

Dual Arm Manipulation - a survey

Christian Smith^{a,*}, Yiannis Karayiannidis^a, Lazaros Nalpantidis^a, Xavi Gratal^a, Peng Qi^a, Dimos V. Dimarogonas^a, Danica Kragic^a

^a*Centre for Autonomous Systems, School of Computer Science and Communication, Royal Institute of Technology, 10044 Stockholm, Sweden*

Abstract

Recent advances in both anthropomorphic robots and bimanual industrial manipulators had led to an increased interest in the specific problems pertaining to dual arm manipulation. For the future, we foresee robots performing human-like tasks in both domestic and industrial settings. It is therefore natural to study specifics of dual arm manipulation in humans and methods for using the resulting knowledge in robot control. The related scientific problems range from low-level control to high level task planning and execution. This review aims to summarize the current state of the art from the heterogenous range of fields that study the different aspects of these problems specifically in dual arm manipulation.

1. Introduction

There is an increasing trend of robots being moved into environments originally designed for human use. In industry, anthropomorphic robots of human size are expected to replace human workers without major redesigns of the workplace. The ability to use human and robot workers interchangeably is thought to be the key to low-cost, flexible automation. As robot use in health care and domestic environments increases, so does the need for robots that are well adapted to these intrinsically human-centric environments. More advanced humanoid robots are expected to mimic human behaviors, act and manipulate objects in ways similar to humans.

This has, during the past few years, led to increased interest for the field of anthropomorphic or dual-arm manipulation. Robot manipulation in its basic forms is a well studied field that has seen remarkable developmements in the last 50 years, but the added complexity of dual or multi-arm manipulation presents many challenges that may not be present in the single manipulator case. This

*Corresponding author

Email addresses: ccs@kth.se (Christian Smith), yiankar@kth.se (Yiannis Karayiannidis), lanalpa@kth.se (Lazaros Nalpantidis), javiergm@kth.se (Xavi Gratal), pqi@kth.se (Peng Qi), dimos@kth.se (Dimos V. Dimarogonas), dani@kth.se (Danica Kragic)

higher complexity means that dual arm manipulation requires more advanced system integration, high level planning and reasoning, as well as viable control approaches. The challenges inherent in dual-arm manipulation, especially in unstructured environments, serve also as a motivator for development in basic research areas, and provide relevant application scenarios for various enabling technologies. Figure 1 showcase the wide variation of dual arm systems.

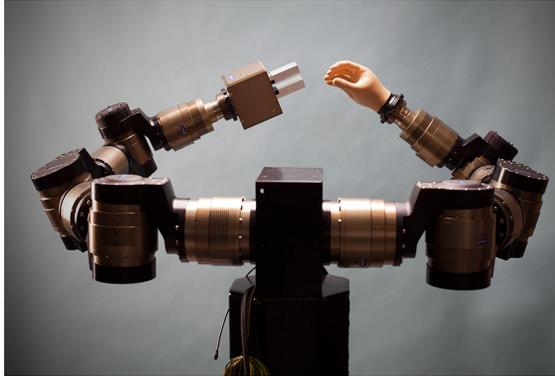
The aim of this paper is to summarize recent developments in manipulator control, modelling, planning, and learning, with special attention given to work that specifically targets the dual arm case. There exist several reviews of each of the abovementioned domains in isolation, but the state-of-the art and future challenges targeted specifically to dual arm cases are not easy to extract from these.

1.1. Background

Some of the very first robotic manipulators were dual-arm systems. Early examples include the manipulators constructed by Goertz in the 1940's and 1950's for handling of radioactive goods [1], that were used in pairs, with the operator controlling one with each hand. The late 1950's also saw dual arm teleoperation setups for deep-sea exploration [2]. NASA's Johnson Space Center started experimenting with anthropomorphic dual arm teleoperators in 1969 [3]. The history of dual arm manipulators and manipulation has been presented in detail in several earlier review papers [4–6].

This early work has been followed by an abundance of applications considering single arm manipulators. These have been a norm for a long time, especially in the 1980's and 1990's, when a lot of initial work on visual servoing was developed [7]. More recent developments in the areas of humanoid robots as well as the work on learning by imitation, has opened for use of dual arm setups. There are several independent factors that motivate the use of dual arm setups:

- **Similarity to operator** - The common motivation for using dual arms in teleoperation setups is that the operator is used to performing bimanual tasks, and having two arms at the slave site means that the operator's bimanual skills can be transferred to the remote site [8–12].
- **Flexibility and stiffness** - By using two arms in a closed kinematic chain, the stiffness and strength of a parallel manipulator can be combined with the task flexibility and dexterity of a serial link manipulator [13].
- **Manipulability** - Dual arm manipulation is motivated with the ability to control both parts of for example a typical peg-in-hole task, with one arm positioning the peg and one arm the hole [18], or screw assembly, where one arm controls the nut and the other the bolt [19]. The high degree of task space redundancy for dual arm systems has been used for optimal performance for domestic tasks such as dishwashing [20].
- **Cognitive motivation** - Humanlike dual-arm setups have been used to explore how human-like physical interaction relates to cognition [21]. Likewise, in an HRI context, it has been argued that since humans have an



(a) Semi-anthropomorphic robot at CAS/KTH



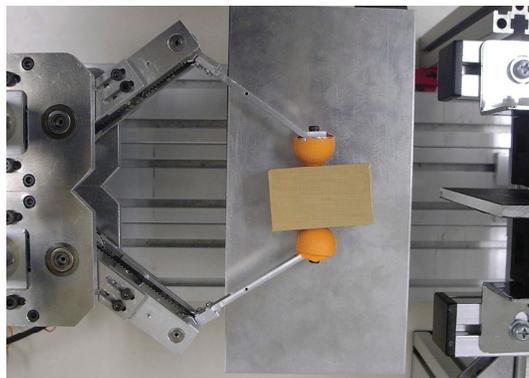
(b) Dual industrial manipulator SDA10 [14]



(c) Mobile Dual manipulator PR2 [15]



(d) Double single-arm setup at PRISMA Lab [16]



(e) Gripper with two articulated fingers [17]

Figure 1: Illustrative examples of different types of dual manipulator setups. All images are used with the permissions of the respective owners.

intuitive understanding of bimanual manipulation, the actions of a dual arm robot are easier for an observing human to understand and relate to [18, 22].

- **Human form factor** - With the advent of robots that are expected to work in environments originally intended for humans, it is claimed that robot manipulators will need to have human-like form to perform well [15, 23–25], even though some acknowledge that this may place significant constraints on performance – especially power and robustness – with contemporary hardware [22, 26]. Recently, there have been several dual arm systems proposed for industrial use, with the motivation that dual arm systems occupy less space and have lower cost, as compared to two single arm units. Also the ability to replace human workers with robots without redesigning the workspace is used as a motivation [14, 27–30].

This wide range of motivations for dual arm robots has led to the development of a large variety of hardware platforms, see Figure 1 for a few examples. Even though the manipulator platforms may be very heterogeneous, there are several common problems that have to be solved, as discussed in the following sections.

1.2. Definition

The term “dual arm manipulation” does not have a specific agreed-upon definition. Manipulation can be defined as physically interacting with an object, exerting forces on it in order to move or reshape it. However, “dual-arm” is not trivial to define. Two dexterous fingers mounted on the same hand may manipulate a small object (Fig. 1e) using the same principles as two separate manipulators that are moving a large object (Fig. 1d). In fact, many authors do not distinguish between multi-agent or multi-arm systems. A broad definition of cooperative manipulation is given instead, and covers the spectrum from different fingers on the same hand to teams of separate robots cooperating [31, 32]. In terms of bimanual grasping, a detailed classification extending Cutkosky’s grasp taxonomy for single-handed grasps to bimanual grasping has also been proposed [33].

One proposed general classification for dual arm manipulation makes distinctions between non-coordinated manipulation, where the two arms are performing two different tasks, and coordinated manipulation, where the arms perform different parts of the same task. Coordinated manipulation is in turn divided into goal-coordinated and bimanual manipulation. For goal-coordinated manipulation, the arms are not physically interacting with one another, but both are solving the same task, with typing different keys on a keyboard given as an example. Bimanual manipulation is defined as physically interacting with the same object [34], see Table 1. Of these, the first definition delimits systems that may consist of two separate manipulators performing tasks independently of one another. As there is no explicit coordination, there is no intrinsic difference

to single-arm systems, and the analysis does not need to differ from single-arm setups. The two later cases include significant amounts of spatial and temporal coordination aspects that set them apart from single-manipulator systems. The papers presented in the present review all belong to one of the the two latter classes, and have been classified accordingly in Table 2. This table also classifies the papers according to their field of study, as a fast reference guide.

In the following section, we structure and review the state of the art in the area starting from modelling paradigms and finishing up with different application examples.

