Virtual memory - Swapping

Johan Montelius

KTH

2021

Virtual memory

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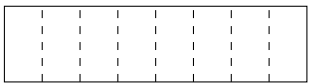
Pages can be temporarily stored in secondary memory i.e. on disk.

Processes

Processes in virtual space



Small physical memory

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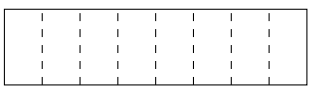

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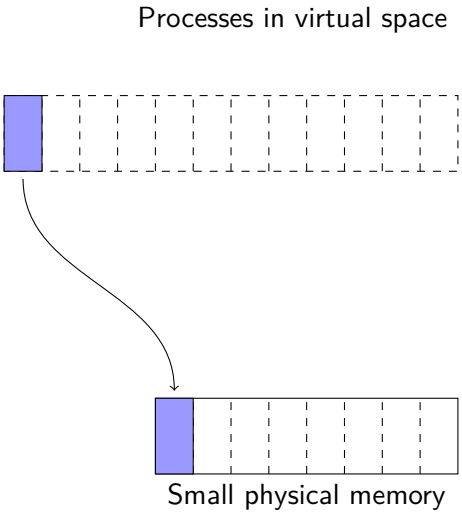

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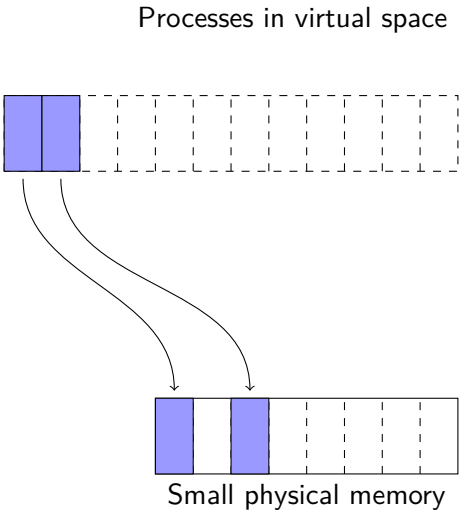

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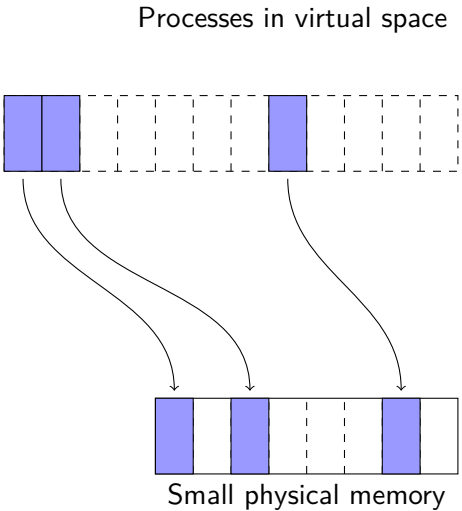

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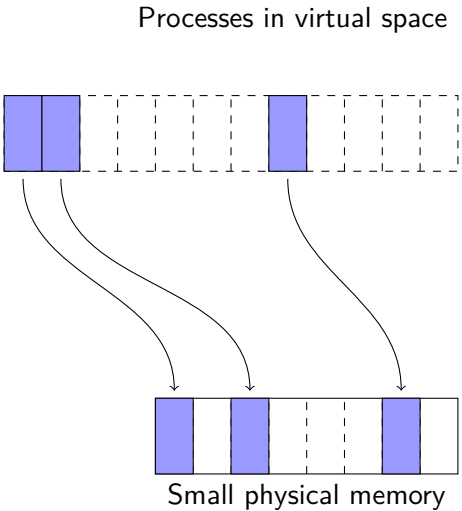

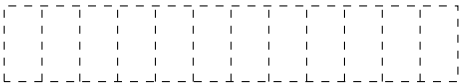

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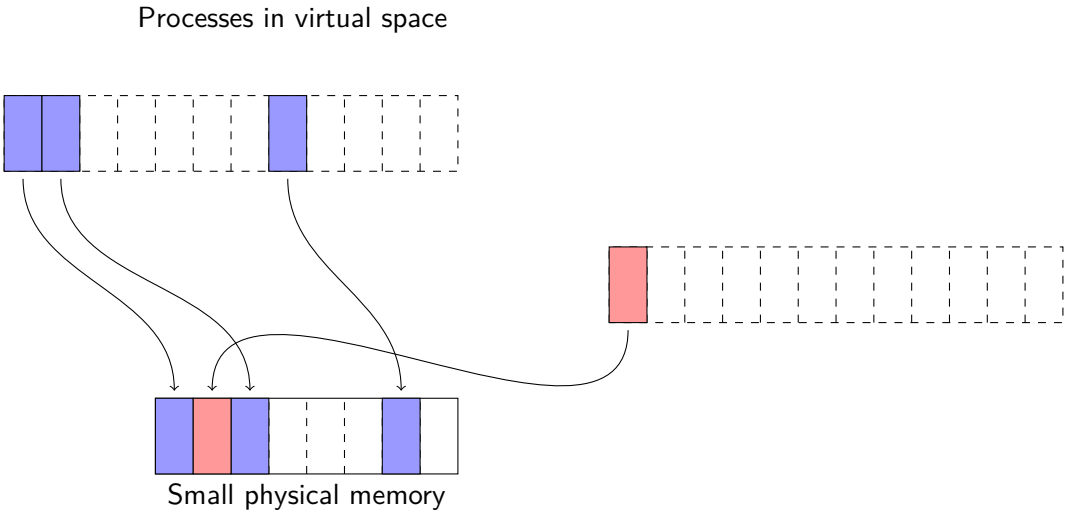

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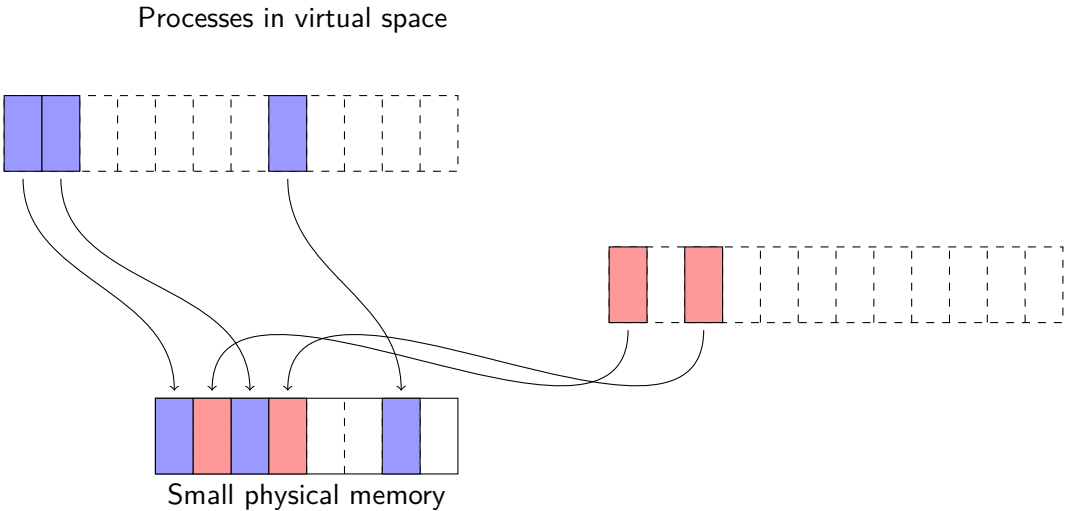

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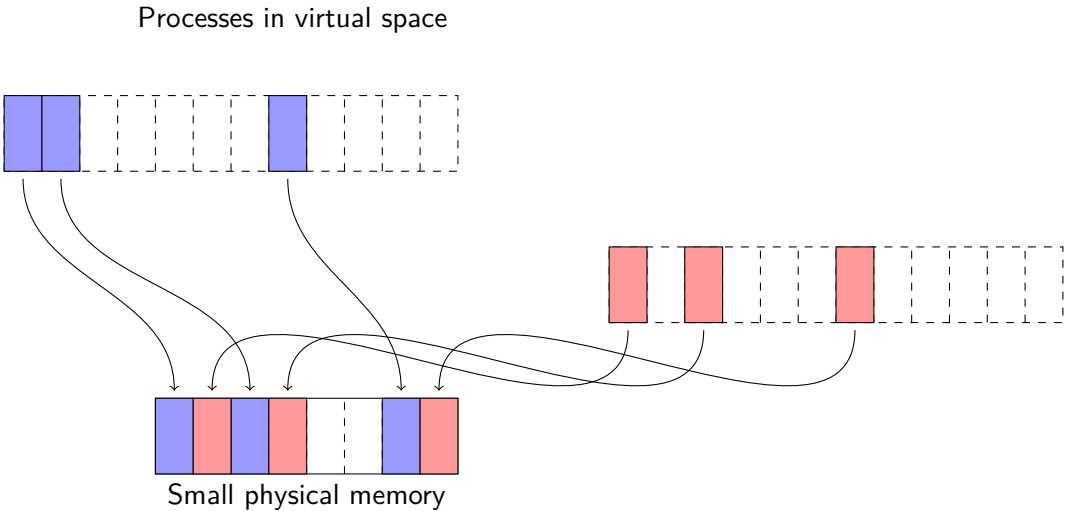

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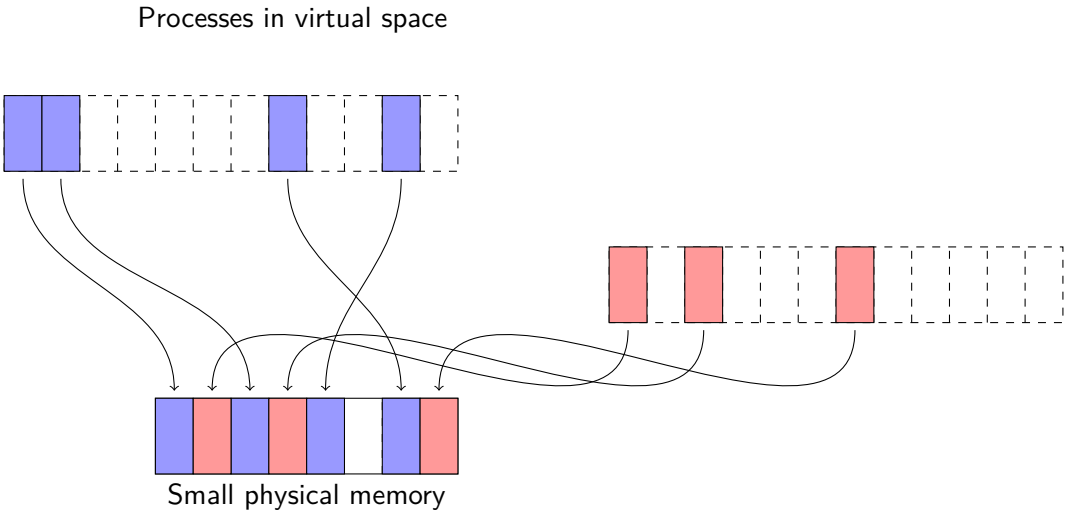

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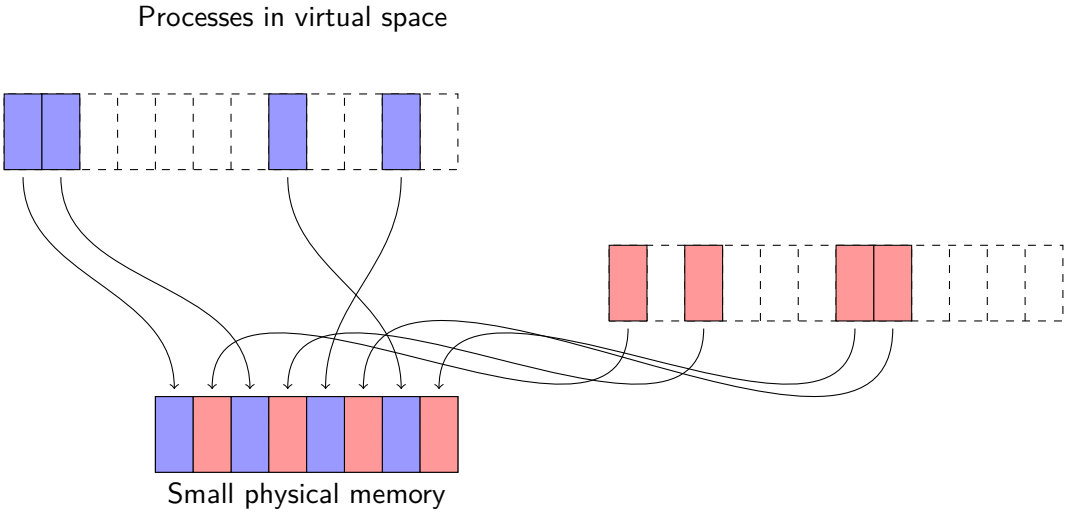

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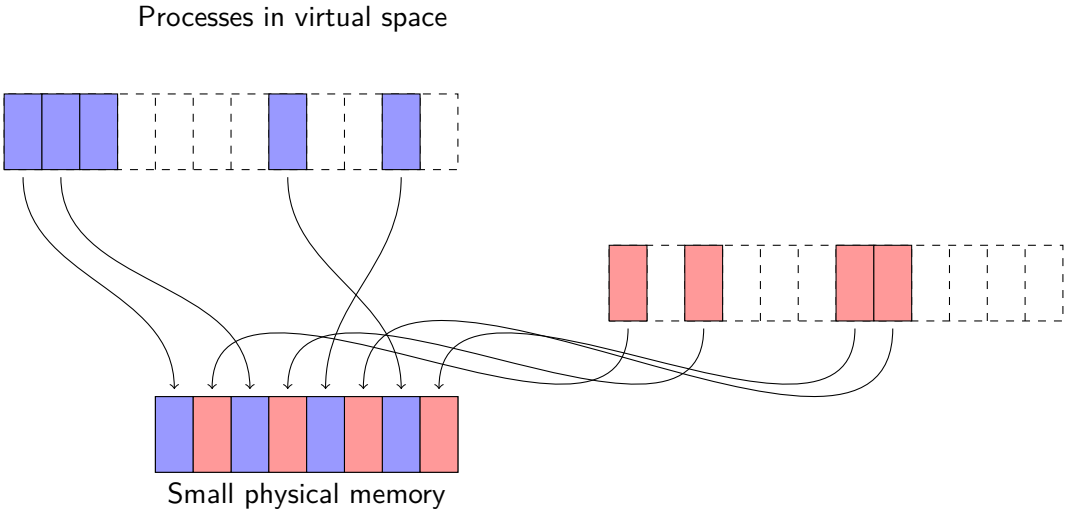

