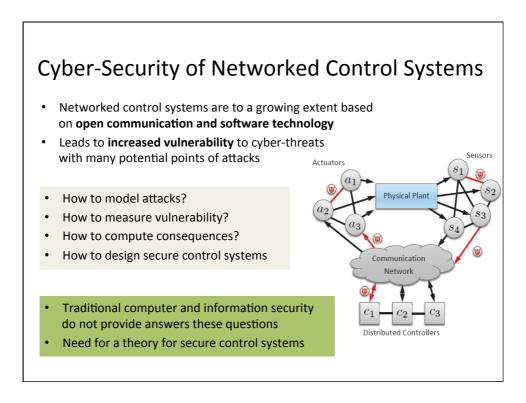




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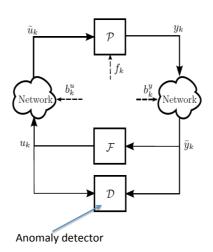


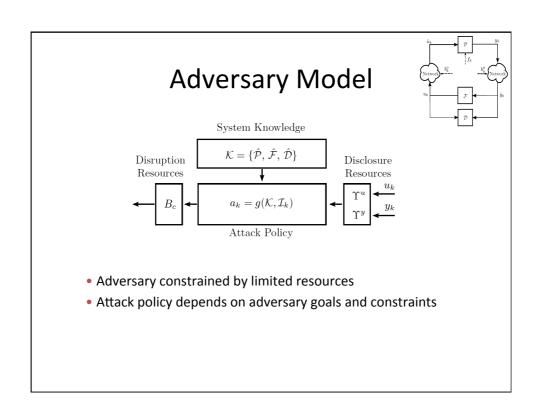


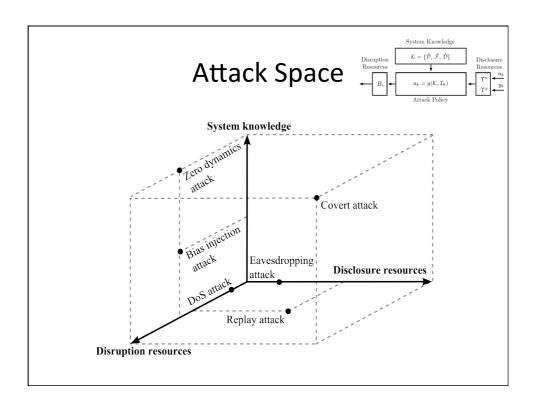


- Introduction
- Attack model for control systems
- Attack on power network state estimator
- Stealthy minimum-effort attacks
- Security index
- Conclusions
- Biography

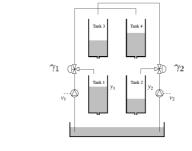
Networked Control System under Attack





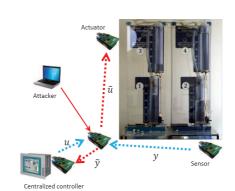






$$\frac{dx}{dt} \ = \ \begin{bmatrix} -\frac{1}{T_1} & 0 & \frac{A_3}{A_1T_3} & 0 \\ 0 & -\frac{1}{T_2} & 0 & \frac{A_4}{A_2T_4} \\ 0 & 0 & -\frac{1}{T_3} & 0 \end{bmatrix} x + \begin{bmatrix} \frac{\gamma_1k_1}{A_1} & 0 & 0 & 0 \\ 0 & \frac{\gamma_2k_2}{A_2} & 0 & 0 \\ 0 & 0 & 0 & -\frac{1}{T_4} & 0 \end{bmatrix} u$$

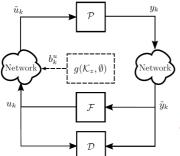
$$y \ = \ \begin{bmatrix} k_c & 0 & 0 & 0 \\ 0 & k_c & 0 & 0 \end{bmatrix} x$$



Quadruple-tank process has non-minimum-phase zero if $~0<\gamma_1+\gamma_2<1$

[J, 2000]