Table 1: Hierarchy of Dual Arm Manipulation [34]

Dual Arm Manipulation		
Un-coordinated	Coordinated	
	goal-coordinated	bimanual
example: <i>The left arm is palletizing parts while the right arm is welding an unrelated seam.</i>	example: <i>Both arms are palletizing parts into the same box.</i>	example: <i>Both arms are lifting and moving the same box full of parts.</i>

1.3. Dual Arm Systems

There exists a wide variety of robot platforms used for dual arm manipulation. While some research is carried out on systems built by simply placing two single-arm manipulators to share the same workspace [9, 16, 129], considerable effort has also been put into constructing dedicated dual arm platforms. Some of these put the effort on manipulation capability, and target industrial manufacturing applications, such as the Toyota Dual Arm Robot [132], the Yaskawa Motoman SDA10D [14], the ABB Frida [135] the Korea Institute of Machinery & Materials dual arm robot [28], the Kawada Hiro [29], the SHARP household robot [27], or the Pi4 Workerbot [30], each of which is shaped like a “torso”, and primarily intended for stationary deployment. Similarly, prototypical torso-type robots have also been constructed for different research purposes, like the Umass. Dexter [21].

A special class are torso-type robots intended to perform some of the tasks traditionally performed by human astronauts, like the NASA Robonaut [136] and CSA Dextre [137]. These can be mounted at the end of large manipulators, and have limited mobility.

Others put the emphasis on mobility, for operation in human environments. Examples include Umass. Ubot [138], Tohoku University Mr Helper [134] Willow Garage PR2 [15], DLR Rollin Justin [24, 139], DFKI Aila [140], KIT ArmarIII [22], TUM Rosie [141], Waseda Twendy-one [126], and GATech Domo [26]

Table 2: Literature Summarizing Table

Domain		Goal-Coordinated	Bimanual
Modeling	Fixed Grasps	[32, 35]	[16, 32, 36–42]
	Non-fixed Grasps		[43–63]
Control	Hybrid F/P		[64–77]
	Impedance		[78–80]
	Position-based		[17, 76, 77, 81–89]
	Vision		[74, 90–101]
Learning		[102]	[103–105]
Planning and Grasping	Motion planning		[106–115]
	Task planning		[116–121]
Applications	Domestic	[22, 122, 123]	[95, 98–100, 122, 124–128]
	Industrial-Space-Hazmat	[28, 129, 130]	[28, 92, 94, 96, 97, 101, 131–134]

and Cody [142]. Yet others place the emphasis on completely mimicking human appearance and structure, such as the Honda Asimo [143] and the Kawada HRP Series [144]. A special class consists of robots especially intended for teleoperation work, where the appearance is not necessarily biomimetic, but the workspace is made to match that of the human operator as closely as possible [8–12, 145].

1.4. Applications

While many dual-arm systems are pure research platforms mainly used for development and evaluation of basic technologies and principles, there are also several examples of practical applications. This section presents typical applications for dual arm manipulation, technical aspects of these systems are detailed in later sections.

As an example of *domestic* applications, folding laundry has been studied in several cases. These applications share the common aspect that they use vision to detect folds and corners, but differ in how the manipulation is performed. In [124], specialized “inchworm type” grippers on an anthropomorphic robot are used to physically trace edges. In [95] autonomous towels folding is demonstrated on the PR2. Stereo vision is used in conjunction with a vision-based grasp point detection algorithm that detects the corners of the towel, and a sequence of vision-based re-grasps and manipulations are performed towards the towel folding goal. In [122], the PR2 is used to grab one corner of a towel and lift

it up and let gravity unfold it to detect further corners using vision. Early considerations about using a visually guided dual-arm robot to interact with clothes have been reported in [127], and in an industrial setting [129] focuses on fixed-frame vision-based techniques to detect and model the shape of clothing items to manipulate with industrial robots, and compare the performance of grabbing the highest point of a pile of towels with grabbing a rough approximation of one end of a towel. In [100] a dual-arm robotic setup for clothes manipulation using a pair of industrial robots (Kawasaki Js2 and Yamaha Rch-40) is presented. Images from a single fixed-position workspace camera are processed so as to detect whether a gripper has reached a corner.

Other domestic application types have also been described for dual arm robots. In [126], the TWENDY-ONE robot is presented. The robot is developed for providing attendant care and kitchen support for the elderly. In [123], a pair of dual arm anthropomorphic robots are used to make pancakes. The paper focuses on high level reasoning, planning and systems integration. In [27], a smaller dual arm robot is demonstrated to serve tea using preprogrammed motions and teaching by demonstration. Loading and unloading a dishwasher with the anthropomorphic robot ARMAR-III has been described in [22, 125]. In [99] the work is extended with a visual servoing controller for dual arm grasping and manipulation tasks. The control framework allows it to track multiple targets. A prototype robot named RIBA with an anthropomorphic torso is proposed to perform health care related lifting tasks, such as transferring a human from a bed to a wheelchair [146].

In [96] a cooperative scenario between two 6-DoF dual-arm mobile robots is considered. The two independent robots grasp and move a box to a target position using visually estimated poses of the robots and the box. In [134], a control system of a mobile dual-arm robot for handling a single object in cooperation with a human is presented. The robot system performs cooperative manipulation task with a human, or transports the object autonomously.

In *industrial* settings, a typical application for dual arm systems is parts assembly. Preprogrammed gearbox assembly has been described in [132], while [28] describe programming by demonstration for similar tasks. Another area studied is material reshaping. In [131], a dual arm system is used to bend metal parts, and in [133], a dual arm system is used to fold cartons into predetermined shapes. Finally, [130] investigates the Learning-from-Observation paradigm for robot learning for industry-oriented assembly tasks for rigid polyhedral objects.

In [94], a dual-arm crew-assisting robotic system for space exploration missions is examined. The goal is the system to autonomously grasp objects using a vision and force-based control strategy. The system consists of a four-wheeled rover and two robotic arms, each with a camera mounted on the arm's end-effector. An image-based visual servoing is used in conjunction with fiducial markers to move each of the robot's arms.

Table 3 summarizes the different hardware platforms used in the papers cited in this work.

Table 3: Characteristics of dual-armed robotic systems.

Reference	Robot	Base	Vision System	Force/torque sensing	DoF	End Effector
[147–149]	Samsung AM1	fixed	E stereo	–	2×4	NA
[91]	HRP2	2×6Dof legs + 2DoF waist	A stereo	wrist F/T	2×6	Articulated hand
[132]	1 DoF prismatic	-	-	-	(2×5)	specialized tool
[14]	SDA10	fixed	-	-	2×7	specialized tool
[92]	SMART3	fixed	W multi-camera	wrist F/T	2×6	Parallel gripper
[94]	EGP	wheeled	mono E	wrist F/T	2×7	Exchangable tools
[95]	PR2	wheeled + adj. height	stereo A / mono E	Gripper F	2×7	parallel gripper
[96]	Dr Robot i90	wheeled	mono A+W	–	2×5	gripper
[97]	PowerCube	fixed	3 IR sensors W	–	2×7	Parallel gripper
[99]	Armar III	wheeled + 3DoF waist	2 stereo A	Joint T	2×7	Articulated hand
[100]	Js2 & RCH40	fixed	mono W	Finger F	6+5	Exchangable grippers
[101]	Robonaut I	wheeled	stereo A	joint F/T	2×7	Articulated hand
[150]	custom	free-floating	stereo A	–	2×6	Gripper
[126]	Twendy-One	wheeled + 4 DoF waist	stereo A	wrist F/T	2×7	Articulated hand
[134]	Mr. Helper	wheeled	stereo A	wrist F/T	2×7	gripper
[130]	custom	fixed	multiview stereo A	wrist/finger F/T	2×7	Articulated hand
[24, 139]	Rollin Justin	wheeled + 4DoF waist	stereo A	joint/finger F/T	2×7	Articulated hand
[30]	Pi4 Workerbot	fixed	ToF A& mono	wrist F/T	2×7	Exchangeable tools
[146]	RIBA	wheeled	stereo A	Tactile skin	2×7	fixed shape
[143]	Asimo	2×6Dof legs + 2DoF waist	stereo A	wrist F/T	2×7	articulated hand
[142]	Cody	wheeled + adj. height	stereo A	wrist F/T	2×7	fixed shape
[26]	Domo	fixed	stereo A	joint T	2×6	articulated hand
[141]	Rosie	wheeled	stereo, ToF A	joint T	2×7	articulated hand
[140]	Aila	wheeled + 4DoF waist	stereo, ToF A	wrist F/T	2×7	fixed shape
[19]	Custom	fixed	Stereo W + 2×mono E	finger F/T	2×7	3-finger hand
[79]	PUMA 560	fixed	-	wrist F/T	2×6	-
[16]	COMAU Smart-3S	fixed	-	wrist F/T	2×6	-
[69]	A465 + A255/CRS Robotics	fixed	-	wrist F/T (A465)	6+5 (2×3 used)	-
[66]	SCARA type	fixed	-	wrist F/T	2×3	-
[17]	2 planar fingers	fixed	-	-	2×2	rubber finger-stalls
Abbreviations:						
H = vision system mounted on active head			ToF = Time of flight			
W = vision system fixed in workspace			F = force sensor			
E = vision system on end effector			T = torque sensor			

2. State of the Art

The goal of this section is to structure and review the work in dual arm systems. We start by providing an insight and review the work on the modelling paradigms. This is followed by an overview of control theoretic approaches, where the aspect if vision based control is studied in more detail. Then, we review the work on planning and relation to grasping and manipulation of objects that consider dual arm setups. We also review different learning approaches and finish up by presenting a number of interesting applications.

