

ID1019

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Programming II (ID1019) 2020-03-09

Instructions

- All answers should be written in these pages, use the space allocated after each question to write down your answer (not on the back side).
- Answers should be written in English.
- You should hand in the whole exam.
- No additional pages should be handed in.

Grade

The exam consists of two parts. The first five questions are about basic functional programming: pattern matching, recursion, immutable data structures etc. The first part is the basic requirement to pass the course:

- FX: 7 points
- E: 8 points

The second part, questions 6-9, are about: semantics, higher-order functions, complexity, processes etc. The higher grades are based only on these questions but is only given (and only corrected) if the basic part has been answered satisfyingly (8 out of 10 point).

- D: one question correctly answered
- C: two questions correctly answered
- B: three questions correctly answered
- A: all questions correctly answered

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1 toggle [2p]

Implement a function, toggle/1, that takes a list and returns a list where the elements have changed place two-by-two. If the number of elements is odd the last element keeps its position.

Example: toggle([:a,:b,:c,:d,:e,:f,:g]) should give the answer [:b,:a,:d,:c,:f,:e,:g].

2 push and pop [2p]

Implement a stack: propose a data structure and implement the two functions push/2 and pop/1. The function push/2 should return the updated stack and the function pop/1 should return either: {:ok, any(), stack()} if there is an element on the stack or :no if the stack is empty.

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3 flatten [2p]

Implement a function flatten/1 that takes a list of lists, that in turn can be lists of lists etc, and returns a flat list with all the elements of the original list in the same order. You can use ++ to append two lists.

Example, the call: flatten([1,[2],[[3,[4,5]], 6]]) returns: [1,2,3,4,5,6]

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4 h-index [2p]

An h-index can be used to describe how much and how far one runs. Your h-index is the highest value h such that you have run at least h km at least h times. Your h-index is for example 12 if you have done 12 km or more 16 times but have not done 13 km or more 13 times. It is fairly simple to have a h-index of 10 but a bit tougher to come up to 30.

Implement a function index/1 that, given a list of values that describes runs in km, calculates the h-index. The list is ordered with the longest runs first. You will be able to calculate the value by going through the list only once. The algorithm is simple:

- The initial estimate of the h-index is 0.
- Traverse the list and if the first element is greater than the current estimate,
 - then increment the estaimate by 1 and continue otherwise,
 - you have found the correct h-index.

Example: index([12,10,8,8,6,4,4,4,2])

should return: 5

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5 more compact [2p]

Implement a function compact/1 that takes a tree on the form below and returns a tree where each node with the same key is both its leafs (or if there is only one leaf) had been replaced with a single leaf. The function should be applied recursively so that changes propagate towords the root.

Trees are represented as follows, note that only the leaves have values:

```
@type tree() :: :nil | {:node, tree(), tree()} | {:leaf, any()}
Example:
   compact({:node, {:leaf, 4}, {:leaf, 4}})
should return: {:leaf, 4}
   compact({:node, {:leaf, 5}, {:node, :nil, {:leaf, 4}}})
should return: {:node, {:leaf, 5}, {:leaf, 4}}
```

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6 Formal semantics [P/F]

In the formal semantic that we have discussed we have used a rule call the S-rule or *scoping rule*. The rule is used when we describe how a sequence of pattern matching expressions are evaluated.

In Elixir we have the possibility to use pattern matching in the head of a function definition (see example below). How should we describe the semantics of a function call if we allow patternmatching in the head?

$$\frac{\sigma' = \sigma \setminus \{v/n \mid v/n \in \sigma \land v \text{ in } p\}}{S(\sigma, p) \to \sigma'}$$

Example of how pattern matching in the head of a function definition:

```
def member(_, []) do :no end
def member(x, [x|_]) do :yes end
def member(x, [_|h]) do member(x, h) end
```

This is how we defined a function call when the function was only allowed to have unique variables in its head.

$$\frac{E\sigma(e) \to \langle v_1, \dots : \text{seq} : \theta \rangle \qquad E\sigma(e_i) \to s_i \qquad E\{v_1/s_1, \dots\} \cup \theta(\text{seq}) \to s}{E\sigma(e_i(e_1, \dots)) \to s}$$

How is this changed if we allow patterns in the head (we assume there is only one head)?

$$\frac{E\sigma(e) \to \langle p_1, \dots : \text{seq} : \theta \rangle}{E\sigma(e.(e_1, \dots)) \to s}$$

Reply on the next page.

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Answer to formal semantics:	

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7 Next prime number [P/F]

You should implement a function primes/0 that returns a function that represents the endless sequence of prime numbers. The returned function should when applied to no arguments, return a tuple {:ok, prime, next} where prime is the next prime number and next a function that will give us the following prime numbers.

```
@type next() :: {:ok, integer(), ( -> next())}
@spec primes() :: ( -> next())
```

One way to solve this is to implement sieve of Eratosthenes. When you have found a prime number p (the first one is 2) then you make sure that you do not return any number n that is a multiple of this prime (rem(n,p) == 0). Below is a good start of this algorithm, it is now up to you to implement sieve/2.

```
def primes() do
  fn() -> {:ok, 2, fn() -> sieve(2, fn() -> next(3) end) end} end
end

def next(n) do
  {:ok, n, fn() -> next(n+1) end}
end
```

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a better flatten [P/F]

If you implement flatten/1 as simple as possible you will end up with an algorith with less than perfect time complexity. You will append longer and longer lists and the complexity will be quadratic to the number of elements in the list. You shall now implement flatten/1 but make sure that the complexity is linear with respect to the number of elements in the lists.

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9 parallel map [P/F]

You should implement funktion pmap/ that works as regular map/2 but where each element has been computed in a separat process thus allowing for parallel execution.

You should use the regular map/2 when you spawn the processes and collect the result.

Example: the expression below

$$pmap([1,2,3,4], fn(x) \rightarrow x + 2 end)$$

should return:[3,4,5,6]