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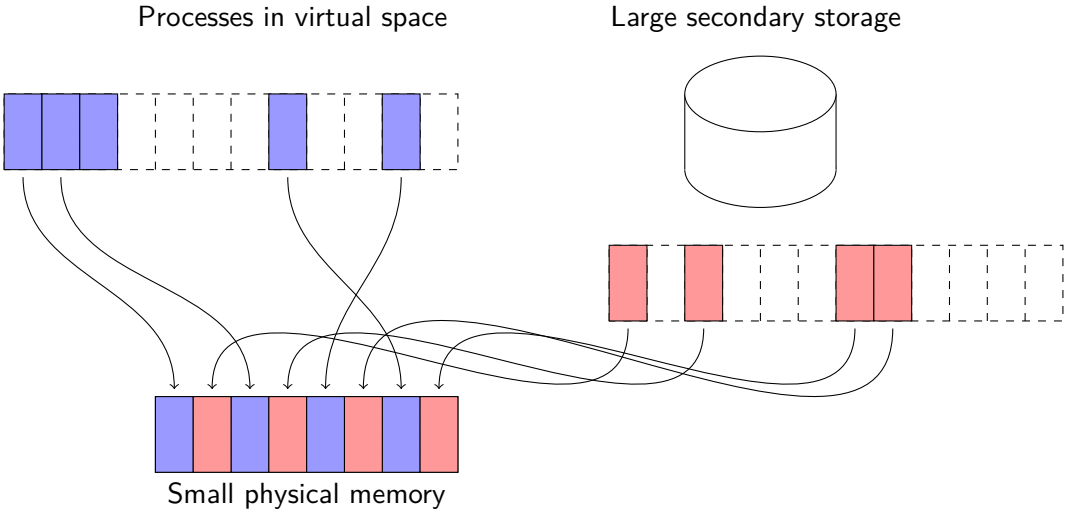
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Small physical memory

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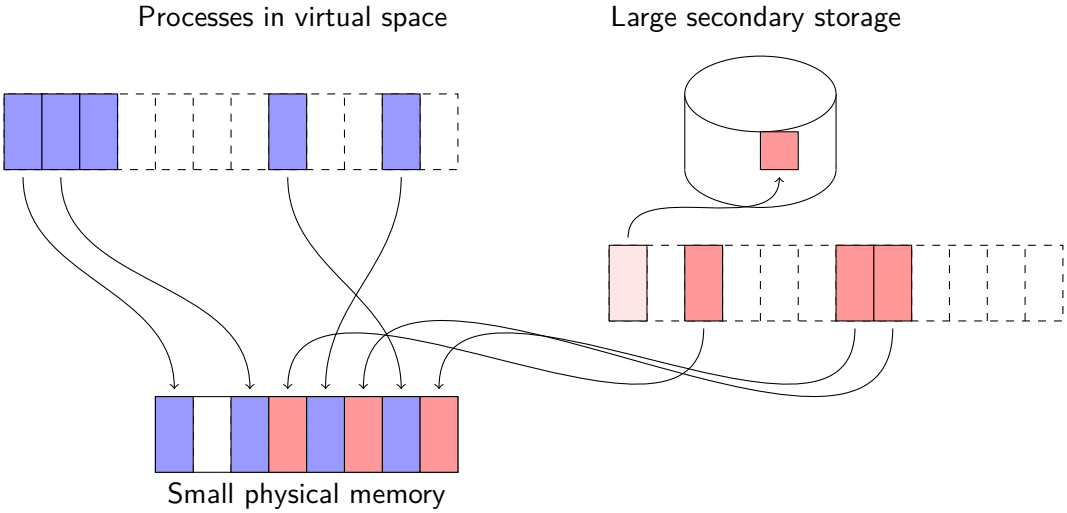
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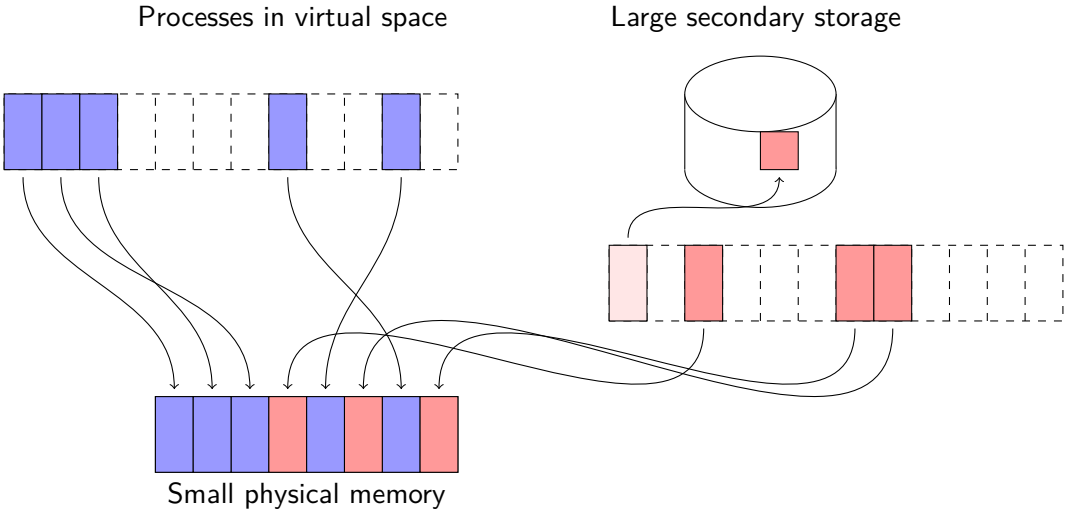
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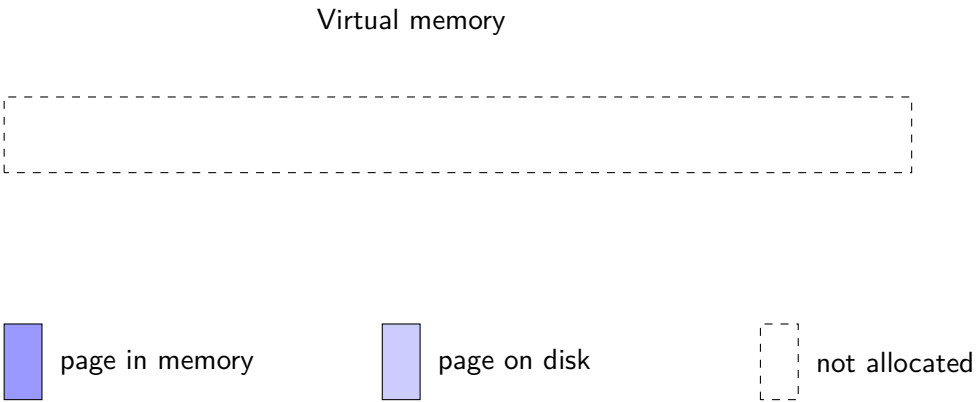

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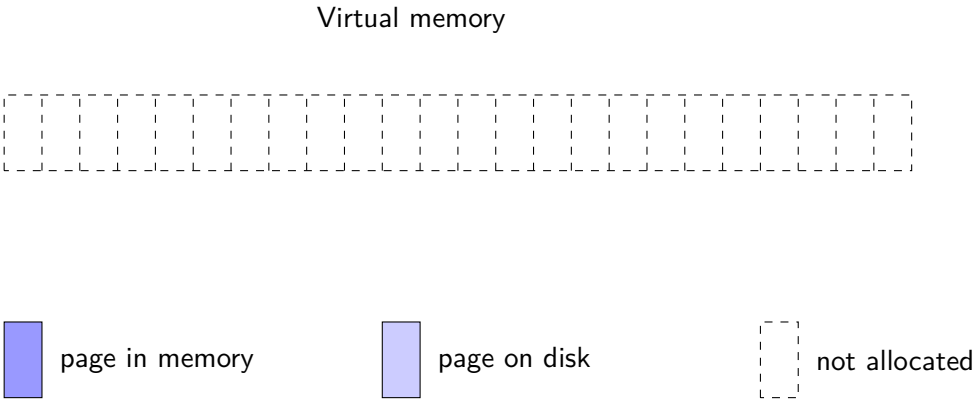

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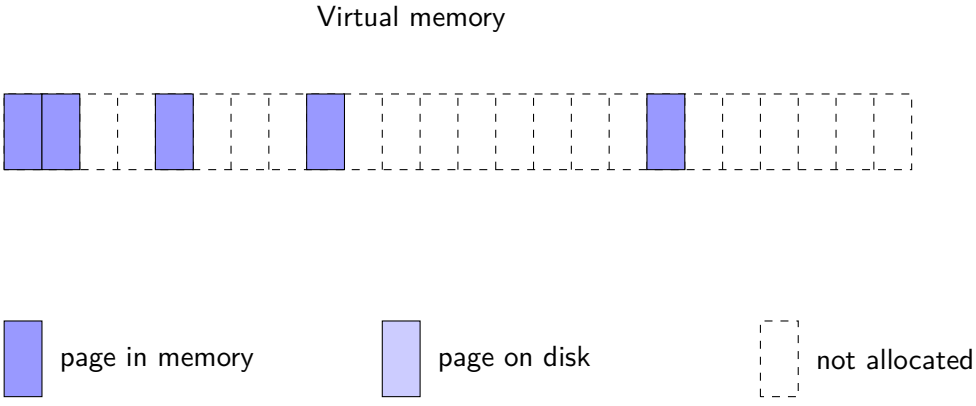

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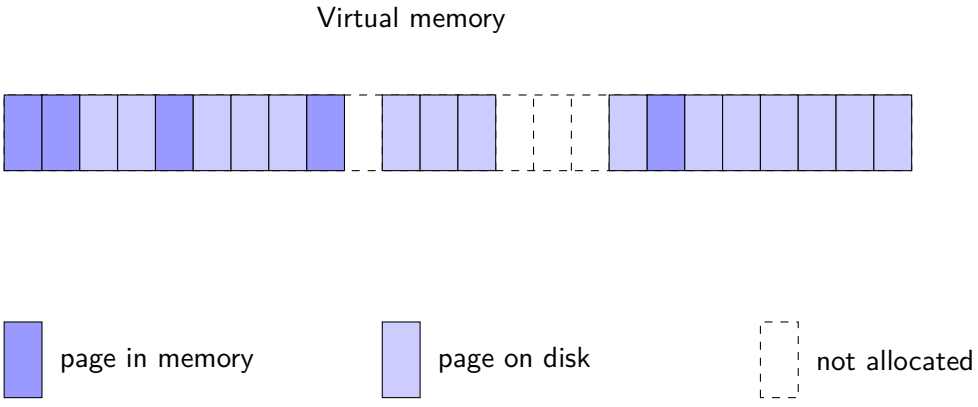

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- Who should do all this, hardware or operating system?

The page table entry (PTE)

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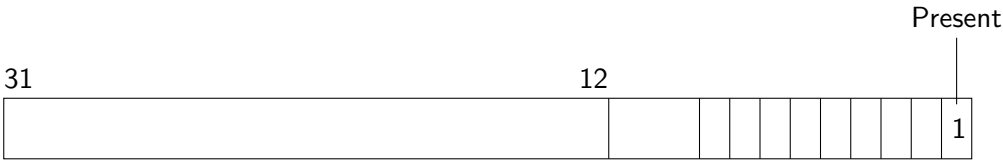

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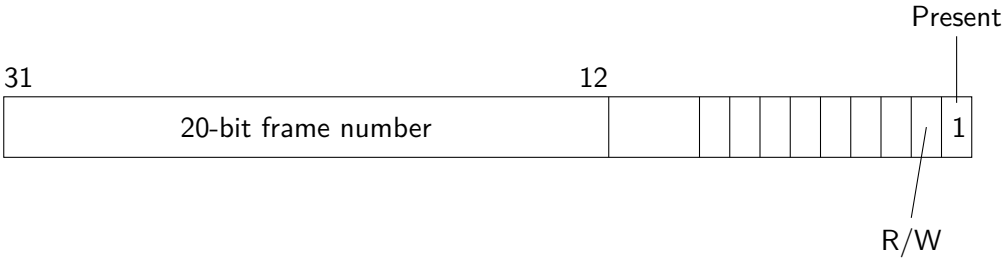

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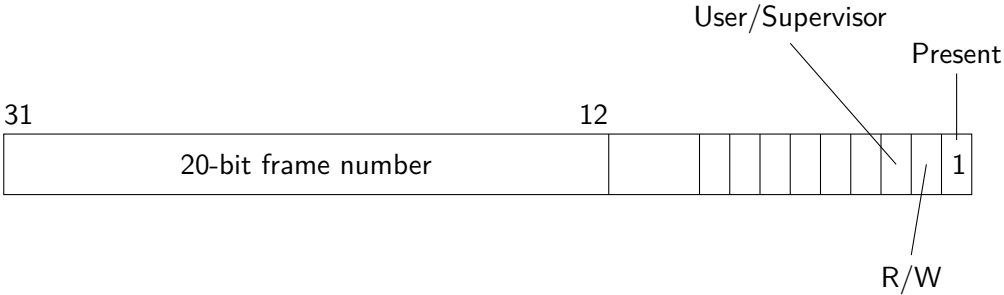

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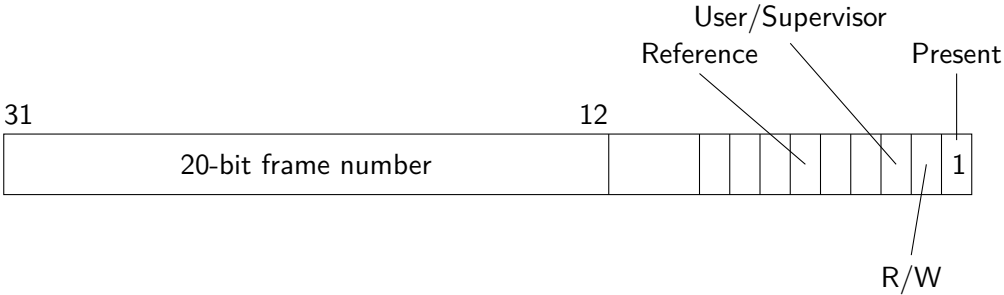

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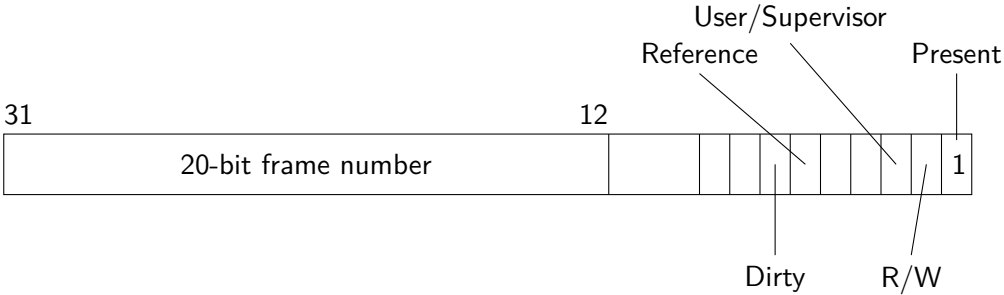

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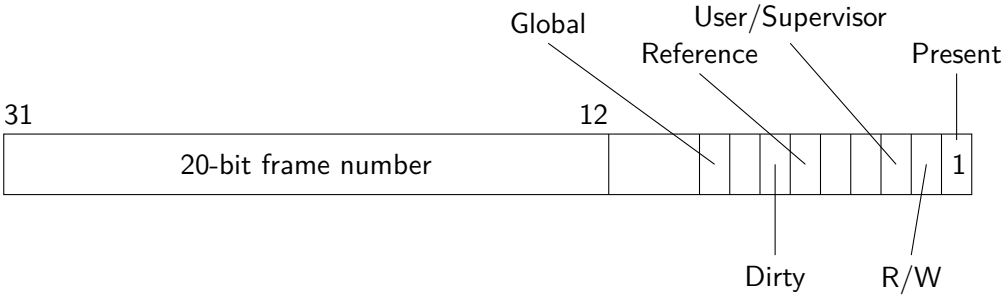