2.1. Modeling

The study of dual-arm robotic systems is an extensive research area and there is a vast literature concerning how to model the system to achieve grasping and manipulation of an object or an object-independent target. Part of this section is based on textbooks [32, 43, 151, 152] and review papers on robotic grasping and manipulation [153, 154]. This section presents literature regarding the characteristics of closed chain systems, such as the grasp matrix, the internal forces, the restraint properties, the force/load distribution, the inherent redundancy as well as the implications of manipulation of deformable sheets and the use of mobile manipulators in dual arm manipulation.

The modeling of a robotic system which consists of multiple cooperative manipulators employed to manipulate an object, heavily depends on the type of the interaction between the end-effectors and the manipulated object. There are two main categories of cooperative manipulator tasks:

1. *Cooperative robot manipulators holding an object with fixed grasp points (Fig. 2a)*: The object is assumed to be rigidly attached to both manipulators, and hence no relative motion can arise between the grasping points and the grasped object. Fixed grasps enable complete interaction by transmitting every motion from the arms to the object while imposing bilateral contact constraints. The use of fixed or tight grasps is appropriate for robots having two arms to perform a bimanual task [16, 32, 36, 152] using for example power (whole hand) grasps [153].
2. *Cooperative robot manipulators holding an object by means of contact points or contact areas (Fig. 2b)*: Relative motion between the object and the manipulators is enabled while rolling or rolling/sliding contacts are allowed. The contact point (contact area) interaction imposes a selection on the force/motion components transmitted to the object while contact constraints are unilateral. In this case a pulling force is translated to contact loss. Unilateral constraints and point (area) contacts are more suitable for the modeling of a robotic hand that uses two fingers to manipulate an object [44–46]. This type of modeling clearly describes the anthropomorphic multi-fingered hands [155] which enables “dexterous manipulation” [156] as illustrated in Bicchi’s and Kumar’s theoretical survey for robotic grasping [157].

In the literature the first category refers to the modeling of dual arm manipulation with fixed grasps (Fig. 2a) while the second mainly refers to manipulation of an object by fingers (Figs. 2b, 1e). These are both covered here for two reasons: 1) ideas and techniques developed for object manipulation with the fingers of a hand can be employed to solve problems in dual arm manipulation without rigid grasps (c.f. Fig. 1d), and vice versa, as is shown in the two recent works [158] and [25] referring to categories 2 and 1 respectively. 2) The combination of the two categories constitutes the dual arm manipulation problem with dexterous hands with non-rigid grasps. In this case additional closed chains are embedded in the typical arm-object-arm chain; for example, two arms with robot fingers in contact with the object through unilateral constraints has been considered in [47].

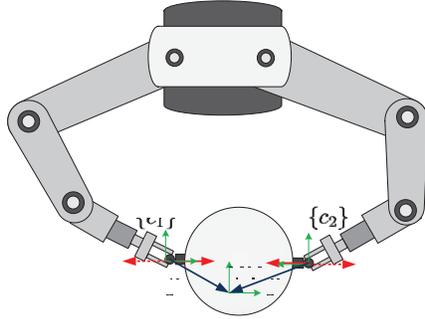
The *Grasp Matrix* formally describes the kineto-static relationships between the velocities and forces at the contact or grasp points, and those mapped at the center of the object mass. The grasp matrix for two manipulators holding an object (Fig. 2a) is mapping the generalized forces from the frames $\{c_i\}$ attached at the grasping points to a frame $\{o\}$ attached at a fixed point of the object (typically the center of mass) can be defined as follows:

$$\mathbf{G} = \begin{pmatrix} \mathbf{I}_3 & \mathbf{O}_3 & \mathbf{I}_3 & \mathbf{O}_3 \\ -\mathbf{S}(\mathbf{p}_{oc1}) & \mathbf{I}_3 & -\mathbf{S}(\mathbf{p}_{oc2}) & \mathbf{I}_3 \end{pmatrix} \quad (1)$$

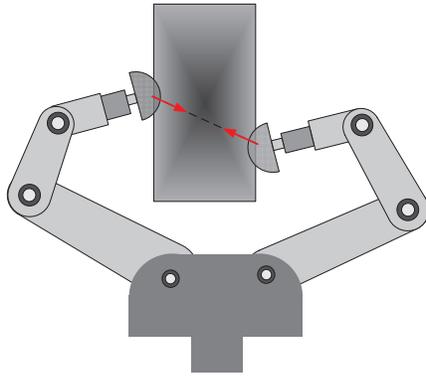
where \mathbf{p}_{oci} is the relative position of frames $\{c_i\}$ and $\{o\}$, \mathbf{O}_3 , \mathbf{I}_3 are 3×3 null and identity matrices respectively and $\mathbf{S}(\cdot)$ is a skew-symmetric matrix being used in order to produce cross-products. The virtual-stick, which is defined for each manipulator to denote the relative position between the end-effector and a fixed point of the object, can be regarded as the core of the kineto-static formulation [32]. On the other hand, the *cooperative task-space formulation* directly defines the task space variables as absolute and relative motion of the dual arm manipulation system, can be applied even for tasks which do not require physical interaction of both arms with the object [152]. In case of contact points (contact areas) the contact modeling is crucial to derive the grasp matrix; in this case, \mathbf{G} given by (1) can be characterized complete grasp matrix, while the inclusion of selection matrices for the components of forces/torques transmitted through the contact yields the grasp matrix.

In particular, the contact modeling determines the components of the end-effector wrenches at the contact point which are going to reach the object and thus the components of the velocity which are transmitted to the object. There are three main type of contact models [151, 153]:

- **Frictionless Point Contact** is used to model cases wherein very small contact areas arise allowing the slippage between the contacted parts.
- **Frictional Point Contact or Hard Finger model** approximates the cases of small area contact able to transmit tangential frictional forces. When very small contact areas arise the friction moment around the contact normal is negligible.



(a) Top view of dual arm setup manipulating a pan by means of fixed grasps



(b) Two soft fingers manipulating an object

Figure 2: Dual manipulator setups

- **Soft Contact or Soft Finger model** is used when the fingertip or end-effector material is soft enough and thus capable of producing significant contact areas. Arbitrarily large contact area enables fingertips to exert frictional torques around the contact normal.

Soft contact may intuitively seem more practical, but is not commonly utilized; details on soft contact modeling for dexterous manipulation can be found in [48].

The type of contacts described above do not affect modeling of dual arm manipulation with fixed grasps but it is important for cooperative manipulation in cases of the end-effector cannot achieve a fixed grasp. The grasping formation as well as the type of contact (in the case of non-fixed grasp) discussed above are used in order to derive the constraints that governs the manipulation task. The Lagrange multipliers associated with differentiable algebraic constraints have been used in order to model the forces in dual arm manipulation arms with no relative motion[36]. Non-holonomic constraints are imposed in case of rolling motion between the manipulators and the contacted object [44]. In [37] the dynamic modeling of a dual-arm manipulator using constraints has been

presented along a comparison between experimental and simulation results. In case of manipulators with soft end-effectors, like for example soft fingers, the normal interaction force is the resultant of the spring forces, and consequently it is related to the material deformation and to the deformation velocity in the case of deformable viscoelastic materials [63]. Hence, for compliant contacts the interaction forces are functions of the system state while for rigid contacts they depend on both the system states and the system inputs [38]. Modeling of frictional contacts for the fingertips manipulating an object typically obeys the Coulomb law and thus the magnitude of the tangential frictional forces are proportionally related to the pressing forces [151]. The replacement of the sign function for Coulomb law by smooth functions is proposed in [63]. The friction coefficient determines the cone of friction and is subsequently directly involved in the slippage detection condition. The part of the exerted force which does not contribute to the motion of the object is the so-called internal or squeeze forces. Recently, port-Hamiltonian modeling for object manipulation by soft fingers has been proposed in order to describe uniformly the transition from the non-contact case to the visco-elastic contact case [62]. The virtual linkage [39] and virtual truss models [49] have been used in order to characterize the range of the internal forces in multiple cooperative manipulators, for the cases of a tightly grasped object and of an object manipulated by fingertips.

In the case of dual arm manipulation using fixed grasp points, the restraint properties such as force or form closures are not of interest. In the case of dual arm manipulation using contact points or contact areas, the force and form closure properties have been extensively studied in the literature. A survey of the state-of-art before 2000 can be found in [153]. The difference between the form and force closure properties lies in the contact model that is assumed. The *force closure* properties rely on the ability of the contact to exert frictional forces which are dependent on the exerted normal force. The *form closure* property is more restrictive since it relies on a frictionless contact model. In addition, passive and active closure properties have been introduced in [50] to characterize the ability of the grasping mechanism to transfer motions to the grasped object.

Han et al. formulate the grasp analysis problems as a set of convex optimization problems involving linear matrix inequalities, and show the simplicity and efficiency of this LMI formulation [51]. The choice of optimal grasp synthesis and its evaluation, as well the force distribution problem for object grasping [52, 153, 159], are of fundamental importance and has been extensively explored in recent publications [53–56].

The problem of force distribution for an object manipulated by fingers is analog with the load distribution problem for cooperative constrained manipulators. The load distribution problem is related to finding ways to share the load to each arm according to its actuation ability [152]. New perspectives in the grasp synthesis arise by considering the concept of “postural synergies” or “hand configuration subspace” implying underactuated system of cooperative manipulators [57, 58].

