

Problem Set 8, Algebraic Stacks

Lecturer: Georg Oberdieck

Due date: Friday, Jan 29. Weights: 20 points each.

Problem 1. Show that the algebraic stack $[\mathbb{A}^1/\mathbb{G}_m]$ does not have a coarse moduli space. (You may assume that you work over \mathbb{C} .)

Problem 2. Show that $B\mathbb{G}_m \rightarrow \text{Spec } \mathbb{Z}$ is a gerbe.

Problem 3. Show that any gerbe $\mathcal{X} \rightarrow X$ over an algebraic space X is a coarse moduli space. (Hint: For start show that for a smooth affine group scheme G over a field k , $BG \rightarrow \text{Spec}(k)$ is a coarse moduli space.)

Problem 4. Olsson, 11.G

Problem 5. (Optional, but looks fun) Olsson, 11.H