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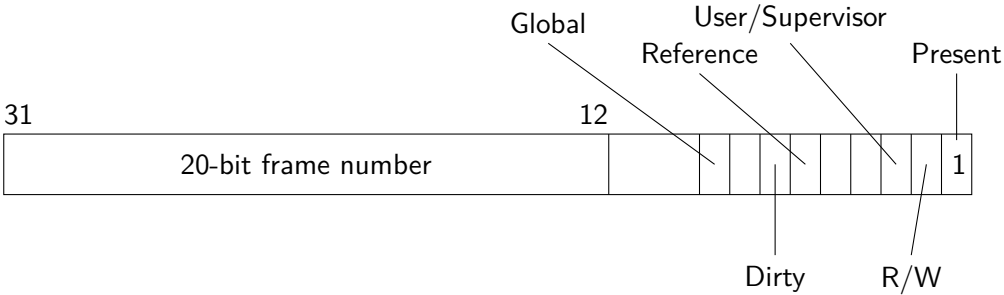

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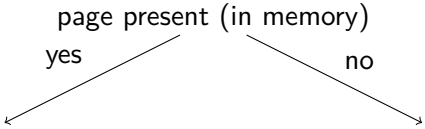
Page faults



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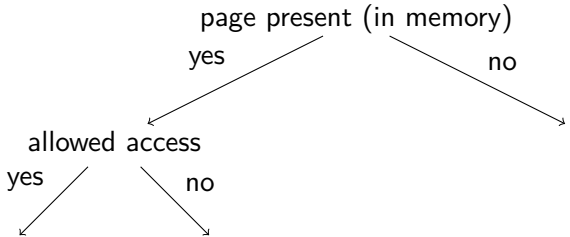

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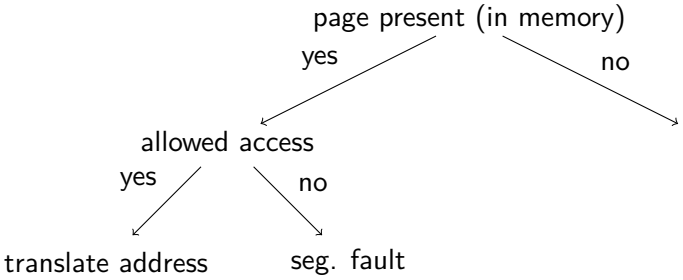
page present (in memory)
yes
no
allowed access
yes
no
translate address
seg. fault

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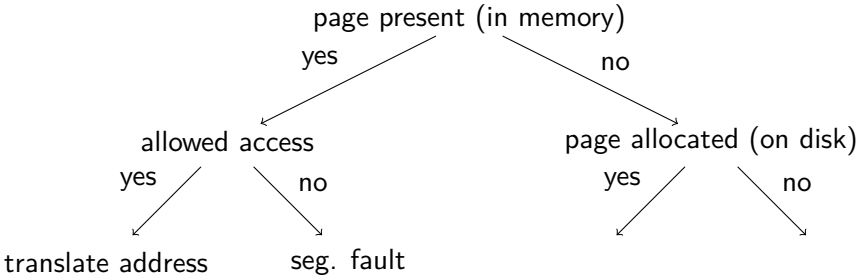
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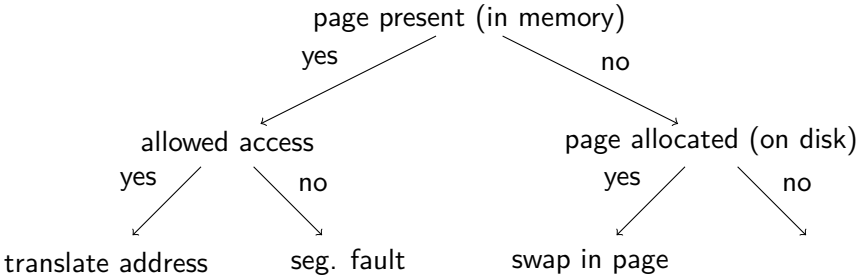
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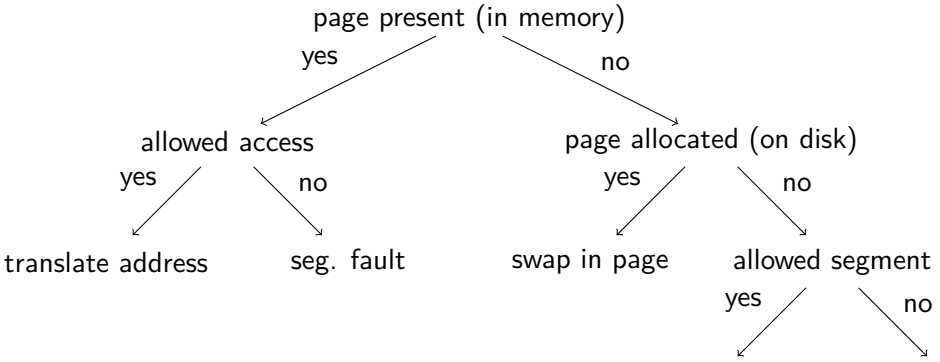
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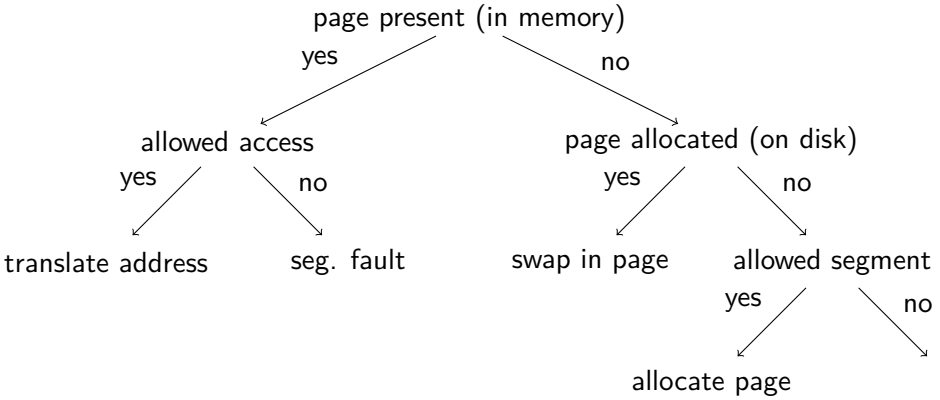
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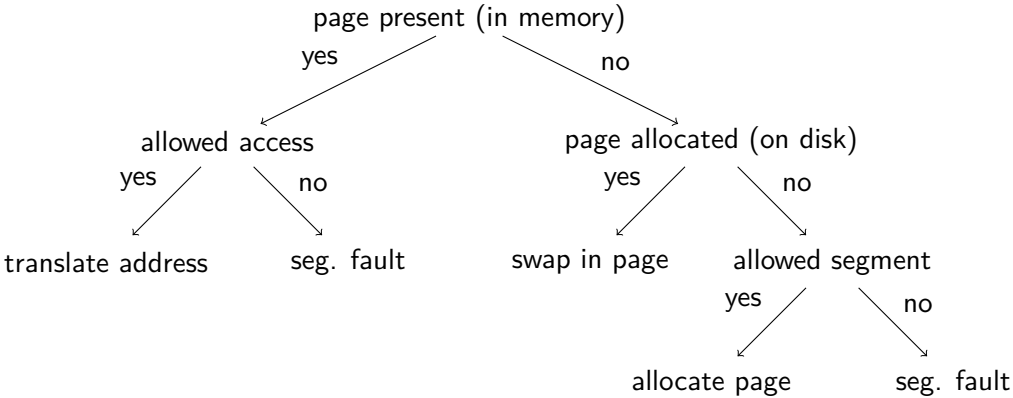
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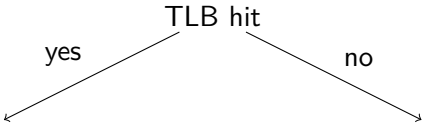

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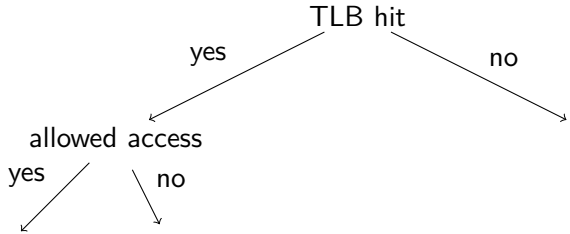

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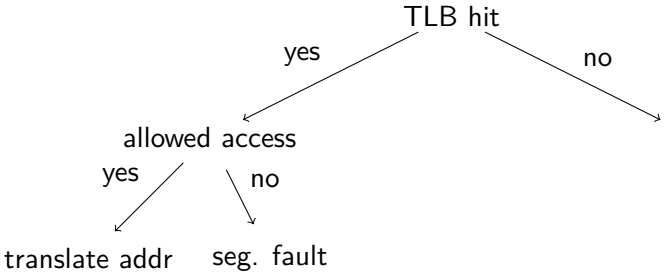

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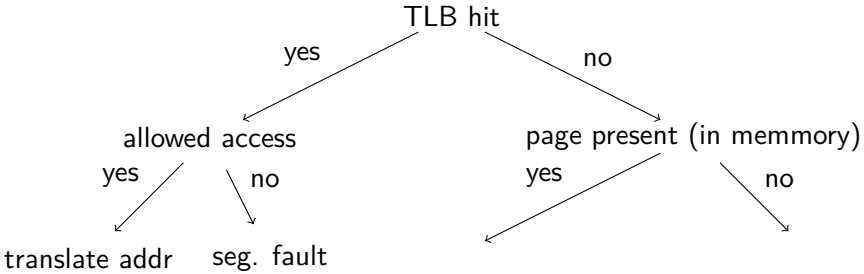

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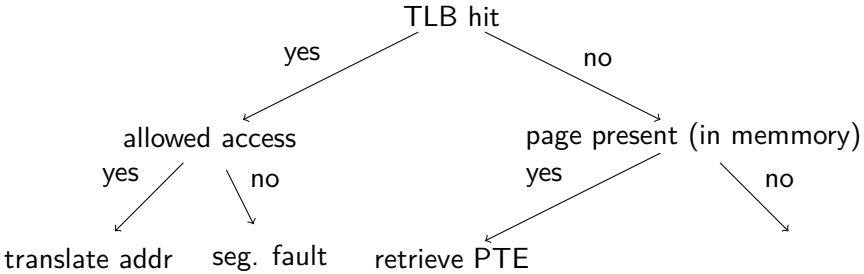

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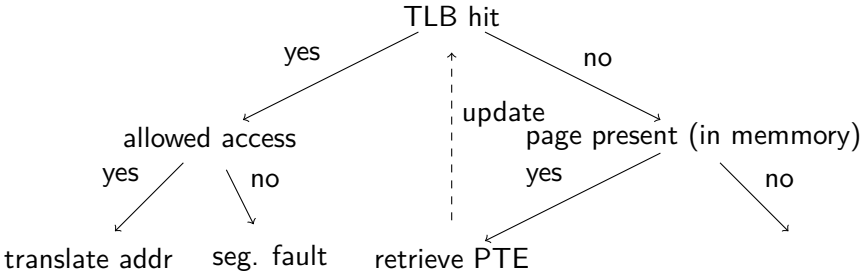

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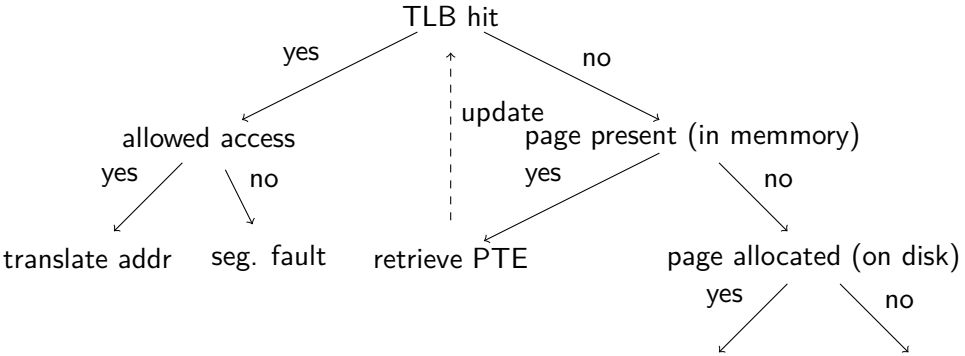

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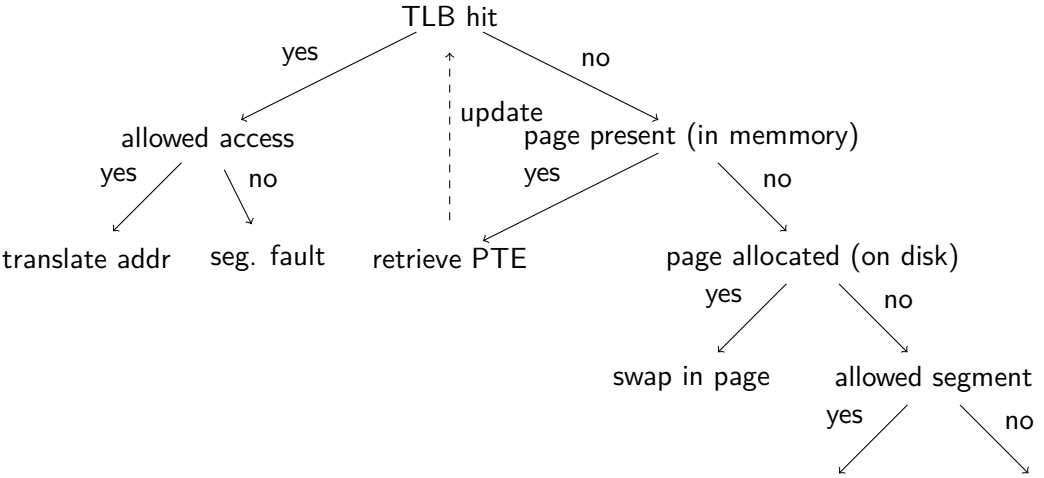

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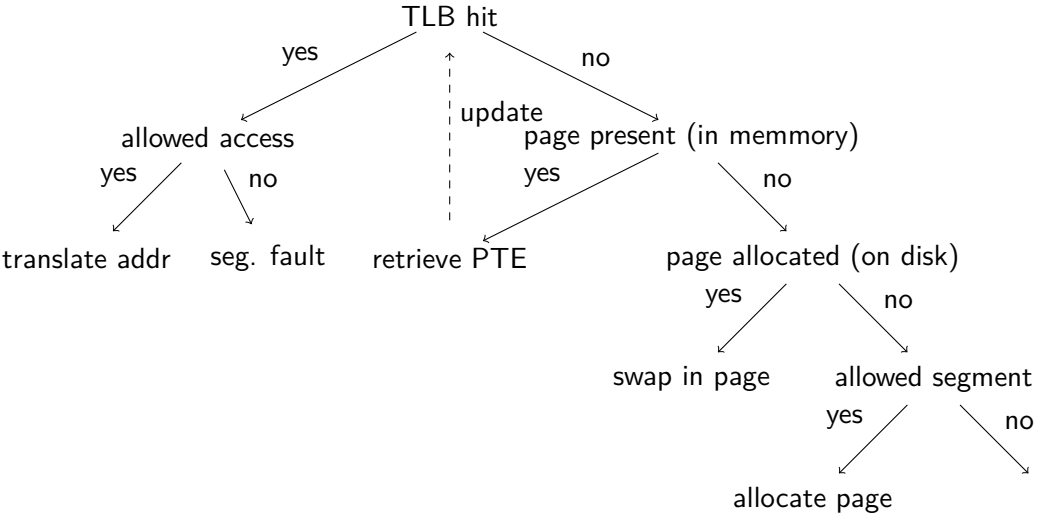