Recently has also been significant interest in understanding how to manip-

ulate deformable objects such as rope, napkins and cloth [35]. Wakamatsu et al. [60] analyze stable grasping of deformable objects based on the concept of a bounded force closure, and apply the proposed method to linear deformable objects. Modeling of deformable objects is an active research area and different approaches have been considered. A useful survey can be found in [160]. In robotics, low-complexity representations for the deformable objects should be the objective. One simple and recently well used representation for the folding manipulation is to consider the deformable object as a mechanism, with creases as revolute joints and facets as mechanism links. This has been successfully exploited in automatic paper folding [161] and industrial carton handling [162].

In dual arm manipulation, redundancies may arise even in cases where two single arm manipulators with no inherent redundancies are used. The redundancies are a direct result of the cooperative task definition. The controlled task space variables are 6 generalized positions while internal forces also can be controlled. Redundancies are also useful for increasing the robotic hand or the cooperative dual-arm manipulation system dexterity. The kinetostatic performance indices such as velocity and force manipulability ellipsoids have been formally expanded to evaluate performance quality for cooperative arm manipulation [40] and mechanical hands with cooperative fingers [59]. The effect of softness at the contact area on the manipulability and the grasp stability of a system which consists of multiple manipulators grasping an object have been recently studied in [61].

The modeling of dual arm manipulators systems becomes more complex when the robot arms are mounted on mobile or free-flying platforms. Specifically, the modeling of mobile manipulators holding a deformable object is considered within the framework of Kane’s approach in [41]. The dynamic equation of motion for dual free-flying arms are described in [42].

2.2. Control

In this section we review the main results on both dynamic and kinematic control approaches considering manipulation of an object using cooperative manipulators. Thus, we provide an overview of important works of the literature, in which the underlying solution is designed by closing the loop at the operational space and/or the interaction force level; in this case the operational space is mainly defined based on the object position, while in some cases task coordination positions are used. We here exclude task hierarchical levels used to achieve the same objective by combining higher level grasp and motion planning (producing the desired joint trajectories) with lower level joint space control that drives the robot to the specific configuration. Subsection 2.1 as well as the survey [153] describe several higher level grasp and motion planning techniques specific for dual arm setups, while standard control techniques for joint position regulation and tracking for single arms can be used without any modification. Hence, this section mainly treats papers that consider force/motion control and closed chains (either flexible or rigid) formed by the manipulators and the object. In robot control literature there are two main categories of problems: regulation and trajectory tracking. Such categorization can be adopted for dual-arm

manipulation control to distinguish between the cases of a constant and a time dependent desired object pose and internal forces.

The trajectory tracking problem has mainly been treated using *input-output linearization* methods which are in general model-based, where the estimation step requires the knowledge of the robotic system structure. Nonlinear feedback techniques have been used to linearize the dynamic equations of the closed chain motion [38]. The constraints imply that one part of the output, which is the interaction forces, depends on the input; thus input integrators have been utilized. Input-output linearization systematic approach has also been used for 3D rolling contacts [44] and for point contact with friction and compliance [64]. The application of input-output linearization for cooperative manipulation through compliant contacts enables the control of the normal force without employing input integrators, but increases the required design and implementation effort by giving rise to the singularity of the decoupling matrix.

Hybrid force/position control and *impedance control* have been extensively used in dual-arm manipulation tasks. For a single arm manipulation setup, hybrid force/position control is based on the decomposition between the motion and exerted force control loops, while the impedance control method simultaneously controls the motion along every direction in order to achieve a desired dynamic interaction between the manipulator and the environment. The basic structures of hybrid force/position and impedance control for dual-manipulator systems manipulating an object which may be in contact with the environment as well as a comparison of their performance can be found in [45]. An impedance controller may lack in precision of controlling the position of an object as compared to hybrid force/position control but can be applied without any switching procedure between contact and non-contact cases.

Hybrid force/position control for dual-arm manipulation tasks is mainly based on the decomposition of the object motion and the internal forces space using kineto-static filtering and thus enable the direct control of internal forces which is crucial in many dual arm manipulation applications. In [65], the authors propose independent nonlinear feedback with hybrid force/position control of each robot of the dual-robot setup; the controller is driven by reference trajectories which are obtained by a centralized planner aiming to achieve coordination for a pushing and pulling operation. Force/position hybrid control has been proposed in [66] in order to control the internal forces at a desirable level and to enable load distribution of the control effort simultaneously with the main task of object position tracking; cooperative tasks with respect to rigid objects such as screwing a nut onto a bolt have been considered. A feedback linearizing input and the grasp matrix have been exploited in [67] in order to decompose the object motion control directions and the internal force directions. This work in addition proposes a hybrid control for rolling and rolling/sliding contacts. Exploiting the orthogonality between the spaces of active and passive force closure, a decomposing control input which enables the simultaneous control of internal forces and object motion is proposed in [68]. Adaptive passivity-based hybrid force/position control has been designed in the joint space by incorporating the law of Slotine-Li for dynamic parametric uncertainties [36] and the need of

velocity measurement in such type of controllers has been studied in [69]. Decomposition of the force and position control loop is also used in a model-based control scheme that requires derivatives of force measurements in order to control a cooperativeness error which is related to the velocities of the arms lying on the normal to the object directions. The corresponding error can then be regarded as a measure of pushing/pulling forces, [70]. Hybrid force/position has been also combined with vibration suspension control in order to control a dual-flexible arm system manipulating a rigid object, [71]. Moreover, hybrid control has been utilized for underactuated cooperative manipulators — in which case recalculation of the dynamic load-carrying capacity is proposed in order to verify the ability of the manipulator to execute the cooperative task [72].

Schneider and Cannon [78] have initially defined the desired impedance for the object dynamics in contact with the environment enlightening the cooperative perspective of impedance control. The generic structure of an impedance controller requires the acceleration of the object in order to be implemented, but estimates as well as finger force sensing can be used instead, [45]. Furthermore, the impedance control can be used for internal force control as described in [79, 80]. Recent research has proposed also the combination of a decentralized impedance controller for each manipulator with centralized impedance control for the manipulated object [16]. The last results in the use of impedance control in dual arm manipulation can achieve a desired impedance for the motion of the object with respect to its environment as well as desired impedance for the motion of its manipulator with respect to the object (indirect internal force control). Both impedance and hybrid force/position tracking control are based on the robot and object dynamic model.

The ideas of sliding mode control, robust adaptive control as well as neuro-adaptive control have also been used for cooperative manipulator tasks in order to cope with dynamic *model uncertainties* by assuming a closed chain model. Intelligent control using neural networks and fuzzy systems have been proposed in [73] and [87] respectively in order to cope with dynamic model uncertainties. Neuro-adaptive control with visual feedback has been also proposed in order to deal with Jacobian kinematic uncertainties [74]. Such type of techniques are straightforward generalizations from the one to multiple manipulator case, since dynamic model uncertainties affect the dynamic response of the controlled system in a similar way in both cases.

In case of regulation the entire dynamic model of the robotic system, however, is not required and hence simpler control structures have been proposed. In the last decade, effort has been put into designing *regulators for the grasping and manipulation of an object by a pair of robotic fingers*; this effort can be transferred to the context of dual arm manipulation. In [17] two rigid fingers have been used to control the object position and orientation simultaneously, with rigid object grasping. The stability proof for this is based on passivity and proposes the concepts of stability and transferability on a manifold in order to cope with redundancies. The aforementioned concepts do not require the definition of additional tasks and augmented projection method for task prioritization as in [81]. Several extensions on this work have been done to-

wards i) control of whole arm and dual arm with fingers for achieving grasping and manipulation ([82] and [47] respectively), ii) 3D object motion [46], and iii) multiple fingers manipulating an object [17]. The implementations of the aforementioned controllers use estimates of the orientation and position of the objects in order to avoid the use of vision, but position-based visual servoing can also be used. Simple controllers accompanied by passivity-based stability proofs have also been proposed for the case of soft fingers manipulating rigid materials [83], [84]. The softness of the fingertip in general enhances dexterity and but also requires measurements of the fingertip deformation and some additional control terms, specifically in the case of deformable fingertips [84]. Passivity-based regulation for three robotic fingers manipulating an object in the 3D space with 3D deformation have been considered for grasping and manipulation [75]. Object-level impedance behaviour without inertia shaping has been applied to multi-finger hands for dynamic dexterous manipulation [158] and extended to the dual-arm manipulation problem [25].

The aforementioned work considers an object-centered workspace. On the other hand, there is work which considers *the cooperative task-space formulation* for fixed-grasp typical dual arm manipulation problems and proposes very simple control laws based on PD with gravity compensation structure. The two basic approaches are the following: i) finding the desired joint values that correspond to the cooperative task using inverse kinematic algorithms and substituting them within a joint space PD control scheme [76], and ii) finding the desired position of each manipulator based on the desired absolute and relative position of the task-space formulation and substitute them within the robot's operational space PD controllers [77]. The regulators can be also combined with internal force feedback and can be regarded as hybrid force/position controllers since they exploit the kineto-static filtering of the control actions. Recently, kinematic control for performing dual-arm manipulation using dual quaternions has been proposed [88]. The dual quaternions have been used to define the "cooperative dual task-space" since they simultaneously describe the position and the orientation of a rigid body.