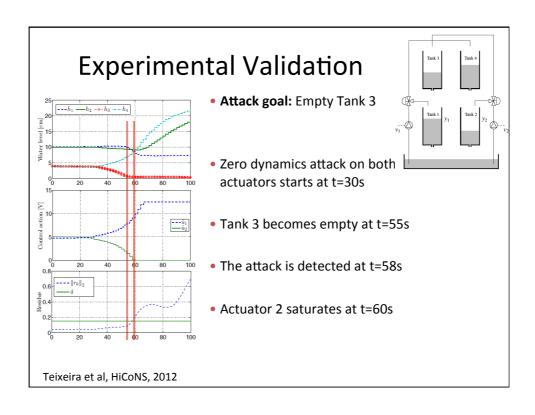
Zero Dynamics Attack



• Zero dynamics are characterized by:

$$\begin{bmatrix} \nu I - A & -B \\ C & 0 \end{bmatrix} \begin{bmatrix} x_0 \\ g \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \end{bmatrix}$$

- Suggests attack on actuators with policy: $a_k = g \nu^k$
- If the zero is unstable, then the plant state can be moved by this attack without detection
- Requires system knowledge (zero dynamics) but no disclosure resources



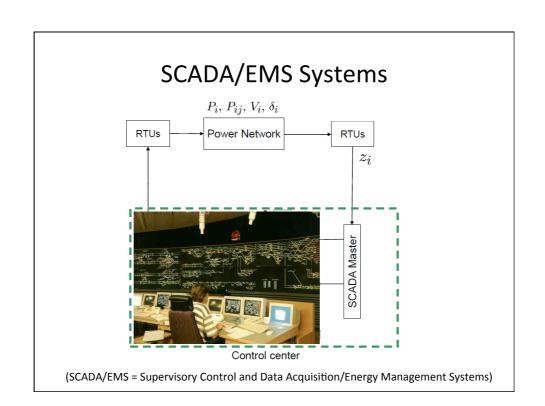
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Motivation

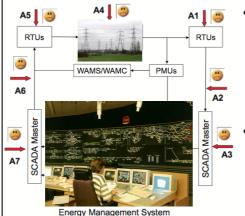
- Northeast blackout Aug 14, 2003: 55 million people affected
- Software bug in energy management system stalled alarms in state estimator for over an hour
- Cyber-attacks against the power network control systems with similar consequences pose a substantial threat







Attacks on Power Systems



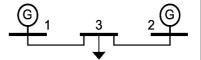
- Many attack opportunities
 - Sensor and actuators
 - Communication systems
 - Software systems (e.g., control)
 - Human operators
 - Physical infrastructure
- How strengthen the systems against cyber-attacks?

SCADA = Supervisory Control and Data Acquisition EMS = Energy Management System WAMS = Wide Area Monitoring System RTUs = Remote Terminal Units (Sensors/Actuators) PMUs = Phasor Measurement Units (Sensors)



(Static) Power Network Model

- · Local states at bus i:
 - θ_i phase angle
 - V_i voltage magnitude



• Active and reactive power injections:

$$\begin{array}{rcl} P_i &=& V_i \sum_{j \in N_i} V_j \left(G_{ij} \cos \theta_{ij} + B_{ij} \sin \theta_{ij} \right) \\ Q_i &=& V_i \sum_{j \in N_i} V_j \left(G_{ij} \sin \theta_{ij} - B_{ij} \cos \theta_{ij} \right) \end{array}$$

• Measurement model:

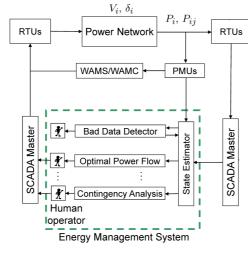
$$z = h(x) + \epsilon$$
 - $x \in \mathbb{R}^n$: network states - $z \in \mathbb{R}^m$: power flow

• Active and reactive power flows: measurements
$$P_{ij} = V_i^2(g_{si} + g_{ij}) - V_i V_j \left(g_{ij} \cos \theta_{ij} + b_{ij} \sin \theta_{ij}\right) - \epsilon : \text{measurement noise } Q_{ij} = -V_i^2(b_{si} + b_{ij}) - V_i V_j \left(g_{ij} \sin \theta_{ij} - b_{ij} \cos \theta_{ij}\right)$$
 where

$$\theta_{ij} = \theta_i - \theta_j$$

Static model because the power grid time constant ~10 ms is beyond existing measurement technology. Typical sampling time ~1 s.