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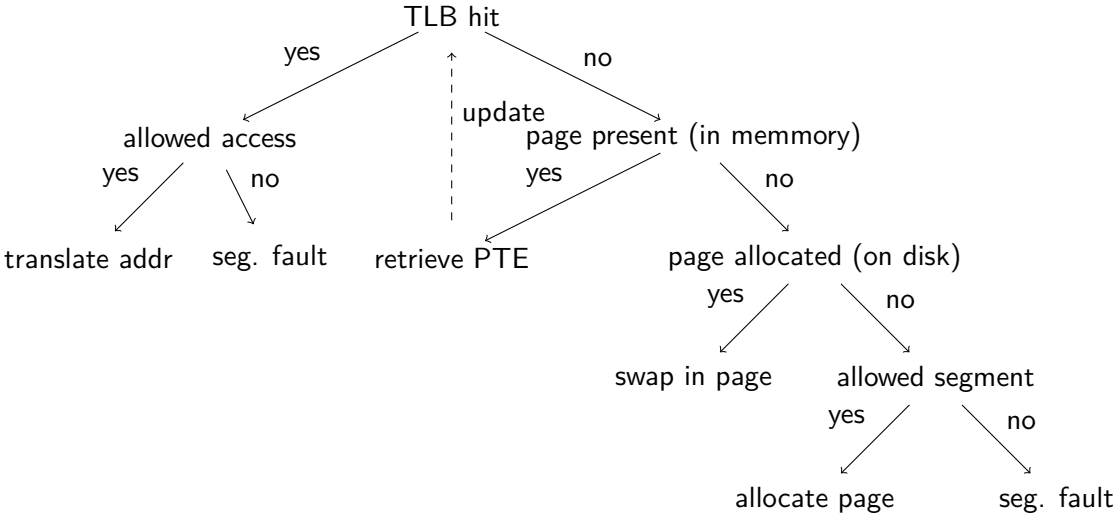

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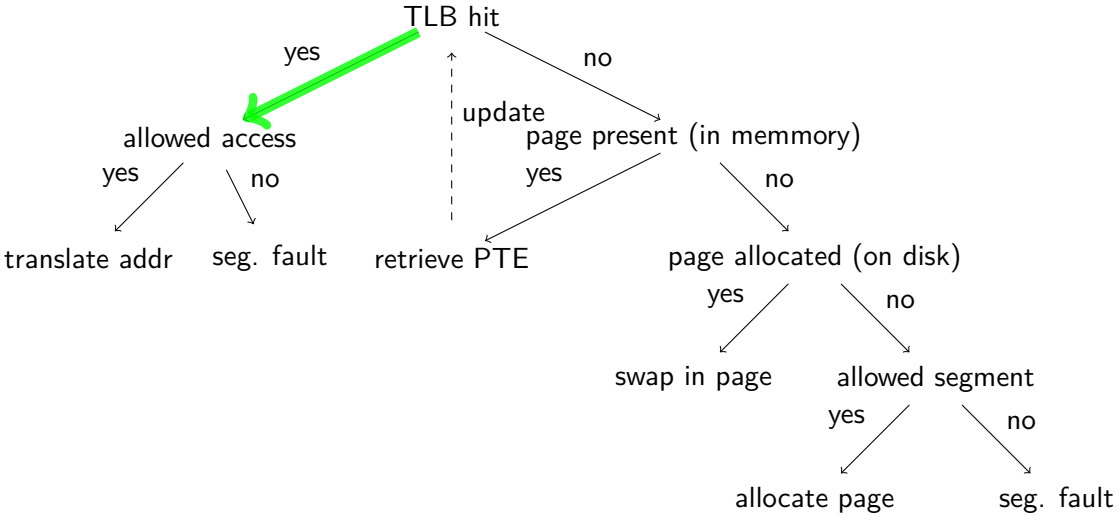

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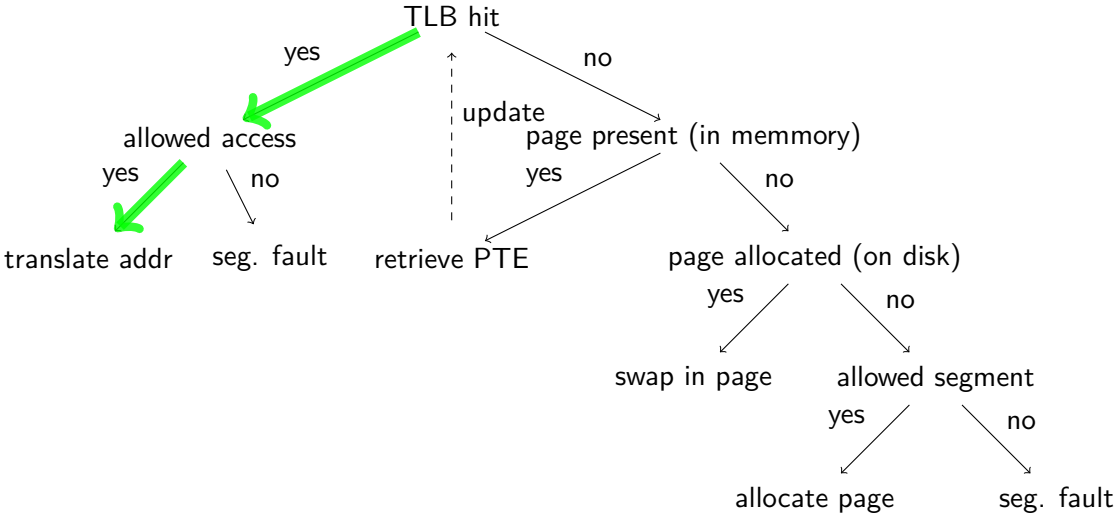

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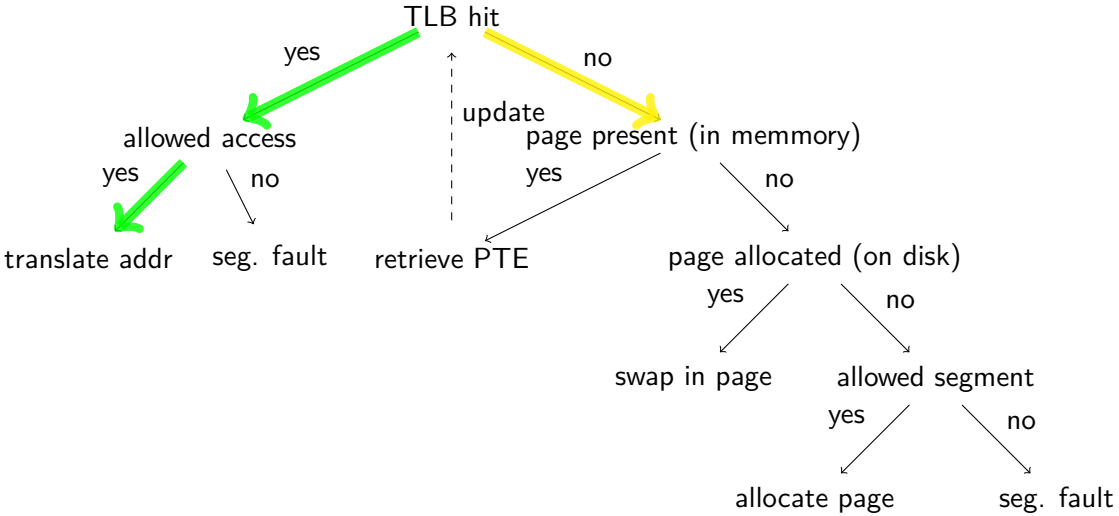

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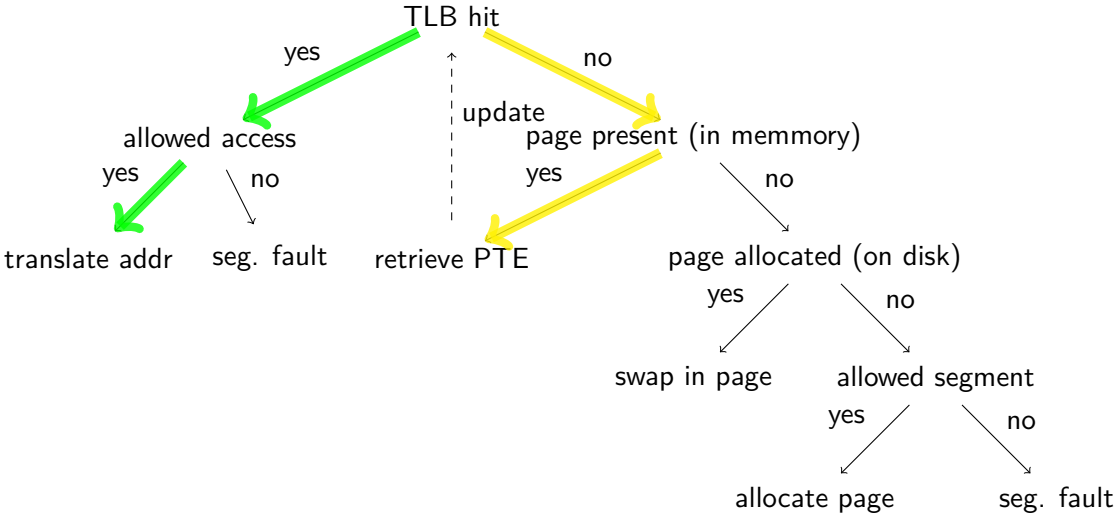

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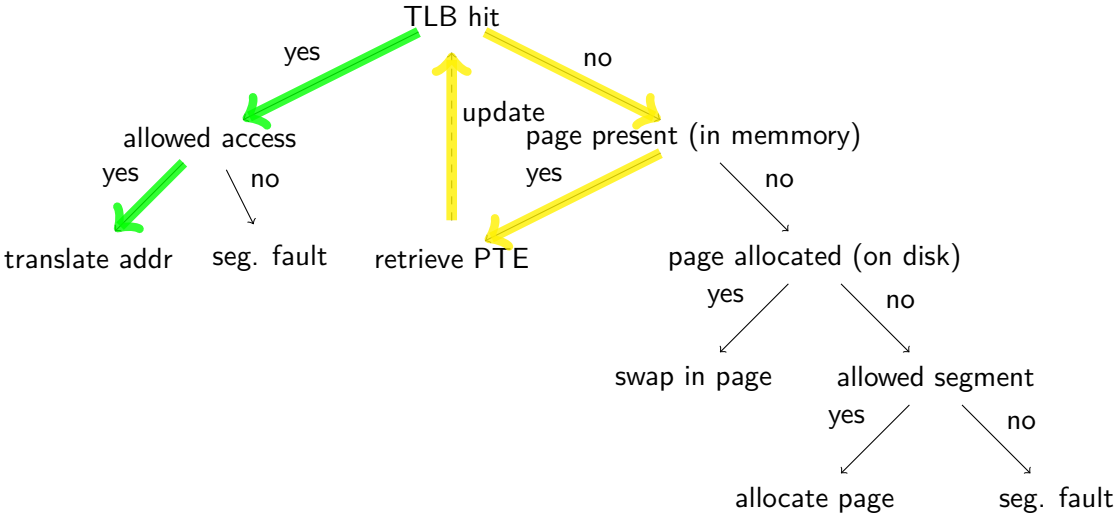

The operating system

The operating system keeps track of all processes and maintains:

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- Which segments are allowed.

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- Which segments are allowed.
- Read/write access.

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- Which segments are allowed.
- Read/write access.
- User/Supervisor mode.

The operating system keeps track of all processes and maintains:

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- Which segments are allowed.
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- Copy on write.

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The operating system keeps track of all processes and maintains:

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- Which segments are allowed.
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a page table

The operating system

The operating system keeps track of all processes and maintains:

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a page table

- Which pages are allocated?

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- Which pages are allocated?
- Physical frames of pages or
- .. location on secondary storage.

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- Modified, accessed, cacheable...

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a page table

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The cost of page faults

The cost of memory access:

- TLB hit, address found in cache: $\sim 1ns$

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Retrieving from disk is a factor 100.000 times more expensive than finding things in memory.

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Retrieving from disk is a factor 100.000 times more expensive than finding things in memory.

What can we do while we're waiting?

Replacement policy

The problem with caching - which item do we throw out when the cache is filled?

Replacement policy

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Why try to be smart - pick a page by random.

Replacement policy

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Why try to be smart - pick a page by random.

Replacement policy

The problem with caching - which item do we throw out when the cache is filled?

Why try to be smart - pick a page by random.

Are pages referenced randomly?

Locality of references

Memory references are not random in space nor time.

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- **Temporal locality**: an address that has been referenced is likely to be referenced soon again.
- **Spatial locality**: an address that is close to something that has been referenced is likely to be referenced.

Locality of references

Memory references are not random in space nor time.

- **Temporal locality**: an address that has been referenced is likely to be referenced soon again.
- **Spatial locality**: an address that is close to something that has been referenced is likely to be referenced.

In these benchmarks we have simulated locality by assuming that 20% of the pages are access 80% of the time.

The random policy

When the memory is full select a frame by random and move it to disk.

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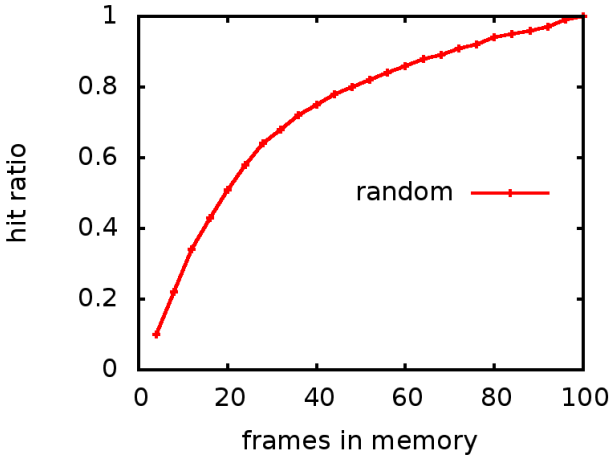

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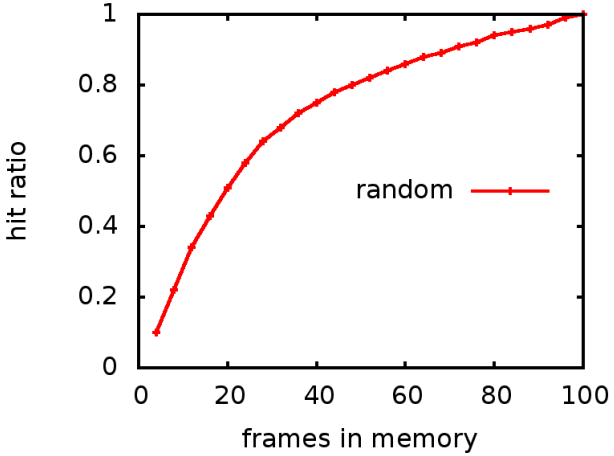

Is this good?

We can do better!

- When you need to throw out a page, select the one that will be used *the furthest in the future*.