The perspective of control of dual- or multiple-arm manipulation systems via the *coordinated motion of multiple autonomous agents* mainly considers robot arms mounted on mobile platforms and is an ongoing research topic. In this case additional issues such as obstacle avoidance and exchange of information between the manipulators need to be taken into account. Kinematic control for nonholonomic manipulators grasping a deformable object has been applied in order to move between two states in a known static environment with obstacles without over-stretching the object [89]. Navigation functions with an obstacle avoidance term have been exploited to achieve the control objective. The tracking of fixed-base, free-floating, and free-flying co-operating manipulator systems have been treated by using inverse dynamics control algorithms with motive force [42]. Schemes with one agent acting as a leader and one or more agents acting as followers have been considered for the coordinated motion of multiple mobile manipulators holding a single object [85]. The leader knows the desired trajectory of the object while the followers estimate it and manipulate

the object by coordinating with the leader. Synchronization of the manipulators has been addressed in [86] where an adaptive synchronized controller proposed to drive the synchronization error to zero and hence maintain certain kinematic relationships between the cooperative manipulators. The work in [86] has been extended in [163] to accommodate a control loop for the internal forces under both flexible and rigid constraints. However, the proposed direct force cancellation technique cannot be applied in general.

2.3. Vision and Visual Servoing

Visual feedback has been widely used for providing robots with the ability to perceive and interact with their environment [23]. Vision based techniques were originally developed for single-armed robots and have been later adapted for use in dual-arm setups. As a result, explicitly dual arm-oriented vision systems are not commonly found in the relevant literature. In practice, there are two different ways for visual information to be exploited. The first one is by establishing a vision based closed-loop position correcting procedure, a technique which is known as visual servoing. The second one is by observing the environment once, calculating a desired movement and then applying it without any further corrections.

The task of visual servoing is to establish a closed control loop for a robot to manipulate objects within its environment using visual feedback [7]. The concept and the techniques of visual servoing have been described by Hutchinson in 1996 [164] and more recently by Chaumette in [165, 166]. Visual servoing techniques for dual-arm robots are usually extensions of the techniques used in the simpler case of single robot arms. As such, they can be also classified into the same categories, i.e. *image-based*, *position-based*, and *hybrid* methods.

Image-based visual servoing uses the difference between the observed and desired position of selected features on the 2D image plane. As such, no pose estimation is required and the calculations that provide the robot control signals can be performed very rapidly. As an example, an image-based visual servoing technique is presented in the work of [74] that uses the image Jacobian matrix to control multi-fingered robot hands. Furthermore, the use of planar markers as the guide for image-based visual servoing has been exploited in [94].

On the other end of the spectrum, position-based visual servoing uses the difference between the observed and desired pose of the tracked object in the 3D space with respect to the camera. A 3D model of the object is reconstructed based on some extracted features and its pose in the Cartesian space is calculated either by exploiting information of a pre-captured model (for monocular vision systems) or by taking into consideration depth information as well (for visual sensor arrangements providing depth). Within this context, the anthropomorphic robot ARMAR-III has been used to perform grasping of objects considering the possible configurations of both the left or the right arm [98]. The same platform has been used in [99] to demonstrate a position-based visual servoing controller for dual arm grasping and manipulation tasks. Furthermore, [92] also uses a position-based visual servoing scheme for the control of two

robot manipulators, and [19] uses the end-effector mounted camera on each arm to align the parts held by each hand to perform an assembly task.

Vision sensors can also provide general information about the context or the elements of a scene. Such information could be exploited in ways different than for controlling the arms, i.e. for understanding a scene, or localization purposes. As a result, active vision has to do with observing the environment and making decisions about the robot's next actions. However, this kind of decision-making is not a closed loop control scheme

Visual systems can be characterized according to where their point of view is placed. Most of the proposed systems employ one (or possibly a combination) of the following camera configurations:

- **End-effector mounted** - This configuration, often also called *eye-in-hand* configuration, has the camera mounted on the robot's end-effector. This configuration provides a predefined geometric relationship between the position and orientation of the camera with respect to the arm. A typical example of such a configuration in a dual-armed robot are the visual sensors placed on the end-effectors of each of the Willow Garage PR2 robot's arms [15].
- **Fixed in the workspace** - This configuration provides a constant, stable place for the vision system to observe the scene.
- **Active head** - Active heads provide the vision system with a limited flexibility of translating and rotating with respect to the arms' reference system.

These configurations are graphically depicted in Fig. 3.

The first two configurations, depicted in Fig. 3a and Fig. 3b, are more commonly found in industrial and generally non-domestic robotic setups. The case of an end-effector mounted vision system has been studied in [90]. The work of [94] examines a robotic system for space exploration missions that has two arms, each with a camera mounted on the end-effector and uses an image-based visual servoing strategy. Recently, the popular PR2 robot has also adopted, apart from an active head, an eye-in-hand camera configuration with limited reported results yet. The configuration of two cameras fixed in the workspace is used in the work of [92], which is further discussed in [93], for vision-based control of two industrial arms. Finally, the system presented in [97] also uses a fixed vision system to control a robot having two industrial arms.

On the other hand, the active head configuration, depicted in Fig. 3c, is a common choice for anthropomorphic robots found in domestic environments, due to its similarity to the human vision apparatus. An example of such a setup is the ARMAR-III robot [125], whose vision system is comprised of an active head and a double binocular camera setup for wide and narrow angle vision, respectively. Furthermore, the work of [126] presents the TWENDY-ONE elderly assisting robot that employs a 3-DOF active head for its stereo vision system. Finally, the active head of the PR2 robot and its vision system have been used for vision-based towel folding in [95].

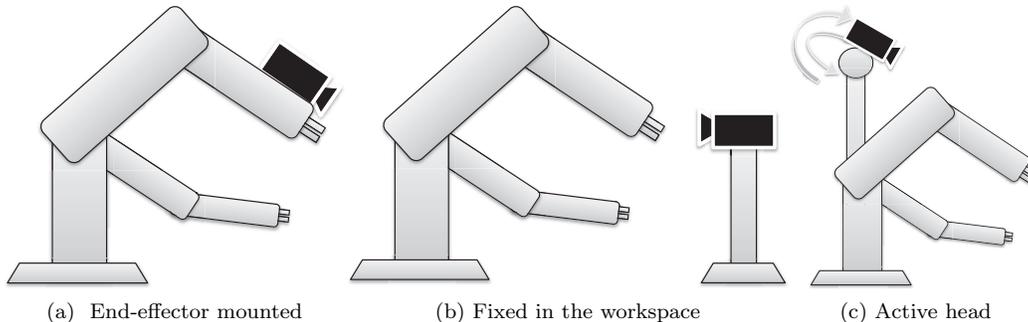


Figure 3: Types of camera configurations

Another, characterizing factor of vision systems is the kind of visual sensors they employ. The most commonly used systems use regular cameras in either *monocular*, *stereo* or *multicamera* setups, but combinations of these are also found. However, lately *other imaging devices*, often called RGB-D due to their ability to provide depth information along with typical color images, are finding their way into practical systems. Such sensors include the Microsoft Kinect and other structured light sensors, as well as time-of-flight sensors. An example of a real robot using the Kinect sensor is the anthropomorphic Cosero service robot, which uses its two arms to assist a human in carrying large objects [128].

2.4. Planning and Grasping

This section reviews methods used for motion, trajectory and manipulation planning in dual-arm systems. In principle, there is nothing special about having multiple arms, as it can be considered as a single robotic system with an increased number of degrees of freedom. However, the large number of DOFs that can arise, together with the possibilities for decoupling the motion of the different arms, provide sufficient reasons to study multi-arm planning independently, [110].

Early dual-arm robotic systems were teleoperated setups, where the operator directly controlled the robot and was responsible for planning the trajectory and the sequence of movements. With the appearance of more autonomous systems, the late 1980s saw an increasing interest in finding methods for dual-arm motion planning. In general, the methods described in those papers are extensions of single-arm methods, adapted to work with dual-arm systems.

Koga et al. analyze in [106] the problem of path-planning for two cooperating robot arms carrying a movable object between two given configurations, in a setup which includes obstacles. In the scenario described, the object to be moved is a single bar in a 2D plane. The arms can be moved independently, but both of them must hold the object at the same time in order to move it. In order to be able to avoid collisions between arm, object and obstacles, the arms may have to change their grasp of the object. The method proposed

extends the randomized potential field planning techniques introduced in [116] with the introduction of transit (where the arms move independently and the object remains static) and transfer (where the arms and the object form a closed kinematic chain) subpaths. The paper presents successful experimental results for a very simple version of the problem. In [107], the same authors consider the problem of several robotic manipulators moving an object in a 3D environment. It again breaks the problem into transit and transfer subpaths, which together form a manipulation path, and uses a Randomized Path Planner to generate a trajectory for the object from its initial to its goal configuration. The Randomized Path Planner algorithm [116] is modified to ensure that for each configuration along the path, not only is the configuration collision-free, but also the object can be grasped. The set of transfer paths is thus generated. Then, RPP is used again to generate the transit paths between the different transfer paths. The method is tested with 3 6-DOF arms.