Energy Management System for Power Networks



WAMC = Wide Area Monitoring and Control System

RTUs = Remote Terminal Units (Sensors/Actuators)

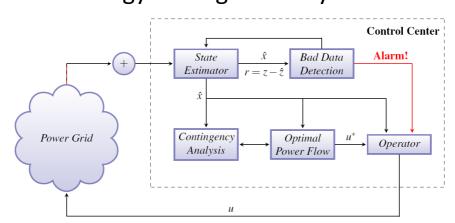
- SCADA-EMS provides power network state information to
 - Identify faulty equipment
 - Optimize power flows
 - Analyze reliability (contingency)
 - Etc
- Large system with slow sampling
 - 100-1 000's of RTUs sampled in sec's
 - 10K-40K measurements
- · Decisions taken by human operators

Remark

New WAMCs based on high-rate PMUs are better protected but constitute only a small portion of the overall network

PMUs = Phasor Measurement Units (Sensors)

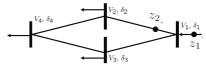
Energy Management System



- The state estimator has a crucial role in the EMS
- If the bad data detector identifies a faulty sensor, the corresponding measurement is removed from the state estimator
- Bad data detection is typically done under the assumption of uncorrelated faults, which does not hold for intelligent attacks

State Estimator

• Steady-state models:



$$\begin{pmatrix} z_1 \\ z_2 \end{pmatrix} = \begin{pmatrix} \frac{V_1 V_2}{X_{12}} \sin(\delta_1 - \delta_2) + \frac{V_1 V_3}{X_{13}} \sin(\delta_1 - \delta_3) \\ \frac{V_1 V_2}{X_{12}} \sin(\delta_1 - \delta_2) \end{pmatrix} + \begin{pmatrix} e_1 \\ e_2 \end{pmatrix} = h(x) + e \in \mathbb{R}^m$$

• WLS estimates of bus phase angles δ_i (in vector \widehat{x}):

$$\hat{x}^{k+1} = \hat{x}^k + (H_k^T R^{-1} H_k)^{-1} H_k^T R^{-1} (z - h(\hat{x}^k))$$

$$H_k := \frac{\partial h}{\partial x} (\hat{x}_k) \qquad R := \mathbf{E} e e^T$$

• Linear DC approximation (≈ ML estimate):

$$\hat{x} = (H^T R^{-1} H)^{-1} H^T R^{-1} z$$
 $H := \frac{\partial h(x)}{\partial x} \Big|_{x=0}$

E.g., [Schweppe and Wildes, 1970; Abur and Exposito, 2004]

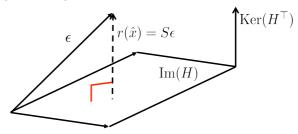
Bad Data Detector

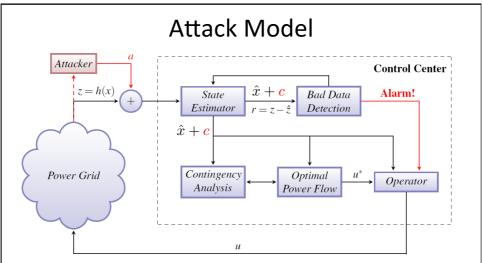
$$H = \left. \frac{\partial h(x)}{\partial x} \right|_{x = \hat{x}}$$

• Today's BDD is based on measurement residual $\,r(\hat{x}) = z - h(\hat{x})\,$

$$\|Wr(\hat{x})\|_p \lesssim_{H_1}^{H_0} \tau$$

- For the Gauss-Newton method: $r(\hat{x}) \approx (I H(H^{\top}H)^{-1}H^{\top})\epsilon = S\epsilon$
- Note that $S = \mathbf{P}_{\mathrm{Ker}(H^\top)}$ is the orthogonal projection onto $\mathrm{Ker}(H^\top)$
- Can be exploited by an attacker

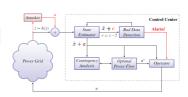




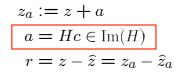
- Scenario: Attacker injects malicious data a to corrupt analog measurements in the power grid, in order to change state estimates without generating bad data detection alarm
- How characterize the set of undetectable malicious data α?