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- page references: 0,1,2,3,0,2,3,1,2,0,3,0

We can do better!

access	hit/miss	evict	memory
0			

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access	hit/miss	evict	memory
0	miss	-	0

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We can do better!

access	hit/miss	evict	memory
0	miss	-	0
1			

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0	miss	-	0
1	miss	-	0,1

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access	hit/miss	evict	memory
0	miss	-	0
1	miss	-	0,1
2			

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access	hit/miss	evict	memory
0	miss	-	0
1	miss	-	0,1
2	miss	-	0,1,2

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access	hit/miss	evict	memory
0	miss	-	0
1	miss	-	0,1
2	miss	-	0,1,2
3			

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0			

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access	hit/miss	evict	memory
0	miss	-	0
1	miss	-	0,1
2	miss	-	0,1,2
3	miss	1	0,3,2
0	hit		0,3,2

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access	hit/miss	evict	memory
0	miss	-	0
1	miss	-	0,1
2	miss	-	0,1,2
3	miss	1	0,3,2
0	hit		0,3,2
2			

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0	miss	-	0
1	miss	-	0,1
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0	hit		0,3,2
2	hit		0,3,2

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0	hit		0,3,2
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3			

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2	hit		0,3,2
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3	hit		0,3,2
1			

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1	miss	-	0,1
2	miss	-	0,1,2
3	miss	1	0,3,2
0	hit		0,3,2
2	hit		0,3,2
3	hit		0,3,2
1	miss	3	0,1,2

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0	miss	-	0
1	miss	-	0,1
2	miss	-	0,1,2
3	miss	1	0,3,2
0	hit		0,3,2
2	hit		0,3,2
3	hit		0,3,2
1	miss	3	0,1,2
2			

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1	miss	-	0,1
2	miss	-	0,1,2
3	miss	1	0,3,2
0	hit		0,3,2
2	hit		0,3,2
3	hit		0,3,2
1	miss	3	0,1,2
2	hit		0,1,2

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3	miss	1	0,3,2
0	hit		0,3,2
2	hit		0,3,2
3	hit		0,3,2
1	miss	3	0,1,2
2	hit		0,1,2
0			

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0	miss	-	0
1	miss	-	0,1
2	miss	-	0,1,2
3	miss	1	0,3,2
0	hit		0,3,2
2	hit		0,3,2
3	hit		0,3,2
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2	hit		0,1,2
0	hit		0,1,2

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1	miss	-	0,1
2	miss	-	0,1,2
3	miss	1	0,3,2
0	hit		0,3,2
2	hit		0,3,2
3	hit		0,3,2
1	miss	3	0,1,2
2	hit		0,1,2
0	hit		0,1,2
3			

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0	miss	-	0
1	miss	-	0,1
2	miss	-	0,1,2
3	miss	1	0,3,2
0	hit		0,3,2
2	hit		0,3,2
3	hit		0,3,2
1	miss	3	0,1,2
2	hit		0,1,2
0	hit		0,1,2
3	miss	1	0,3 2

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0	miss	-	0
1	miss	-	0,1
2	miss	-	0,1,2
3	miss	1	0,3,2
0	hit		0,3,2
2	hit		0,3,2
3	hit		0,3,2
1	miss	3	0,1,2
2	hit		0,1,2
0	hit		0,1,2
3	miss	1	0,3 2
0			

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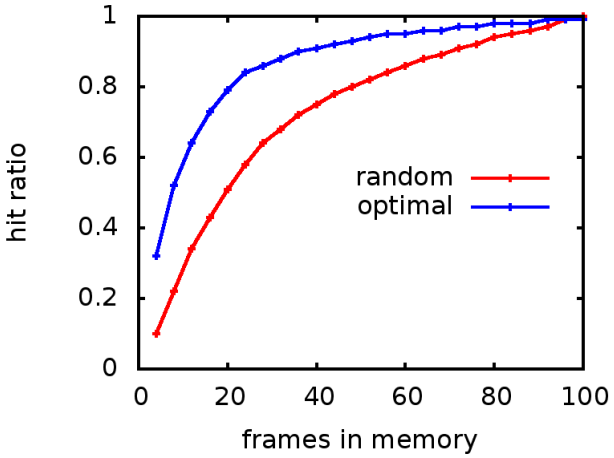
access	hit/miss	evict	memory
0	miss	-	0
1	miss	-	0,1
2	miss	-	0,1,2
3	miss	1	0,3,2
0	hit		0,3,2
2	hit		0,3,2
3	hit		0,3,2
1	miss	3	0,1,2
2	hit		0,1,2
0	hit		0,1,2
3	miss	1	0,3 2
0	hit		0,1 2

Optimal replacement policy



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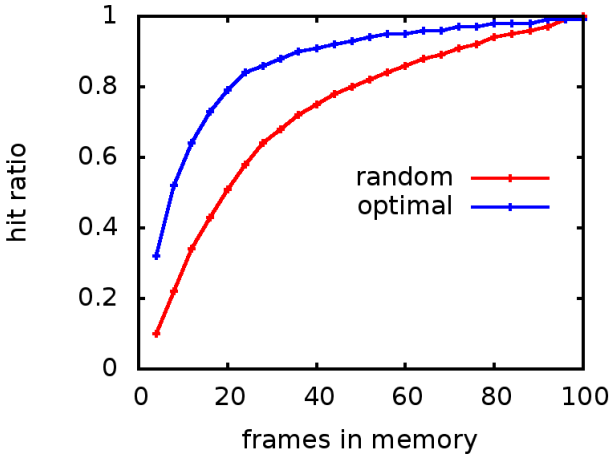

Case closed .... ehhh?

Optimal replacement policy

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Important to know the best possible solution (even if it's not obtainable).

Optimal replacement policy

Important to know the best possible solution (even if it's not obtainable).

We might not have access to the future - but the past might give us a good approximation.

Least Recently Used (LRU)

- A page that has not been referenced for long is not likely to be referenced in the near future.

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Least Recently Used (LRU)

access	hit/miss	evict	queue
0			

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Least Recently Used (LRU)

access	hit/miss	evict	queue
0	miss	-	0

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Least Recently Used (LRU)

access	hit/miss	evict	queue
0	miss	-	0
1			

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Least Recently Used (LRU)

access	hit/miss	evict	queue
0	miss	-	0
1	miss	-	0,1

- A page that has not been referenced for long is not likely to be referenced in the near future.
- page references: 0,1,2,3,0,2,3,1,2,0,3,0

Least Recently Used (LRU)

access	hit/miss	evict	queue
0	miss	-	0
1	miss	-	0,1
2			

- A page that has not been referenced for long is not likely to be referenced in the near future.
- page references: 0,1,2,3,0,2,3,1,2,0,3,0

Least Recently Used (LRU)

access	hit/miss	evict	queue
0	miss	-	0
1	miss	-	0,1
2	miss	-	0,1,2

- A page that has not been referenced for long is not likely to be referenced in the near future.
- page references: 0,1,2,3,0,2,3,1,2,0,3,0

Least Recently Used (LRU)

access	hit/miss	evict	queue
0	miss	-	0
1	miss	-	0,1
2	miss	-	0,1,2
3			

- A page that has not been referenced for long is not likely to be referenced in the near future.
- page references: 0,1,2,3,0,2,3,1,2,0,3,0

Least Recently Used (LRU)

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- page references: 0,1,2,3,0,2,3,1,2,0,3,0

access	hit/miss	evict	queue
0	miss	-	0
1	miss	-	0,1
2	miss	-	0,1,2
3	miss	0	1,2,3

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- page references: 0,1,2,3,0,2,3,1,2,0,3,0

access	hit/miss	evict	queue
0	miss	-	0
1	miss	-	0,1
2	miss	-	0,1,2
3	miss	0	1,2,3
0			

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access	hit/miss	evict	queue
0	miss	-	0
1	miss	-	0,1
2	miss	-	0,1,2
3	miss	0	1,2,3
0	miss	1	2,3,0

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- page references: 0,1,2,3,0,2,3,1,2,0,3,0

access	hit/miss	evict	queue
0	miss	-	0
1	miss	-	0,1
2	miss	-	0,1,2
3	miss	0	1,2,3
0	miss	1	2,3,0
2			

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- page references: 0,1,2,3,0,2,3,1,2,0,3,0

access	hit/miss	evict	queue
0	miss	-	0
1	miss	-	0,1
2	miss	-	0,1,2
3	miss	0	1,2,3
0	miss	1	2,3,0
2	hit		3,0,2

Least Recently Used (LRU)

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- page references: 0,1,2,3,0,2,3,1,2,0,3,0

access	hit/miss	evict	queue
0	miss	-	0
1	miss	-	0,1
2	miss	-	0,1,2
3	miss	0	1,2,3
0	miss	1	2,3,0
2	hit		3,0,2
3			

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access	hit/miss	evict	queue
0	miss	-	0
1	miss	-	0,1
2	miss	-	0,1,2
3	miss	0	1,2,3
0	miss	1	2,3,0
2	hit		3,0,2
3	hit		0,2,3

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0	miss	-	0
1	miss	-	0,1
2	miss	-	0,1,2
3	miss	0	1,2,3
0	miss	1	2,3,0
2	hit		3,0,2
3	hit		0,2,3
1			

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0	miss	-	0
1	miss	-	0,1
2	miss	-	0,1,2
3	miss	0	1,2,3
0	miss	1	2,3,0
2	hit		3,0,2
3	hit		0,2,3
1	miss	0	2,3,1

Least Recently Used (LRU)

- A page that has not been referenced for long is not likely to be referenced in the near future.
- page references: 0,1,2,3,0,2,3,1,2,0,3,0

access	hit/miss	evict	queue
0	miss	-	0
1	miss	-	0,1
2	miss	-	0,1,2
3	miss	0	1,2,3
0	miss	1	2,3,0
2	hit		3,0,2
3	hit		0,2,3
1	miss	0	2,3,1
2			

Least Recently Used (LRU)

- A page that has not been referenced for long is not likely to be referenced in the near future.
- page references: 0,1,2,3,0,2,3,1,2,0,3,0

access	hit/miss	evict	queue
0	miss	-	0
1	miss	-	0,1
2	miss	-	0,1,2
3	miss	0	1,2,3
0	miss	1	2,3,0
2	hit		3,0,2
3	hit		0,2,3
1	miss	0	2,3,1
2	hit		3,1,2

Least Recently Used (LRU)

- A page that has not been referenced for long is not likely to be referenced in the near future.
- page references: 0,1,2,3,0,2,3,1,2,0,3,0

access	hit/miss	evict	queue
0	miss	-	0
1	miss	-	0,1
2	miss	-	0,1,2
3	miss	0	1,2,3
0	miss	1	2,3,0
2	hit		3,0,2
3	hit		0,2,3
1	miss	0	2,3,1
2	hit		3,1,2
0			

Least Recently Used (LRU)

- A page that has not been referenced for long is not likely to be referenced in the near future.
- page references: 0,1,2,3,0,2,3,1,2,0,3,0

access	hit/miss	evict	queue
0	miss	-	0
1	miss	-	0,1
2	miss	-	0,1,2
3	miss	0	1,2,3
0	miss	1	2,3,0
2	hit		3,0,2
3	hit		0,2,3
1	miss	0	2,3,1
2	hit		3,1,2
0	miss	3	1,2,0

Least Recently Used (LRU)

- A page that has not been referenced for long is not likely to be referenced in the near future.
- page references: 0,1,2,3,0,2,3,1,2,0,3,0

access	hit/miss	evict	queue
0	miss	-	0
1	miss	-	0,1
2	miss	-	0,1,2
3	miss	0	1,2,3
0	miss	1	2,3,0
2	hit		3,0,2
3	hit		0,2,3
1	miss	0	2,3,1
2	hit		3,1,2
0	miss	3	1,2,0
3			

Least Recently Used (LRU)

- A page that has not been referenced for long is not likely to be referenced in the near future.
- page references: 0,1,2,3,0,2,3,1,2,0,3,0

access	hit/miss	evict	queue
0	miss	-	0
1	miss	-	0,1
2	miss	-	0,1,2
3	miss	0	1,2,3
0	miss	1	2,3,0
2	hit		3,0,2
3	hit		0,2,3
1	miss	0	2,3,1
2	hit		3,1,2
0	miss	3	1,2,0
3	miss	1	2,0,3

Least Recently Used (LRU)

- A page that has not been referenced for long is not likely to be referenced in the near future.
- page references: 0,1,2,3,0,2,3,1,2,0,3,0

access	hit/miss	evict	queue
0	miss	-	0
1	miss	-	0,1
2	miss	-	0,1,2
3	miss	0	1,2,3
0	miss	1	2,3,0
2	hit		3,0,2
3	hit		0,2,3
1	miss	0	2,3,1
2	hit		3,1,2
0	miss	3	1,2,0
3	miss	1	2,0,3
0			

Least Recently Used (LRU)

- A page that has not been referenced for long is not likely to be referenced in the near future.
- page references: 0,1,2,3,0,2,3,1,2,0,3,0

access	hit/miss	evict	queue
0	miss	-	0
1	miss	-	0,1
2	miss	-	0,1,2
3	miss	0	1,2,3
0	miss	1	2,3,0
2	hit		3,0,2
3	hit		0,2,3
1	miss	0	2,3,1
2	hit		3,1,2
0	miss	3	1,2,0
3	miss	1	2,0,3
0	hit		2,0,3

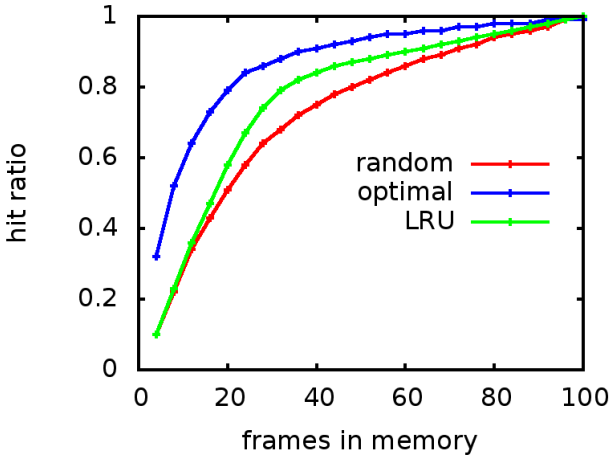
Least Recently Used (LRU)

- A page that has not been referenced for long is not likely to be referenced in the near future.
- page references: 0,1,2,3,0,2,3,1,2,0,3,0

access	hit/miss	evict	queue
0	miss	-	0
1	miss	-	0,1
2	miss	-	0,1,2
3	miss	0	1,2,3
0	miss	1	2,3,0
2	hit		3,0,2
3	hit		0,2,3
1	miss	0	2,3,1
2	hit		3,1,2
0	miss	3	1,2,0
3	miss	1	2,0,3
0	hit		2,0,3

Result: two more misses compared to the optimal.

Least Recently Used



Implement Least Recently Used

Keep track of a queue of pages (as many as we have frames).

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Keep track of a queue of pages (as many as we have frames).

In each page reference, move page to the end of the list.

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When evicting a page, select the first page in the list.

Implement Least Recently Used

Keep track of a queue of pages (as many as we have frames).

In each page reference, move page to the end of the list.

When evicting a page, select the first page in the list.

Is this expensive?

The Atlas Computer / Atlas Supervisor

- Manchester University, 1962
- 48-bit word, 16 K word memory, 96 K word “drum”
- 24-bit address space
- paged virtual memory
- 512 word pages
- approximated Least Recently Used replacement policy

a much cheaper solution - FIFO

The problem with LRU is that we need to update the lists in each page reference.