Manipulability ellipsoids are defined as the mapping of the unit hypersphere at the origin of the joint velocity space into an ellipsoid in the Cartesian velocity space by a Jacobian transformation. These manipulability ellipsoids can be used to describe, at certain critical task points, the requirements for Cartesian motions and static forces. This allows the definition of a task-oriented manipulability measure (TOMM), which expresses the similarity between the desired and actual manipulability ellipsoids at the selected task points. In [117], this concept is extended to define a task-oriented dual-arm manipulability measure (TODAMM), which is the similarity between the desired manipulability ellipsoid and the intersection of two individual manipulability ellipsoids.

An approach to constrained motion planning for robotic systems with many degrees of freedom is introduced in [108]. It first establishes which are the conditions under which the manipulation constraints are holonomic. Then, it simplifies the problem, which in general includes non-holonomic constraints, so that all the constraints are holonomic. This is done by replacing an equality-constrained problem with a converging series of inequality-constrained problems, penalizing motions which do not satisfy the constraints. The result of each step of the series is used as the input for the next step, and each of the problems can be solved using a standard path planner.

In [109], a very specific problem arising in space applications of dual-arm systems is described. It studies the case of a free-floating dual-arm manipulator, where one of the arms is required to perform a certain task, while the other performs the necessary compensating motions to maintain the base inertially fixed. The main problem faced is to avoid the singularities. It uses an algorithm based position kinematics equations together with an iterative search procedure. The study shows the potential of the method, while finding configurations where the methods fail.

Lavalle in [110] proposes a formulation of the multiple-robot planning problem, and describes several strategies for decoupled planning:

- Prioritized planning assigns priorities to each of the robots in the system. Then, the path is calculated for the first robot without considering the rest.

Then, the method is repeated for each of the other robots, considering only the higher-priority robots for collision detection.

- Fixed-path coordination considers the case where each robot must follow a fixed path, and the goal is to find the timings that allow the robots to do so in a way that the robots don't collide with each other. Examples of this strategy are described in [111] and [112]
- Fixed-roadmap coordination extends fixed-path coordination to enable each robot to move over a roadmap or topological graph

Sezgin et al. [113, 114] introduce control configuration points (CCPs) for using redundancy for obstacle avoidance when using multiple planar robot manipulators. CCPs are selected along the kinematic structure of a manipulator, usually in the midpoint of links. These are used by Liu and Dai [118] to develop a method for planning the trajectory of multiple robotic fingers for carton-folding. They create a path connection based on CCPs and geometry guiding points (GGPs). The method generates the minimum number of fingers required for a certain manipulation of the carton, and integrates the carton motion into the trajectory of the robotic fingers.

Based on the RRT algorithm first introduced by Lavelle in [115], Vahrenkamp et al. introduce in [119] a method that combines into a single planner the three tasks needed for grasping an object: finding a feasible grasp, solving the inverse kinematics and finding a trajectory from some initial position to the grasping pose. A single probabilistic planner based on RRTs is used to search for a grasp that is both feasible and reachable, without the need of using precalculated grasping positions, which limit the possible grasps to a predefined set. The paper presents experimental results for bimanual grasping with the ARMAR-III robot. ARMAR-III has also been employed to demonstrate the application of probabilistically complete RRT-based motion planning algorithms for solving the problems of inverse kinematics, dual-arm manipulation motion planning and re-grasping tasks [167].

Also based on RRTs, the method in [120] introduces the concept of task maps, which represent the manifold of feasible grasps for an object. The task maps are learnt using the RRT algorithm. Then, choosing a grasp and choosing the path from the starting position of the robot to the position where the object is grasped is treated as a single problem, which leads to choosing a grasp which is easy to reach from the current position of the robot. The problem is solved using a gradient-based optimisation method.

As an alternative to roadmap and RRT-based planning, [121] introduces a new planning method based on a new approach for representing the state. This is done based on models of the robot and its environment, which aim at taking advantage of the structure found in robotic environments, and uses multiple variables to describe the current state. These variables may represent body parts, objects or constraints, but also provide abstractions for the current state. They assume that the state of the system is described by these random variables.

2.5. Learning

To achieve the goal of having robots that can work in unrestricted environments, it is necessary to equip them with the ability to adapt to the surroundings. Without the ability to learn, human designers must manually program all aspects of the behaviour of the robot, which is burdensome in unrestricted environments, where it is impossible to foresee every possible situation that the robot might encounter. Learning by demonstration has been used for some time to help with this learning process, by enabling robots to learn new actions by looking at a human performing them. Most of these methods have been traditionally aimed at a single manipulator. While it is possible, in some cases, to trivially extend these methods to two arms, just by repeating the process for each arm, there are some peculiarities of dual-arm manipulation which require some modifications to the frameworks [101] [168].

In [103], a framework for dual-arm programming by demonstration (PbD) is described. Bi-manual actions are classified based on the spatial relationship between the trajectory of hands performing coordinated actions. This leads to a threefold classification into coordinated symmetric, coordinated asymmetric and uncoordinated actions. This classification is made from the recorded demonstration, which is divided into one and two-hand fragments. Two-hand fragments are those where both hands are in the “grasped” state. Coordinated symmetric action is then detected by looking at closed kinematic chains. Several heuristics are then used to distinguish between asymmetric and uncoordinated action. For the execution of the actions, a synchronisation framework based on Petri nets is implemented.

The system in [104] uses Hidden Markov Models and Gaussian Mixture Regression to deal with the variability across several demonstrations and extract redundancies. Though it is not specifically dual-arm based, it has been used successfully to learn a bimanual dancing motion containing crossings, on an iCub robot.

In [105], a framework is presented that aims at teaching a bimanual coordination task to a robot. This method combines Dynamical Systems movement control with a Programming by Demonstration approach. The Programming by Demonstration method is a low-level one, which encapsulates the task at the trajectory level. Their main contribution is the use of a dynamical system approach which is used to encode coordinated motion patterns, which allows the use of a PbD approach to learn the movements of both arms simultaneously, and focusing on the relation between them.

A new framework for the learning of coordinated movements is presented in [102]. The system builds on the concept of learning control as learning a policy which maps the state to a control vector. It uses nonlinear dynamic systems as policy primitives. These primitives, called programmable pattern generators (PPG), implement a globally stable attractor with specifics determined by the values of a set of parameters. Different types of PPGs can represent different types of movement relationships. They implement their system on a 30-DOF Sarcos Humanoid Robot, using both arms to generate a regular rhythm on a couple of drums.

3. Where are we headed?

A future direction in robotic systems in general, and in dual arm manipulation in particular, will be the integration of elements from systems theory with tools from cognitive methodologies. These will involve the consideration of vision and learning capabilities in the actual feedback design. This seems necessary in advanced collaborative control tasks where the manipulators have incomplete knowledge of the environment, and might have been assigned their tasks independently. In particular, the lack of global knowledge about the environment and the final objective of the task in hand, along with the limitations in coordination due to sensing and communication constraints, suggest the integration of cognitive features in order to modify the individual agent controllers in an on-line data-driven manner. Future research will thus build, among others, towards the integration of the different research features addressed in this paper in order to address complex coordinated tasks.

Examining sensing and perception, this survey has shown a multitude of studies detailing different approaches, and several application papers where a specific sensor configuration is more or less given by technical capabilities or limitations of the chosen platform. In future work, it would be of interest to have a deeper discussion on the choice of sensors. Not only do we need to ask what sensors we should use, what modalities they should have, or where they should be placed, but we also need a discussion on what motivations that should be driving these choices. Is it meaningful to mimic the (proven successful) configuration of biological systems, such as humans? Should more advanced sensors be used to cover deficiencies in planning, modelling, and control, or should the latter be developed to cover deficiencies in sensors?

We could also turn the question around, and examine how developments in one subfield influences another. For instance, how would developments in sensing and perception affect modeling and control? What developments in sensing and perception would be necessary to support desired developments in planning?

How should we model and implement high level understanding of environments, objects and tasks. How can we support high-level reasoning about known entities? How do we extrapolate from existing knowledge in order to fill in gaps? How do we transfer domain-specific knowledge from humans to robots?

There are several possible routes towards answering these questions. We will need methods to analyze human behavior based on information from vision, haptics, or other sensors, along with reasoning systems to determine what aspects of a task are relevant, and need to be replicated by the robot. We will need strategies to map the human task performance to a dissimilar manipulator, identifying the goals of a task rather than the exact procedure. We will need efficient planning systems to achieve these goals.

With dual arm robots working in domestic and other human-centric environments, we also anticipate a substantial increase in applications for human-robot joint manipulation. Current state of the art typically employs different types of compliance, such as admittance or impedance control approaches, putting the

human in complete control. However, for robots to truly replace parts of the human work-force, we will need systems that can participate actively, as leaders as well as followers in collaborative tasks.

All of these issues need to be treated before robots can successfully replace humans in manipulation tasks in unstructured environments.

Acknowledgment

This work has been supported by the Swedish Research Council (VR), the Swedish Foundation for Strategic Research (SSF), and the European Union FP7 project RoboHow.Cog (FP7-ICT-288533).