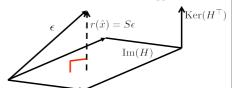
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Bad-Data Detection and Stealthy Attacks



- Bad-data detection trigger alarm when residual r is large $r:=z-\hat{z}=z-H\hat{x}=z-H(H^TR^{-1}H)^{-1}H^TR^{-1}z$
- Characterization of undetectable malicious data $oldsymbol{a}$





- The attacker has a lot of freedom in the choice of a!
- Attacker likely to seek sparse solutions α , i.e., manipulate only few measurements

[Liu et al., 2009]

Stealthy Minimum-Effort Attack

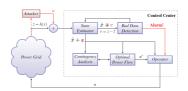
ullet Attack single measurement $\,z_k\,$

$$\min_{a} \|a\|_{2}$$
s.t. $a \in \mathcal{U} \cap \mathcal{G}_{k} \cap \mathcal{C}$

$$-\mathcal{U} = \operatorname{Im}(H)$$

$$-\mathcal{G}_{k} = \{a \in \mathbb{R}^{m} : a_{k} = 1\}$$

$$-\mathcal{C} = \mathbb{R}^{m}$$



Optimal attack

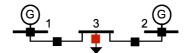
$$a^* = K_{kk}^{-1} K e_k$$

$$K = H H^\dagger$$

- a^* is typically not sparse, so many sensors need to be corrupted
- Consider 0-norm instead of 2-norm

Stealthy Minimum-Effort Attack

$$\min_{a} ||a||_{0}$$
 s.t. $a \in \mathcal{U} \cap \mathcal{G}_{k} \cap \mathcal{C}$



- ullet P_3 is the target measurement
- A few possible attacks:
 - $\{P_3\}$, $\{P_3, \star\}$ not stealthy $\{P_1, P_{13}, P_3\}$ minimum $\{P_2, P_{23}, P_3\}$ effort $\{P_1, P_{13}, P_3, P_{23}, P_2\}$

Security Index ρ_k

• Security index for measurement k: $ho_k = \|a^*\|_0$

- a^{*} is the optimal solution of

$$\min_{a} \|a\|_0$$

s.t.
$$a \in \mathcal{U} \cap \mathcal{G}_k \cap \mathcal{C}$$

$$-\mathcal{G}_k = \{ a \in \mathbb{R}^m : a_k = 1 \}$$

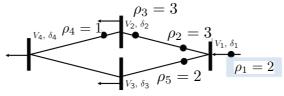
Stealthy Corrupted

$$\begin{aligned}
& \mathcal{U} = \operatorname{Im}(H) \\
& \mathcal{G}_k = \{ a \in \mathbb{R}^m : a_k = 1 \} \\
& \mathcal{C} = \{ a \in \mathbb{R}^m : a_i = 0 \quad \forall i \in \mathcal{P} \}
\end{aligned}$$

Protected

ullet ho_k is the minimum number of measurements to manipulate for a successful attack

Example



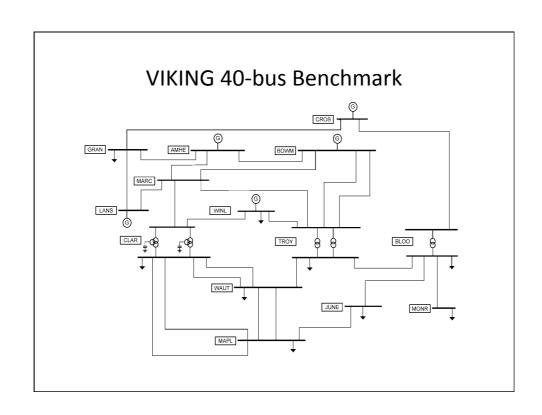
Sparse attack corresponding to $ho_{\it k}$:

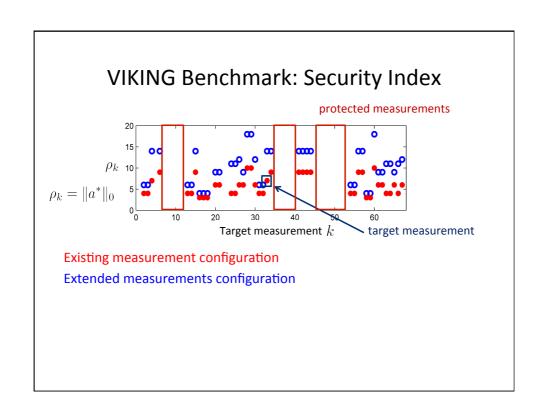
$$(a_1 \ a_2 \ a_3 \ a_4 \ a_5) = \begin{pmatrix} 1 & 1 & -1 & 0 & 1 \\ 0 & 1 & -1 & 0 & 0 \\ 0 & -1 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 \\ 1 & 0 & 0 & 0 & 1 \end{pmatrix}$$

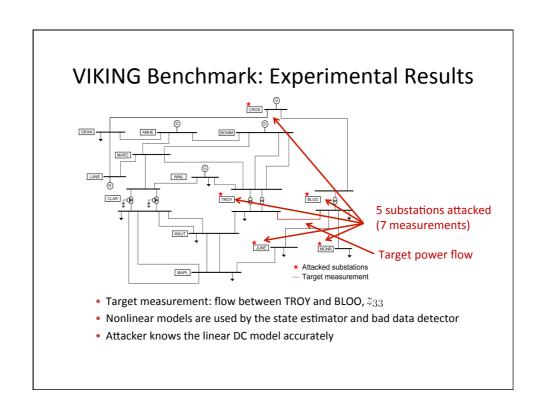
Compare with the "hat matrix":
$$\begin{pmatrix}
\hat{z}_1 \\
\hat{z}_2 \\
\hat{z}_3 \\
\hat{z}_4 \\
\hat{z}_5
\end{pmatrix} = \begin{pmatrix}
0.60 & 0.20 & -0.20 & 0 & 0.40 \\
0.20 & 0.40 & -0.40 & 0 & -0.20 \\
-0.20 & -0.40 & 0.40 & 0 & 0.20 \\
0 & 0 & 0 & 1.00 & 0 \\
0.40 & -0.20 & 0.20 & 0 & 0.60
\end{pmatrix} \begin{pmatrix}
z_1 \\
z_2 \\
z_3 \\
z_4 \\
z_5
\end{pmatrix}$$

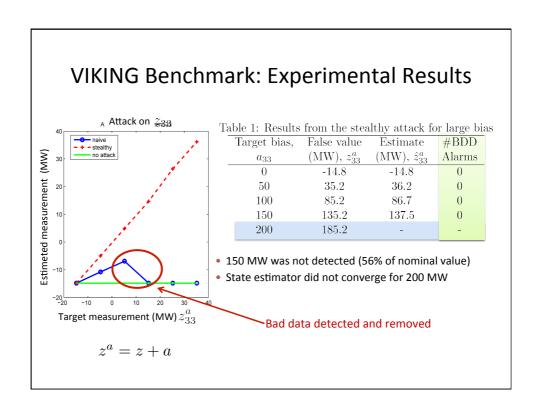
$$= H(H^T R^{-1} H)^{-1} H R^{-1}$$

Hat matrix misleading for judging sparsity of attacks!







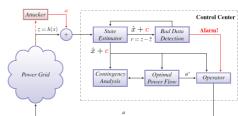


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Conclusions

- Cyber-attack models for networked control systems
- Undetectable false-data attack against power systems state estimator possible, both in theory and practice
- New **security index** ρ_k to estimate vulnerabilities
- Suggests locations of counter measures
- Many open problems in secure networked control theory





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