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The problem with LRU is that we need to update the lists in each page reference.

It is much cheaper if we only update the list when we have a page fault.

Idéa: It's better to keep a page that was recently brought in compared to one that has been around for a while.

FIFO - first-in, first-out

- Keep allocated pages in a queue - add in one end, reclaim in the other.
- page references: 0,1,2,3,0,2,3,1,2,0,3,0

FIFO - first-in, first-out

access	hit/miss	evict	fifo
0			

- Keep allocated pages in a queue - add in one end, reclaim in the other.
- page references: 0,1,2,3,0,2,3,1,2,0,3,0

FIFO - first-in, first-out

access	hit/miss	evict	fifo
0	miss	-	0

- Keep allocated pages in a queue - add in one end, reclaim in the other.
- page references: 0,1,2,3,0,2,3,1,2,0,3,0

FIFO - first-in, first-out

access	hit/miss	evict	fifo
0	miss	-	0
1			

- Keep allocated pages in a queue - add in one end, reclaim in the other.
- page references: 0,1,2,3,0,2,3,1,2,0,3,0

FIFO - first-in, first-out

access	hit/miss	evict	fifo
0	miss	-	0
1	miss	-	0,1

- Keep allocated pages in a queue - add in one end, reclaim in the other.
- page references: 0,1,2,3,0,2,3,1,2,0,3,0

FIFO - first-in, first-out

access	hit/miss	evict	fifo
0	miss	-	0
1	miss	-	0,1
2			

- Keep allocated pages in a queue - add in one end, reclaim in the other.
- page references: 0,1,2,3,0,2,3,1,2,0,3,0

FIFO - first-in, first-out

access	hit/miss	evict	fifo
0	miss	-	0
1	miss	-	0,1
2	miss	-	0,1,2

- Keep allocated pages in a queue - add in one end, reclaim in the other.
- page references: 0,1,2,3,0,2,3,1,2,0,3,0

FIFO - first-in, first-out

access	hit/miss	evict	fifo
0	miss	-	0
1	miss	-	0,1
2	miss	-	0,1,2
3			

- Keep allocated pages in a queue - add in one end, reclaim in the other.
- page references: 0,1,2,3,0,2,3,1,2,0,3,0

FIFO - first-in, first-out

access	hit/miss	evict	fifo
0	miss	-	0
1	miss	-	0,1
2	miss	-	0,1,2
3	miss	0	1,2,3

- Keep allocated pages in a queue - add in one end, reclaim in the other.
- page references: 0,1,2,3,0,2,3,1,2,0,3,0

FIFO - first-in, first-out

- Keep allocated pages in a queue - add in one end, reclaim in the other.
- page references: 0,1,2,3,0,2,3,1,2,0,3,0

access	hit/miss	evict	fifo
0	miss	-	0
1	miss	-	0,1
2	miss	-	0,1,2
3	miss	0	1,2,3
0			

FIFO - first-in, first-out

- Keep allocated pages in a queue - add in one end, reclaim in the other.
- page references: 0,1,2,3,0,2,3,1,2,0,3,0

access	hit/miss	evict	fifo
0	miss	-	0
1	miss	-	0,1
2	miss	-	0,1,2
3	miss	0	1,2,3
0	miss	1	2,3,0

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- page references: 0,1,2,3,0,2,3,1,2,0,3,0

access	hit/miss	evict	fifo
0	miss	-	0
1	miss	-	0,1
2	miss	-	0,1,2
3	miss	0	1,2,3
0	miss	1	2,3,0
2			

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- Keep allocated pages in a queue - add in one end, reclaim in the other.
- page references: 0,1,2,3,0,2,3,1,2,0,3,0

access	hit/miss	evict	fifo
0	miss	-	0
1	miss	-	0,1
2	miss	-	0,1,2
3	miss	0	1,2,3
0	miss	1	2,3,0
2	hit		2,3,0

FIFO - first-in, first-out

- Keep allocated pages in a queue - add in one end, reclaim in the other.
- page references: 0,1,2,3,0,2,3,1,2,0,3,0

access	hit/miss	evict	fifo
0	miss	-	0
1	miss	-	0,1
2	miss	-	0,1,2
3	miss	0	1,2,3
0	miss	1	2,3,0
2	hit		2,3,0
3			

FIFO - first-in, first-out

- Keep allocated pages in a queue - add in one end, reclaim in the other.
- page references: 0,1,2,3,0,2,3,1,2,0,3,0

access	hit/miss	evict	fifo
0	miss	-	0
1	miss	-	0,1
2	miss	-	0,1,2
3	miss	0	1,2,3
0	miss	1	2,3,0
2	hit		2,3,0
3	hit		2,3,0

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- Keep allocated pages in a queue - add in one end, reclaim in the other.
- page references: 0,1,2,3,0,2,3,1,2,0,3,0

access	hit/miss	evict	fifo
0	miss	-	0
1	miss	-	0,1
2	miss	-	0,1,2
3	miss	0	1,2,3
0	miss	1	2,3,0
2	hit		2,3,0
3	hit		2,3,0
1			

FIFO - first-in, first-out

- Keep allocated pages in a queue - add in one end, reclaim in the other.
- page references: 0,1,2,3,0,2,3,1,2,0,3,0

access	hit/miss	evict	fifo
0	miss	-	0
1	miss	-	0,1
2	miss	-	0,1,2
3	miss	0	1,2,3
0	miss	1	2,3,0
2	hit		2,3,0
3	hit		2,3,0
1	miss	2	3,0,1

FIFO - first-in, first-out

- Keep allocated pages in a queue - add in one end, reclaim in the other.
- page references: 0,1,2,3,0,2,3,1,2,0,3,0

access	hit/miss	evict	fifo
0	miss	-	0
1	miss	-	0,1
2	miss	-	0,1,2
3	miss	0	1,2,3
0	miss	1	2,3,0
2	hit		2,3,0
3	hit		2,3,0
1	miss	2	3,0,1
2			

FIFO - first-in, first-out

- Keep allocated pages in a queue - add in one end, reclaim in the other.
- page references: 0,1,2,3,0,2,3,1,2,0,3,0

access	hit/miss	evict	fifo
0	miss	-	0
1	miss	-	0,1
2	miss	-	0,1,2
3	miss	0	1,2,3
0	miss	1	2,3,0
2	hit		2,3,0
3	hit		2,3,0
1	miss	2	3,0,1
2	miss	3	0,1,2

FIFO - first-in, first-out

- Keep allocated pages in a queue - add in one end, reclaim in the other.
- page references: 0,1,2,3,0,2,3,1,2,0,3,0

access	hit/miss	evict	fifo
0	miss	-	0
1	miss	-	0,1
2	miss	-	0,1,2
3	miss	0	1,2,3
0	miss	1	2,3,0
2	hit		2,3,0
3	hit		2,3,0
1	miss	2	3,0,1
2	miss	3	0,1,2
0			

FIFO - first-in, first-out

- Keep allocated pages in a queue - add in one end, reclaim in the other.
- page references: 0,1,2,3,0,2,3,1,2,0,3,0

access	hit/miss	evict	fifo
0	miss	-	0
1	miss	-	0,1
2	miss	-	0,1,2
3	miss	0	1,2,3
0	miss	1	2,3,0
2	hit		2,3,0
3	hit		2,3,0
1	miss	2	3,0,1
2	miss	3	0,1,2
0	hit		0,1,2

FIFO - first-in, first-out

- Keep allocated pages in a queue - add in one end, reclaim in the other.
- page references: 0,1,2,3,0,2,3,1,2,0,3,0

access	hit/miss	evict	fifo
0	miss	-	0
1	miss	-	0,1
2	miss	-	0,1,2
3	miss	0	1,2,3
0	miss	1	2,3,0
2	hit		2,3,0
3	hit		2,3,0
1	miss	2	3,0,1
2	miss	3	0,1,2
0	hit		0,1,2
3			

FIFO - first-in, first-out

- Keep allocated pages in a queue - add in one end, reclaim in the other.
- page references: 0,1,2,3,0,2,3,1,2,0,3,0

access	hit/miss	evict	fifo
0	miss	-	0
1	miss	-	0,1
2	miss	-	0,1,2
3	miss	0	1,2,3
0	miss	1	2,3,0
2	hit		2,3,0
3	hit		2,3,0
1	miss	2	3,0,1
2	miss	3	0,1,2
0	hit		0,1,2
3	miss	0	1,2,3

FIFO - first-in, first-out

- Keep allocated pages in a queue - add in one end, reclaim in the other.
- page references: 0,1,2,3,0,2,3,1,2,0,3,0

access	hit/miss	evict	fifo
0	miss	-	0
1	miss	-	0,1
2	miss	-	0,1,2
3	miss	0	1,2,3
0	miss	1	2,3,0
2	hit		2,3,0
3	hit		2,3,0
1	miss	2	3,0,1
2	miss	3	0,1,2
0	hit		0,1,2
3	miss	0	1,2,3
0			

FIFO - first-in, first-out

- Keep allocated pages in a queue - add in one end, reclaim in the other.
- page references: 0,1,2,3,0,2,3,1,2,0,3,0

access	hit/miss	evict	fifo
0	miss	-	0
1	miss	-	0,1
2	miss	-	0,1,2
3	miss	0	1,2,3
0	miss	1	2,3,0
2	hit		2,3,0
3	hit		2,3,0
1	miss	2	3,0,1
2	miss	3	0,1,2
0	hit		0,1,2
3	miss	0	1,2,3
0	miss	1	2,3,0

FIFO - first-in, first-out

- Keep allocated pages in a queue - add in one end, reclaim in the other.
- page references: 0,1,2,3,0,2,3,1,2,0,3,0

access	hit/miss	evict	fifo
0	miss	-	0
1	miss	-	0,1
2	miss	-	0,1,2
3	miss	0	1,2,3
0	miss	1	2,3,0
2	hit		2,3,0
3	hit		2,3,0
1	miss	2	3,0,1
2	miss	3	0,1,2
0	hit		0,1,2
3	miss	0	1,2,3
0	miss	1	2,3,0

Result: only 3 hits :-(

Let's try again

- Let's try with more pages 0-4

Let's try again

- Let's try with more pages 0-4
- page references: 0,1,2,3,0,1,4,0,1,2,3,4

Let's try again

access	hit/miss	evict	fifo
0			

- Let's try with more pages 0-4
- page references: 0,1,2,3,0,1,4,0,1,2,3,4

Let's try again

access	hit/miss	evict	fifo
0	miss		0

- Let's try with more pages 0-4
- page references: 0,1,2,3,0,1,4,0,1,2,3,4

Let's try again

access	hit/miss	evict	fifo
0	miss		0
1			

- Let's try with more pages 0-4
- page references: 0,1,2,3,0,1,4,0,1,2,3,4

Let's try again

access	hit/miss	evict	fifo
0	miss		0
1	miss		0,1

- Let's try with more pages 0-4
- page references: 0,1,2,3,0,1,4,0,1,2,3,4

Let's try again

access	hit/miss	evict	fifo
0	miss		0
1	miss		0,1
2			

- Let's try with more pages 0-4
- page references: 0,1,2,3,0,1,4,0,1,2,3,4

Let's try again

access	hit/miss	evict	fifo
0	miss		0
1	miss		0,1
2	miss		0,1,2

- Let's try with more pages 0-4
- page references: 0,1,2,3,0,1,4,0,1,2,3,4

Let's try again

access	hit/miss	evict	fifo
0	miss		0
1	miss		0,1
2	miss		0,1,2
3			

- Let's try with more pages 0-4
- page references: 0,1,2,3,0,1,4,0,1,2,3,4

Let's try again

access	hit/miss	evict	fifo
0	miss		0
1	miss		0,1
2	miss		0,1,2
3	miss	0	1,2,3

- Let's try with more pages 0-4
- page references: 0,1,2,3,0,1,4,0,1,2,3,4

Let's try again

access	hit/miss	evict	fifo
0	miss		0
1	miss		0,1
2	miss		0,1,2
3	miss	0	1,2,3
0			

- Let's try with more pages 0-4
- page references: 0,1,2,3,0,1,4,0,1,2,3,4

Let's try again

access	hit/miss	evict	fifo
0	miss		0
1	miss		0,1
2	miss		0,1,2
3	miss	0	1,2,3
0	miss	1	2,3,0

- Let's try with more pages 0-4
- page references: 0,1,2,3,0,1,4,0,1,2,3,4

Let's try again

- Let's try with more pages 0-4
- page references: 0,1,2,3,0,1,4,0,1,2,3,4

access	hit/miss	evict	fifo
0	miss		0
1	miss		0,1
2	miss		0,1,2
3	miss	0	1,2,3
0	miss	1	2,3,0
1			

Let's try again

- Let's try with more pages 0-4
- page references: 0,1,2,3,0,1,4,0,1,2,3,4

access	hit/miss	evict	fifo
0	miss		0
1	miss		0,1
2	miss		0,1,2
3	miss	0	1,2,3
0	miss	1	2,3,0
1	miss	2	3,0,1

Let's try again

- Let's try with more pages 0-4
- page references: 0,1,2,3,0,1,4,0,1,2,3,4

access	hit/miss	evict	fifo
0	miss		0
1	miss		0,1
2	miss		0,1,2
3	miss	0	1,2,3
0	miss	1	2,3,0
1	miss	2	3,0,1
4			

Let's try again

- Let's try with more pages 0-4
- page references: 0,1,2,3,0,1,4,0,1,2,3,4

access	hit/miss	evict	fifo
0	miss		0
1	miss		0,1
2	miss		0,1,2
3	miss	0	1,2,3
0	miss	1	2,3,0
1	miss	2	3,0,1
4	miss	3	0,1,4

Let's try again

- Let's try with more pages 0-4
- page references: 0,1,2,3,0,1,4,0,1,2,3,4

access	hit/miss	evict	fifo
0	miss		0
1	miss		0,1
2	miss		0,1,2
3	miss	0	1,2,3
0	miss	1	2,3,0
1	miss	2	3,0,1
4	miss	3	0,1,4
0			

Let's try again

- Let's try with more pages 0-4
- page references: 0,1,2,3,0,1,4,0,1,2,3,4

access	hit/miss	evict	fifo
0	miss		0
1	miss		0,1
2	miss		0,1,2
3	miss	0	1,2,3
0	miss	1	2,3,0
1	miss	2	3,0,1
4	miss	3	0,1,4
0	hit		0,1,4

Let's try again

- Let's try with more pages 0-4
- page references: 0,1,2,3,0,1,4,0,1,2,3,4

access	hit/miss	evict	fifo
0	miss		0
1	miss		0,1
2	miss		0,1,2
3	miss	0	1,2,3
0	miss	1	2,3,0
1	miss	2	3,0,1
4	miss	3	0,1,4
0	hit		0,1,4
1			

Let's try again

- Let's try with more pages 0-4
- page references: 0,1,2,3,0,1,4,0,1,2,3,4

access	hit/miss	evict	fifo
0	miss		0
1	miss		0,1
2	miss		0,1,2
3	miss	0	1,2,3
0	miss	1	2,3,0
1	miss	2	3,0,1
4	miss	3	0,1,4
0	hit		0,1,4
1	hit		0,1,4

Let's try again

- Let's try with more pages 0-4
- page references: 0,1,2,3,0,1,4,0,1,2,3,4

access	hit/miss	evict	fifo
0	miss		0
1	miss		0,1
2	miss		0,1,2
3	miss	0	1,2,3
0	miss	1	2,3,0
1	miss	2	3,0,1
4	miss	3	0,1,4
0	hit		0,1,4
1	hit		0,1,4
2			