- [1] R. C. Goertz, "Fundamentals of general-purpose remote manipulators," *Nucleonics*, vol. 10, no. 11, pp. 36–45, 1952.
- [2] T. Fletcher, "The undersea mobot," Nuclear Electronics Laboratory of Hughes Aircraft Company, Tech. Rep., Jan 1960.
- [3] R. Ambrose, H. Aldridge, R. Askew, R. Burrige, W. Bluethmann, M. Diftler, C. Lovchik, D. Magruder, and F. Rehnmark, "Robonaut: Nasa's space humanoid," *IEEE Intelligent Systems and their Applications*, vol. 15, no. 4, pp. 57–63, jul/aug 2000.
- [4] D. E. Whitney, "Historical perspective and state of the art in robot force control," *Int. J. Rob. Res.*, vol. 6, no. 1, pp. 3–14, 1987.
- [5] T. B. Sheridan, "Telerobotics," *Automatica*, vol. 25, no. 4, pp. 487–507, 1989.
- [6] R. Dorf and S. Nof, Eds., *Concise international encyclopedia of robotics*. New York, NY: John Wiley and Sons Inc, 1990.
- [7] D. Kragic and H. I. Christensen, "Survey on visual servoing for manipulation," Royal Institute of Technology (KTH), Stockholm, Sweden, Tech. Rep. ISRN KTH/NA/P-02/01-SE, CVAP259, 2002.
- [8] B. M. Jau, "Anthropomorphic exoskeleton dual arm/hand telerobot controller," in *IEEE/RSJ International Conference on Intelligent Robots and Systems*, 1988.
- [9] W.-K. Yoon, Y. Tsumaki, , and M. Uchiyama, "An experimental system for dual-arm robot teleoperation in space with concepts of virtual grip and ball," in *International Conference on Advanced Robotics*, Tokyo, Japan, 1999, pp. 225–230.
- [10] A. Kron and G. Schmidt, "Bimanual haptic telepresence technology employed to demining operations," in *Eurohaptics*, Munich, Germany, 2004, pp. 490–493.

- [11] M. Buss, M. Kuschel, K. Lee, A. Peer, B. Stanczyk, and U. Unterhinninghofen, “High fidelity telepresence systems: Design, control, and evaluation,” in *Joint International COE/HAM SFB-453 Workshop on Human Adaptive Mechatronics and High-Fidelity Telepresence*, Tokyo, Japan, 2006.
- [12] J. Taylor and D. Seward, “Control of a dualarm robotic manipulator,” *Nuclear Engineering International*, vol. 55, no. 673, pp. 24–26, 2010.
- [13] S. Lee and S. Kim, “A self-reconfigurable dual-arm system,” in *IEEE International Conference on Robotics and Automation*, Apr 1991.
- [14] R. Bloss, “Robotics innovations at the 2009 assembly technology expo,” *Industrial Robot: An International Journal*, vol. 37, no. 5, pp. 427–430, 2010.
- [15] A. Oyama, K. Konolige, S. Cousins, S. Chitta, K. Conley, and G. Bradski, “Come on in, our community is wide open for robotics research!” in *The 27th Annual conference of the Robotics Society of Japan*, 09/2009 2009.
- [16] F. Caccavale, P. Chiacchio, A. Marino, and L. Villani, “Six-dof impedance control of dual-arm cooperative manipulators,” *IEEE/ASME Transactions on Mechatronics*, vol. 13, no. 5, pp. 576 –586, oct. 2008.
- [17] R. Ozawa, S. Arimoto, S. Nakamura, and J.-H. Bae, “Control of an object with parallel surfaces by a pair of finger robots without object sensing,” *IEEE Transactions on Robotics*, vol. 21, no. 5, pp. 965 – 976, oct. 2005.
- [18] A. Edsinger and C. C. Kemp, *Lecture Notes in Control and Information Sciences*. Heidelberg: Springer, Feb 2008, vol. 370, ch. Two Arms are Better Than One: A Behavior-Based Control System for Assistive Bimanual Manipulation, Recent Progress in Robotics: Viable Robotic Service to Human, pp. 345–355.
- [19] R. L. A. Shauri and K. Nonami, “Assembly manipulation of small objects by dual-arm manipulator,” *Assembly Automation*, vol. 31, no. 3, pp. 263–274, 2011.
- [20] P. Ögren, C. Smith, Y. Karayiannidis, and D. Kragic, “A multi objective control approach to online dual arm manipulation,” in *International IFAC Symposium on Robot Control, SyRoCo*, Dubrovnik, Croatia, Sep 2012.
- [21] L. Goncalves, R. Grupen, A. Oliveira, D. Wheeler, and A. Fagg, “Attention and categorization: Basis for cognition in a humanoid robot,” *IEEE Intelligent Systems and Applications*, 2000.
- [22] A. Albers, S. Brudniok, J. Ottnad, C. Sauter, and K. Sedchaicham, “Upper body of a new humanoid robot - the design of armar iii,” in *2006 6th IEEE-RAS International Conference on Humanoid Robots*, Dec 2006, pp. 308–313.

- [23] C. Kemp, A. Edsinger, and E. Torres-Jara, “Challenges for robot manipulation in human environments [Grand Challenges of Robotics],” *IEEE Robotics Automation Magazine*, vol. 14, no. 1, pp. 20–29, march 2007.
- [24] M. Fuchs, C. Borst, P. Giordano, A. Baumann, E. Kraemer, J. Langwald, R. Gruber, N. Seitz, G. Plank, K. Kunze, R. Burger, F. Schmidt, T. Wimboeck, and G. Hirzinger, “Rollin’ justin - design considerations and realization of a mobile platform for a humanoid upper body,” in *IEEE International Conference on Robotics and Automation*, may 2009, pp. 4131–4137.
- [25] T. Wimböck and C. Ott, “Dual-arm manipulation,” in *Towards Service Robots for Everyday Environments*, ser. Springer Tracts in Advanced Robotics, E. Prassler, M. Zollner, R. Bischoff, W. Burgard, R. Haschke, M. Hagele, G. Lawitzky, B. Nebel, P. Ploger, and U. Reiser, Eds. Springer Berlin / Heidelberg, 2012, vol. 76, pp. 353–366.
- [26] A. Edsinger-Gonzales and J. Weber, “Domo: a force sensing humanoid robot for manipulation research,” in *IEEE International Conference on Humanoid Robots*, vol. 1, nov. 2004, pp. 273–291.
- [27] H. Nakai, M. Yamataka, T. Kuga, S. Kuge, H. Tadano, H. Nakanishi, M. Furukawa, and H. Ohtsuka, “Development of dual-arm robot with multi-fingered hands,” in *IEEE International Symposium on Robot and Human Interactive Communication*, Hatfield, UK, 2006, pp. 208–213.
- [28] C. Park, K. Park, D. I. Park, and J.-H. Kyung, “Dual arm robot manipulator and its easy teaching system,” in *IEEE International Symposium on Assembly and Manufacturing*, nov. 2009, pp. 242–247.
- [29] H. Tanabe, T. Fujiwara, Y. Miyano, T. Shimada, M. Hirai, and M. Nakahata, “Development of the dual-arm robot for built with our intrinsic safety technology and optimal power output for production of small-scale appliance,” Kawada Industries, Inc., Tech. Rep., Jan 2010.
- [30] J. Krüger, G. Schreck, and D. Surdilovic, “Dual arm robot for flexible and cooperative assembly,” *CIRP Annals - Manufacturing Technology*, vol. 60, no. 1, pp. 5–8, 2011.
- [31] M. Zivanovic and M. Vukobratovic, *Multi-Arm Cooperating Robots – Dynamics and Control*. Springer, 2006.
- [32] F. Caccavale and M. Uchiyama, *Springer Handbook of Robotics*. Springer, 2008, ch. Cooperative Manipulators, pp. 701–718.
- [33] G. Grunwald, C. Borst, and J. Zöllner, “Benchmarking dexterous dual-arm/hand robotic manipulation,” in *IEEE/RSJ International Conference on Intelligent Robots and Systems, Workshop on Performance Evaluation and Benchmarking*, Nice, France, 2008.