Let's try again

- Let's try with more pages 0-4
- page references: 0,1,2,3,0,1,4,0,1,2,3,4

access	hit/miss	evict	fifo
0	miss		0
1	miss		0,1
2	miss		0,1,2
3	miss	0	1,2,3
0	miss	1	2,3,0
1	miss	2	3,0,1
4	miss	3	0,1,4
0	hit		0,1,4
1	hit		0,1,4
2	miss	0	1,4,2

Let's try again

- Let's try with more pages 0-4
- page references: 0,1,2,3,0,1,4,0,1,2,3,4

access	hit/miss	evict	fifo
0	miss		0
1	miss		0,1
2	miss		0,1,2
3	miss	0	1,2,3
0	miss	1	2,3,0
1	miss	2	3,0,1
4	miss	3	0,1,4
0	hit		0,1,4
1	hit		0,1,4
2	miss	0	1,4,2
3			

Let's try again

- Let's try with more pages 0-4
- page references: 0,1,2,3,0,1,4,0,1,2,3,4

access	hit/miss	evict	fifo
0	miss		0
1	miss		0,1
2	miss		0,1,2
3	miss	0	1,2,3
0	miss	1	2,3,0
1	miss	2	3,0,1
4	miss	3	0,1,4
0	hit		0,1,4
1	hit		0,1,4
2	miss	0	1,4,2
3	miss	1	4,2,3

Let's try again

- Let's try with more pages 0-4
- page references: 0,1,2,3,0,1,4,0,1,2,3,4

access	hit/miss	evict	fifo
0	miss		0
1	miss		0,1
2	miss		0,1,2
3	miss	0	1,2,3
0	miss	1	2,3,0
1	miss	2	3,0,1
4	miss	3	0,1,4
0	hit		0,1,4
1	hit		0,1,4
2	miss	0	1,4,2
3	miss	1	4,2,3
4			

Let's try again

- Let's try with more pages 0-4
- page references: 0,1,2,3,0,1,4,0,1,2,3,4

access	hit/miss	evict	fifo
0	miss		0
1	miss		0,1
2	miss		0,1,2
3	miss	0	1,2,3
0	miss	1	2,3,0
1	miss	2	3,0,1
4	miss	3	0,1,4
0	hit		0,1,4
1	hit		0,1,4
2	miss	0	1,4,2
3	miss	1	4,2,3
4	hit		4,2,3

Let's try again

- Let's try with more pages 0-4
- page references: 0,1,2,3,0,1,4,0,1,2,3,4

access	hit/miss	evict	fifo
0	miss		0
1	miss		0,1
2	miss		0,1,2
3	miss	0	1,2,3
0	miss	1	2,3,0
1	miss	2	3,0,1
4	miss	3	0,1,4
0	hit		0,1,4
1	hit		0,1,4
2	miss	0	1,4,2
3	miss	1	4,2,3
4	hit		4,2,3

3 hits out of 12 page references - hmmm

Belady's anomaly

- Let's try with more frames, four instead of three!

Belady's anomaly

- Let's try with more frames, four instead of three!
- page references: 0,1,2,3,0,1,4,0,1,2,3,4

Belady's anomaly

access	hit/miss	evict	fifo
0			

- Let's try with more frames, four instead of three!
- page references: 0,1,2,3,0,1,4,0,1,2,3,4

Belady's anomaly

access	hit/miss	evict	fifo
0	miss		0

- Let's try with more frames, four instead of three!
- page references: 0,1,2,3,0,1,4,0,1,2,3,4

Belady's anomaly

access	hit/miss	evict	fifo
0	miss		0
1			

- Let's try with more frames, four instead of three!
- page references: 0,1,2,3,0,1,4,0,1,2,3,4

Belady's anomaly

access	hit/miss	evict	fifo
0	miss		0
1	miss		0,1

- Let's try with more frames, four instead of three!
- page references: 0,1,2,3,0,1,4,0,1,2,3,4

Belady's anomaly

access	hit/miss	evict	fifo
0	miss		0
1	miss		0,1
2			

- Let's try with more frames, four instead of three!
- page references: 0,1,2,3,0,1,4,0,1,2,3,4

Belady's anomaly

access	hit/miss	evict	fifo
0	miss		0
1	miss		0,1
2	miss		0,1,2

- Let's try with more frames, four instead of three!
- page references: 0,1,2,3,0,1,4,0,1,2,3,4

Belady's anomaly

access	hit/miss	evict	fifo
0	miss		0
1	miss		0,1
2	miss		0,1,2
3			

- Let's try with more frames, four instead of three!
- page references: 0,1,2,3,0,1,4,0,1,2,3,4

Belady's anomaly

access	hit/miss	evict	fifo
0	miss		0
1	miss		0,1
2	miss		0,1,2
3	miss		0,1,2,3

- Let's try with more frames, four instead of three!
- page references: 0,1,2,3,0,1,4,0,1,2,3,4

Belady's anomaly

- Let's try with more frames, four instead of three!
- page references: 0,1,2,3,0,1,4,0,1,2,3,4

access	hit/miss	evict	fifo
0	miss		0
1	miss		0,1
2	miss		0,1,2
3	miss		0,1,2,3
0			

Belady's anomaly

- Let's try with more frames, four instead of three!
- page references: 0,1,2,3,0,1,4,0,1,2,3,4

access	hit/miss	evict	fifo
0	miss		0
1	miss		0,1
2	miss		0,1,2
3	miss		0,1,2,3
0	hit		0,1,2,3

Belady's anomaly

- Let's try with more frames, four instead of three!
- page references: 0,1,2,3,0,1,4,0,1,2,3,4

access	hit/miss	evict	fifo
0	miss		0
1	miss		0,1
2	miss		0,1,2
3	miss		0,1,2,3
0	hit		0,1,2,3
1			

Belady's anomaly

- Let's try with more frames, four instead of three!
- page references: 0,1,2,3,0,1,4,0,1,2,3,4

access	hit/miss	evict	fifo
0	miss		0
1	miss		0,1
2	miss		0,1,2
3	miss		0,1,2,3
0	hit		0,1,2,3
1	hit		0,1,2,3

Belady's anomaly

- Let's try with more frames, four instead of three!
- page references: 0,1,2,3,0,1,4,0,1,2,3,4

access	hit/miss	evict	fifo
0	miss		0
1	miss		0,1
2	miss		0,1,2
3	miss		0,1,2,3
0	hit		0,1,2,3
1	hit		0,1,2,3
4			

Belady's anomaly

- Let's try with more frames, four instead of three!
- page references: 0,1,2,3,0,1,4,0,1,2,3,4

access	hit/miss	evict	fifo
0	miss		0
1	miss		0,1
2	miss		0,1,2
3	miss		0,1,2,3
0	hit		0,1,2,3
1	hit		0,1,2,3
4	miss	0	1,2,3,4

Belady's anomaly

- Let's try with more frames, four instead of three!
- page references: 0,1,2,3,0,1,4,0,1,2,3,4

access	hit/miss	evict	fifo
0	miss		0
1	miss		0,1
2	miss		0,1,2
3	miss		0,1,2,3
0	hit		0,1,2,3
1	hit		0,1,2,3
4	miss	0	1,2,3,4
0			

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- page references: 0,1,2,3,0,1,4,0,1,2,3,4

access	hit/miss	evict	fifo
0	miss		0
1	miss		0,1
2	miss		0,1,2
3	miss		0,1,2,3
0	hit		0,1,2,3
1	hit		0,1,2,3
4	miss	0	1,2,3,4
0	miss	1	2,3,4,0

Belady's anomaly

- Let's try with more frames, four instead of three!
- page references: 0,1,2,3,0,1,4,0,1,2,3,4

access	hit/miss	evict	fifo
0	miss		0
1	miss		0,1
2	miss		0,1,2
3	miss		0,1,2,3
0	hit		0,1,2,3
1	hit		0,1,2,3
4	miss	0	1,2,3,4
0	miss	1	2,3,4,0
1			

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- page references: 0,1,2,3,0,1,4,0,1,2,3,4

access	hit/miss	evict	fifo
0	miss		0
1	miss		0,1
2	miss		0,1,2
3	miss		0,1,2,3
0	hit		0,1,2,3
1	hit		0,1,2,3
4	miss	0	1,2,3,4
0	miss	1	2,3,4,0
1	miss	2	3,4,0,1

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- page references: 0,1,2,3,0,1,4,0,1,2,3,4

access	hit/miss	evict	fifo
0	miss		0
1	miss		0,1
2	miss		0,1,2
3	miss		0,1,2,3
0	hit		0,1,2,3
1	hit		0,1,2,3
4	miss	0	1,2,3,4
0	miss	1	2,3,4,0
1	miss	2	3,4,0,1
2			

Belady's anomaly

- Let's try with more frames, four instead of three!
- page references: 0,1,2,3,0,1,4,0,1,2,3,4

access	hit/miss	evict	fifo
0	miss		0
1	miss		0,1
2	miss		0,1,2
3	miss		0,1,2,3
0	hit		0,1,2,3
1	hit		0,1,2,3
4	miss	0	1,2,3,4
0	miss	1	2,3,4,0
1	miss	2	3,4,0,1
2	miss	3	4,0,1,2

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- Let's try with more frames, four instead of three!
- page references: 0,1,2,3,0,1,4,0,1,2,3,4

access	hit/miss	evict	fifo
0	miss		0
1	miss		0,1
2	miss		0,1,2
3	miss		0,1,2,3
0	hit		0,1,2,3
1	hit		0,1,2,3
4	miss	0	1,2,3,4
0	miss	1	2,3,4,0
1	miss	2	3,4,0,1
2	miss	3	4,0,1,2
3			

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- Let's try with more frames, four instead of three!
- page references: 0,1,2,3,0,1,4,0,1,2,3,4

access	hit/miss	evict	fifo
0	miss		0
1	miss		0,1
2	miss		0,1,2
3	miss		0,1,2,3
0	hit		0,1,2,3
1	hit		0,1,2,3
4	miss	0	1,2,3,4
0	miss	1	2,3,4,0
1	miss	2	3,4,0,1
2	miss	3	4,0,1,2
3	miss	4	0,1,2,3

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- Let's try with more frames, four instead of three!
- page references: 0,1,2,3,0,1,4,0,1,2,3,4

access	hit/miss	evict	fifo
0	miss		0
1	miss		0,1
2	miss		0,1,2
3	miss		0,1,2,3
0	hit		0,1,2,3
1	hit		0,1,2,3
4	miss	0	1,2,3,4
0	miss	1	2,3,4,0
1	miss	2	3,4,0,1
2	miss	3	4,0,1,2
3	miss	4	0,1,2,3
4			

Belady's anomaly

- Let's try with more frames, four instead of three!
- page references: 0,1,2,3,0,1,4,0,1,2,3,4

access	hit/miss	evict	fifo
0	miss		0
1	miss		0,1
2	miss		0,1,2
3	miss		0,1,2,3
0	hit		0,1,2,3
1	hit		0,1,2,3
4	miss	0	1,2,3,4
0	miss	1	2,3,4,0
1	miss	2	3,4,0,1
2	miss	3	4,0,1,2
3	miss	4	0,1,2,3
4	miss	0	1,2,3,4

Belady's anomaly

- Let's try with more frames, four instead of three!
- page references: 0,1,2,3,0,1,4,0,1,2,3,4

access	hit/miss	evict	fifo
0	miss		0
1	miss		0,1
2	miss		0,1,2
3	miss		0,1,2,3
0	hit		0,1,2,3
1	hit		0,1,2,3
4	miss	0	1,2,3,4
0	miss	1	2,3,4,0
1	miss	2	3,4,0,1
2	miss	3	4,0,1,2
3	miss	4	0,1,2,3
4	miss	0	1,2,3,4

WTF!

approximating LRU

approximating LRU

Assume a *reference bit* in the page table entry, initially set to zero.

approximating LRU

Assume a *reference bit* in the page table entry, initially set to zero.

When the page is referenced, the bit is set to one - by the hardware.

approximating LRU

Assume a *reference bit* in the page table entry, initially set to zero.

When the page is referenced, the bit is set to one - by the hardware.

When selecting a page for eviction - select a page with the reference bit set to zero.

approximating LRU

Assume a *reference bit* in the page table entry, initially set to zero.

When the page is referenced, the bit is set to one - by the hardware.

When selecting a page for eviction - select a page with the reference bit set to zero.

A page with a reference bit set to one - **is given a second chance.**

approximating LRU

Assume a *reference bit* in the page table entry, initially set to zero.

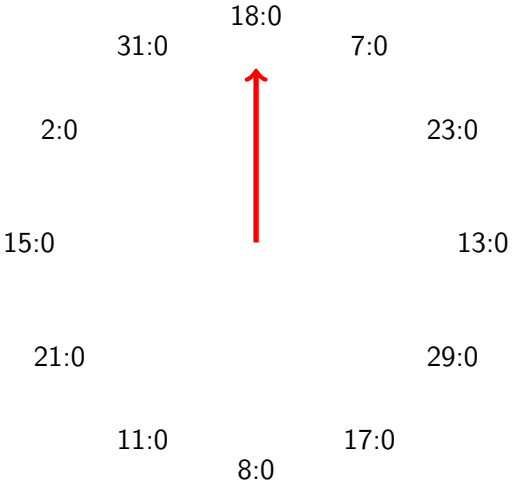
When the page is referenced, the bit is set to one - by the hardware.

When selecting a page for eviction - select a page with the reference bit set to zero.

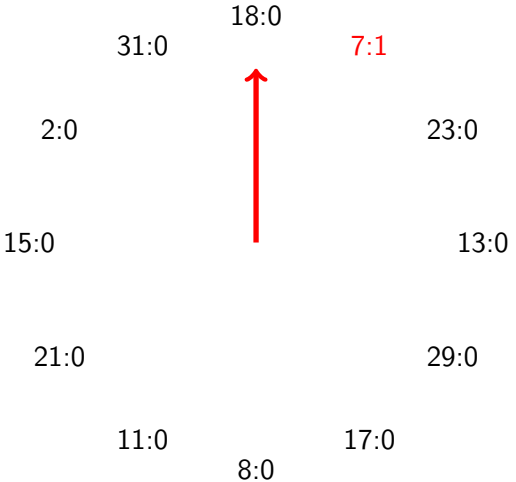
A page with a reference bit set to one - **is given a second chance.**

When should a reference bit be cleared?

the clock algorithm

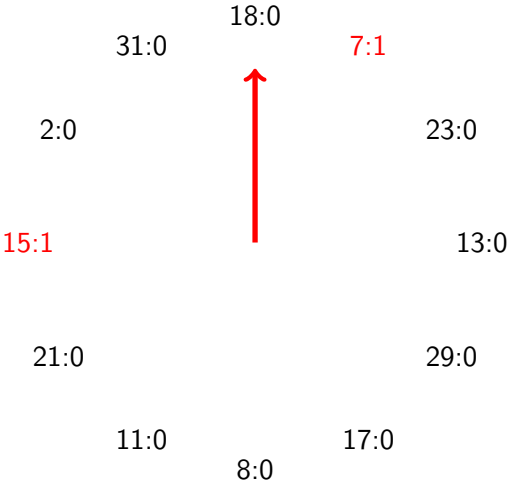


the clock algorithm



access page 7

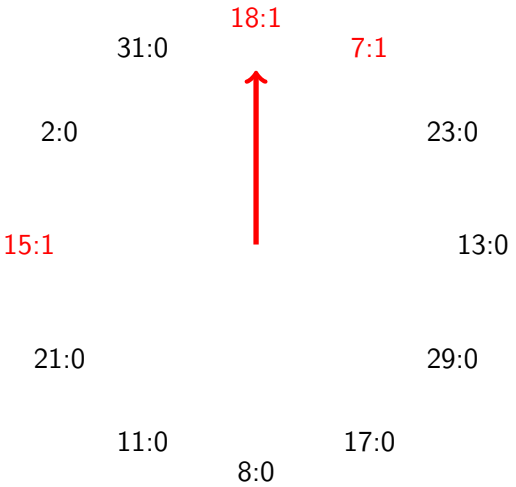
the clock algorithm



access page 7

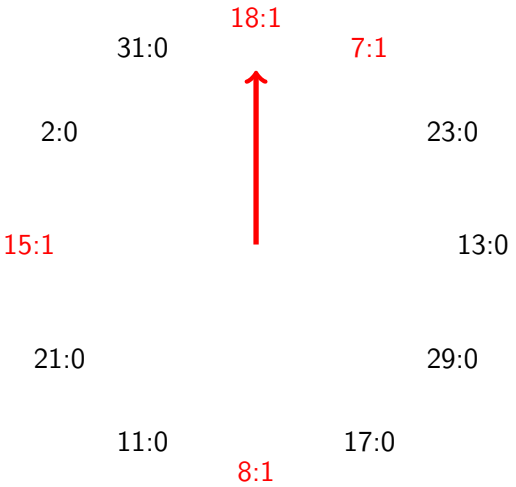
access page 15

the clock algorithm



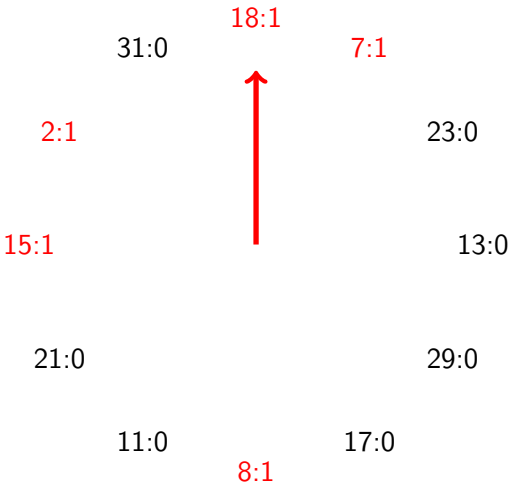
access page 7
access page 15
access page 18

the clock algorithm



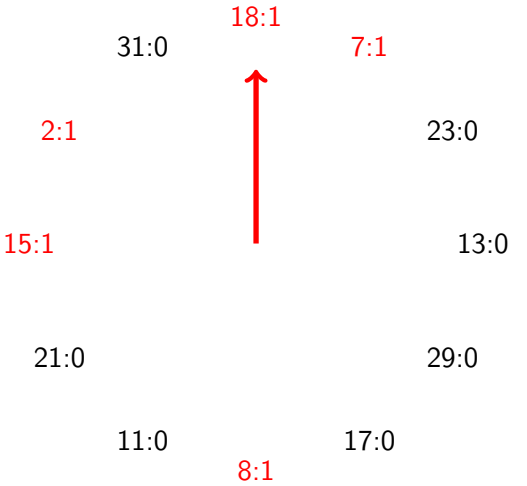
access page 7
access page 15
access page 18
access page 8

the clock algorithm



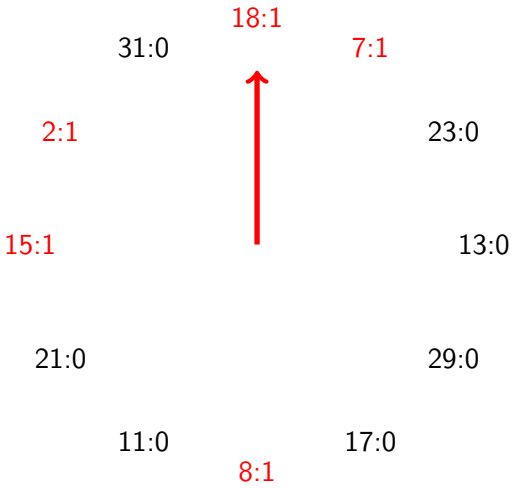
access page 7
access page 15
access page 18
access page 8
access page 2

the clock algorithm



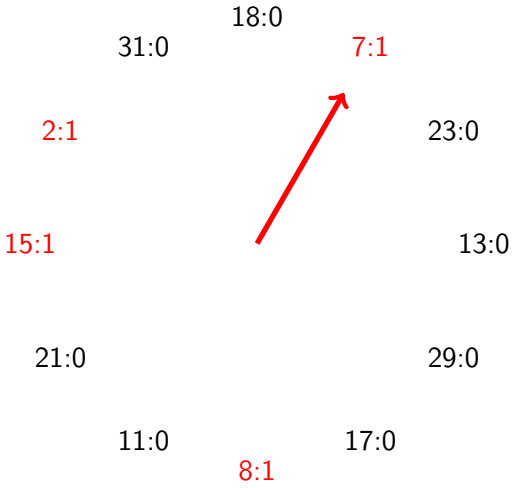
access page 7
access page 15
access page 18
access page 8
access page 2
access page 45

the clock algorithm



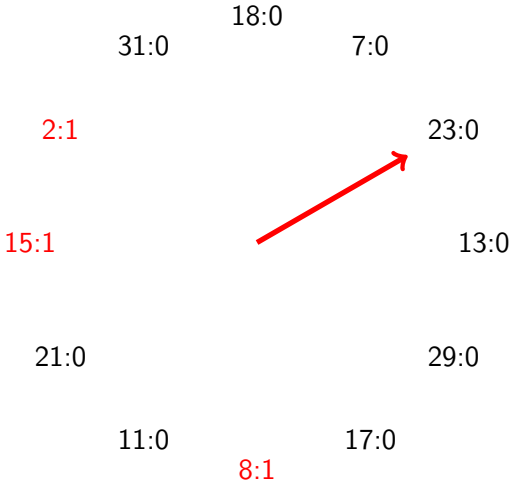
access page 7
access page 15
access page 18
access page 8
access page 2
access page 45
move forward, reset reference bit

the clock algorithm



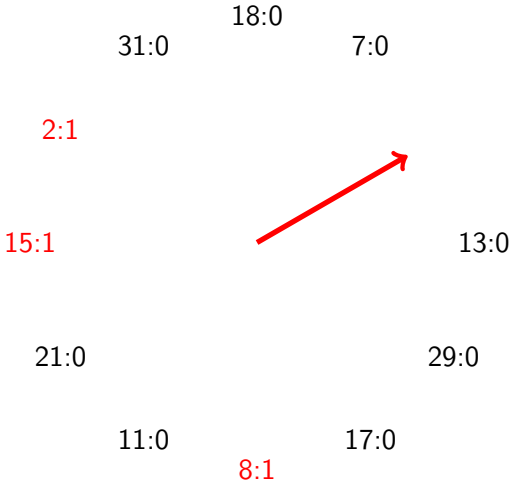
access page 7
access page 15
access page 18
access page 8
access page 2
access page 45
move forward, reset reference bit

the clock algorithm



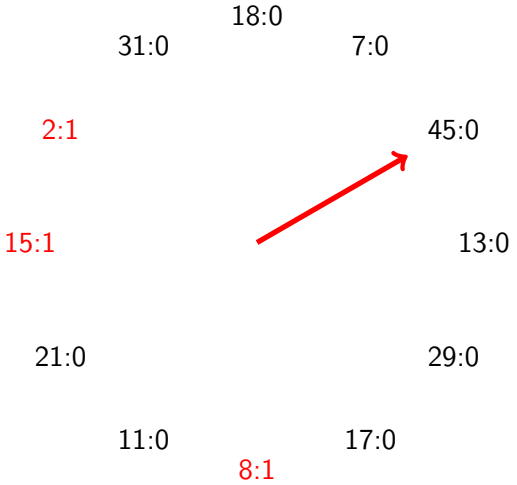
access page 7
access page 15
access page 18
access page 8
access page 2
access page 45
move forward, reset reference bit

the clock algorithm



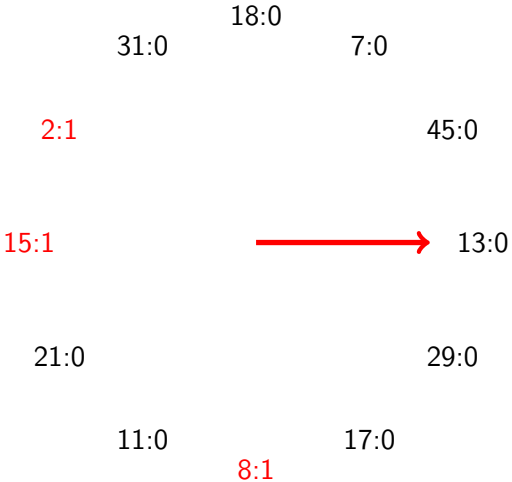
access page 7
access page 15
access page 18
access page 8
access page 2
access page 45
move forward, reset reference bit
remove page

the clock algorithm



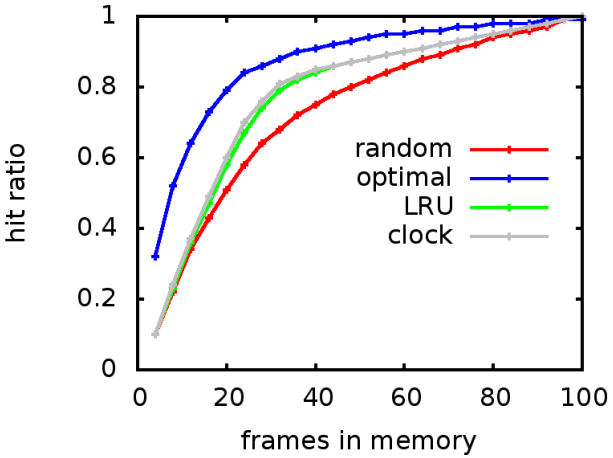
access page 7
access page 15
access page 18
access page 8
access page 2
access page 45
move forward, reset reference bit
remove page
allocate new page

the clock algorithm



access page 7
access page 15
access page 18
access page 8
access page 2
access page 45
move forward, reset reference bit
remove page
allocate new page
move forward

the clock algorithm



dirty pages

dirty pages

You have two frames to choose from, holding:

dirty pages

You have two frames to choose from, holding:

- a page that has been recently used but not modified and,

dirty pages

You have two frames to choose from, holding:

- a page that has been recently used but not modified and,
- a page that has not been used for a long time but has been modified.

dirty pages

You have two frames to choose from, holding:

- a page that has been recently used but not modified and,
- a page that has not been used for a long time but has been modified.

Which one should we reclaim of we need a free frame?

The page table entry (PTE)

The page table entry (PTE)

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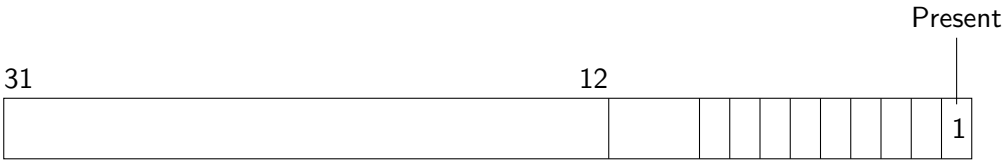

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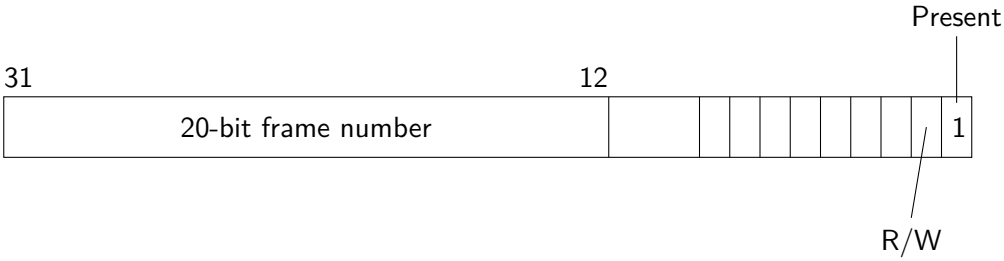

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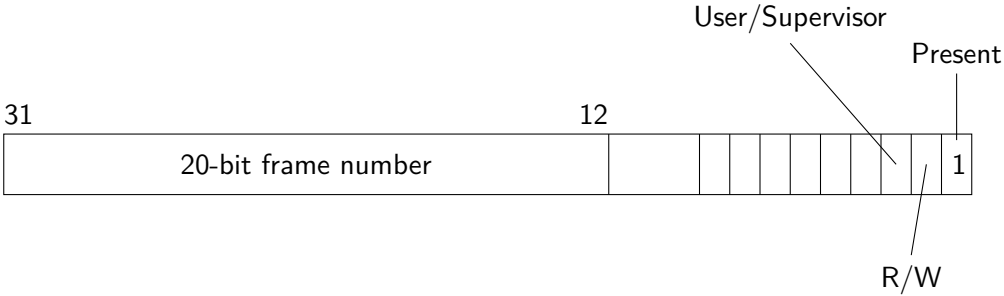

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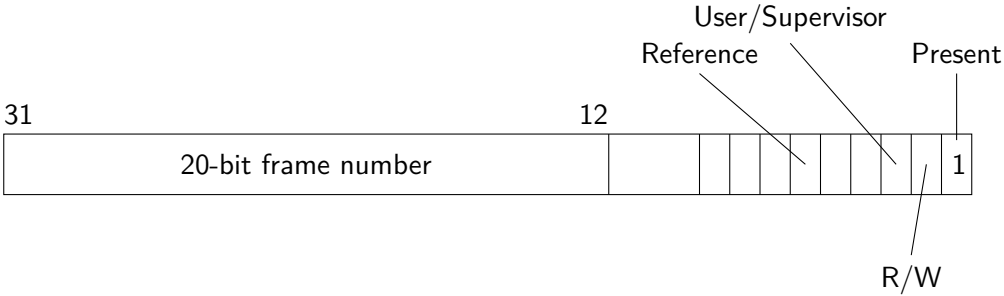

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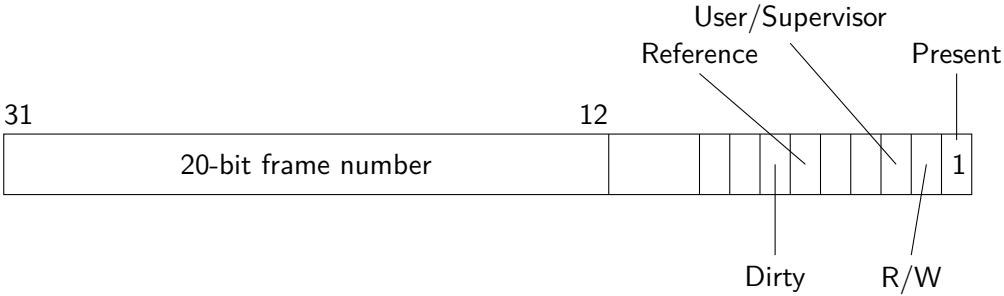

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- Operations are batched to improve disk locality and reduce locking.

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- Who should do all this, hardware or operating system?