- [34] D. Surdilovic, Y. Yakut, T.-M. Nguyen, X. Pham, A. Vick, and R. Martin, “Compliance control with dual-arm humanoid robots: Design, planning, and programming,” in *IEEE International Conference on Humanoid Robots*, 2010, pp. 275–281.
- [35] M. Bell, Ed., *Flexible Object Manipulation*. Dartmouth College: PhD thesis, 2010.
- [36] Y.-H. Liu, S. Arimoto, V. Parra-Vega, and K. Kitagaki, “Adaptive distributed cooperation controller for multiple manipulators,” in *IEEE/RSJ International Conference on Intelligent Robots and Systems, workshop on Human Robot Interaction and Cooperative Robots*, 1995, pp. 489–494 vol.1.
- [37] J. Gudiño-Lau and M. A. Arteaga, “Dynamic model and simulation of cooperative robots: a case study,” *Robotica*, vol. 23, no. 05, pp. 615–624, 2005.
- [38] X. Yun and V. Kumar, “An approach to simultaneous control of trajectory and interaction forces in dual-arm configurations,” *IEEE Transactions on Robotics and Automation*, vol. 7, no. 5, pp. 618–625, oct 1991.
- [39] D. Williams and O. Khatib, “The virtual linkage: A model for internal forces in multi-grasp manipulation,” in *IEEE International Conference on Robotics and Automation*. IEEE, 1993, pp. 1025–1030.
- [40] P. Chiacchio, S. Chiaverini, L. Sciavicco, and B. Siciliano, “Global task space manipulability ellipsoids for multiple-arm systems,” *IEEE Transactions on Robotics and Automation*, vol. 7, no. 5, pp. 678–685, oct 1991.
- [41] H. G. Tanner, K. J. Kyriakopoulos, and N. J. Krikelis, “Modeling of multiple mobile manipulators handling a common deformable object,” *Journal of Robotic Systems*, vol. 15, no. 11, pp. 599–623, 1998.
- [42] A. K. Swain and A. S. Morris, “Dynamic control of multi-arm co-operating manipulator systems,” *Robotica*, vol. 22, pp. 271–283, June 2004.
- [43] D. Prattichizzo and J. C. Trinkl, *Springer Handbook of Robotics*. Springer, 2008, ch. Grasping, pp. 671–700.
- [44] N. Sarkar, X. Yun, and V. Kumar, “Dynamic control of 3-d rolling contacts in two-arm manipulation,” *IEEE Transactions on Robotics and Automation*, vol. 13, no. 3, pp. 364–376, jun 1997.
- [45] T. Yoshikawa, “Multifingered robot hands: Control for grasping and manipulation,” *Annual Reviews in Control*, vol. 34, no. 2, pp. 199–208, 2010.
- [46] S. Arimoto, “A differential-geometric approach for 2d and 3d object grasping and manipulation,” *Annual Reviews in Control*, vol. 31, no. 2, pp. 189–209, 2007.

- [47] A. Kawamura, K. Tahara, R. Kurazume, and T. Hasegawa, “Simple orientation control of an object by regrasping using a dual-arm manipulator with multi-fingered hands,” in *International Conference on Advanced Robotics*, june 2009, pp. 1–6.
- [48] Y. Li and I. Kao, “A review of modeling of soft-contact fingers and stiffness control for dextrous manipulation in robotics,” in *IEEE International Conference on Robotics and Automation*, 2001, pp. 3055–3060 vol.3.
- [49] T. Yoshikawa, “Virtual truss model for characterization of internal forces for multiple finger grasps,” *IEEE Transactions on Robotics and Automation*, vol. 15, no. 5, pp. 941–947, oct 1999.
- [50] T. Yoshikawa, “Passive and active closures by constraining mechanisms,” in *IEEE International Conference on Robotics and Automation*, vol. 2, apr 1996, pp. 1477–1484 vol.2.
- [51] L. Han, J. Trinkle, and Z. Li, “Grasp analysis as linear matrix inequality problems,” *IEEE Transactions on Robotics and Automation*, vol. 16, no. 6, pp. 663–674, Dec 2000.
- [52] A. Bicchi, “On the closure properties of robotic grasping,” *The International Journal of Robotics Research*, vol. 14, no. 4, pp. 319–334, 1995.
- [53] N. S. Pollard, “Closure and quality equivalence for efficient synthesis of grasps from examples,” *The International Journal of Robotics Research*, vol. 23, no. 6, pp. 595–613, 2004.
- [54] Y. Zheng and W.-H. Qian, “Coping with the grasping uncertainties in force-closure analysis,” *The International Journal of Robotics Research*, vol. 24, pp. 311–327, April 2005.
- [55] M. Strandberg and B. Wahlberg, “A method for grasp evaluation based on disturbance force rejection,” *IEEE Transactions on Robotics*, vol. 22, no. 3, pp. 461–469, june 2006.
- [56] T. Watanabe and T. Yoshikawa, “Grasping optimization using a required external force set,” *IEEE Transactions on Automation Science and Engineering*, vol. 4, no. 1, pp. 52–66, jan. 2007.
- [57] M. T. Ciocarlie and P. K. Allen, “Hand posture subspaces for dexterous robotic grasping,” *The International Journal of Robotics Research*, vol. 28, no. 7, pp. 851–867, 2009.
- [58] M. Gabbicini and A. Bicchi, “On the role of hand synergies in the optimal choice of grasping forces,” in *Robotics: Science and Systems*, jun 2010.
- [59] A. Bicchi, C. Melchiorri, and D. Balluchi, “On the mobility and manipulability of general multiple limb robots,” *IEEE Transactions on Robotics and Automation*, vol. 11, no. 2, pp. 215–228, apr 1995.

- [60] H. Wakamatsu, S. Hirai, and K. Iwata, “Static analysis of deformable object grasping based on bounded force closure,” in *IEEE International Conference on Robotics and Automation*, 1996, pp. 3324–3329 vol.4.
- [61] T. Watanabe, “Softness effects on manipulability and grasp stability,” in *IEEE/RSJ International Conference on Intelligent Robots and Systems*, sept. 2011, pp. 1398–1404.
- [62] F. Ficuciello, R. Carloni, L. Visser, and S. Stramigioli, “Port-hamiltonian modeling for soft-finger manipulation,” in *IEEE/RSJ International Conference on Intelligent Robots and Systems*, oct. 2010, pp. 4281–4286.
- [63] P. Song, P. Kraus, V. Kumar, and P. Dupont, “Analysis of rigid body dynamic models for simulation of systems with frictional contacts,” *Journal of Applied Mechanics*, vol. 68, pp. 118–128, 2000.
- [64] Z. Dougeri and A. Golfakis, “Nonlinear manipulation control of a compliant object by dual fingers,” *Journal of Dynamic Systems Measurement and Control-Transactions of The ASME*, vol. 128, no. 3, 2006.
- [65] N. Xi, T.-J. Tarn, and A. Bejczy, “Intelligent planning and control for multirobot coordination: An event-based approach,” *IEEE Transactions on Robotics and Automation*, vol. 12, no. 3, pp. 439–452, jun 1996.
- [66] P. Hsu, “Coordinated control of multiple manipulator systems,” *IEEE Transactions on Robotics and Automation*, vol. 9, no. 4, pp. 400–410, aug 1993.
- [67] T. Yoshikawa, “Control algorithm for grasping and manipulation by multifingered robot hands using virtual truss model representation of internal force,” in *IEEE International Conference on Robotics and Automation*, 2000, pp. 369–376 vol.1.
- [68] T. Watanabe, K. Harada, Z. Jiang, and T. Yoshikawa, “Object manipulation under hybrid active/passive closure,” in *IEEE International Conference on Robotics and Automation*, april 2005, pp. 1013–1020.
- [69] J. Gudiño Lau, M. Arteaga, L. Munoz, and V. Parra-Vega, “On the control of cooperative robots without velocity measurements,” *IEEE Transactions on Control Systems Technology*, vol. 12, no. 4, pp. 600–608, july 2004.
- [70] D. Navarro-Alarcon, V. Parra-Vega, S. Vite-Medecigo, and E. Olguin-Diaz, “Dexterous cooperative manipulation with redundant robot arms,” in *Progress in Pattern Recognition, Image Analysis, Computer Vision, and Applications*, ser. Lecture Notes in Computer Science, E. Bayro-Corrochano and J.-O. Eklundh, Eds. Springer Berlin / Heidelberg, 2009, vol. 5856, pp. 910–917.

- [71] M. Yamano, J.-S. Kim, A. Konno, and M. Uchiyama, “Cooperative control of a 3d dual-flexible-arm robot,” *Journal of Intelligent and Robotic Systems*, vol. 39, pp. 1–15, 2004.
- [72] R. Tinos, M. Terra, and J. Ishihara, “Motion and force control of cooperative robotic manipulators with passive joints,” *IEEE Transactions on Control Systems Technology*, vol. 14, no. 4, pp. 725 – 734, july 2006.
- [73] W. Gueaieb, F. Karray, and S. Al-Sharhan, “A robust hybrid intelligent position/force control scheme for cooperative manipulators,” *IEEE/ASME Transactions on Mechatronics*, vol. 12, no. 2, pp. 109 –125, april 2007.
- [74] Y. Zhao and C. C. Cheah, “Neural network control of multifingered robot hands using visual feedback,” *IEEE Transactions on Neural Networks*, vol. 20, no. 5, pp. 758 –767, may 2009.
- [75] A. Nakashima, T. Shibata, and Y. Hayakawa, “Control of grasp and manipulation by soft fingers with 3-dimensional deformation,” *SICE Journal of Control, Measurement, and System Integration*, vol. 2, no. 2, pp. 78 – 87, 2009.
- [76] F. Caccavale, P. Chiacchio, and S. Chiaverini, “Stability analysis of a joint space control law for a two-manipulator system,” *IEEE Transactions on Automatic Control*, vol. 44, no. 1, pp. 85 –88, jan. 1999.
- [77] F. Caccavale, P. Chiacchio, and S. Chiaverini, “Task-space regulation of cooperative manipulators,” *Automatica*, vol. 36, no. 6, pp. 879 – 887, 2000.
- [78] S. Schneider and R. Cannon, “Object impedance control for cooperative manipulation: theory and experimental results,” *IEEE Transactions on Robotics and Automation*, vol. 8, no. 3, pp. 383 –394, jun 1992.
- [79] R. Bonitz and T. Hsia, “Internal force-based impedance control for cooperating manipulators,” *IEEE Transactions on Robotics and Automation*, vol. 12, no. 1, pp. 78 –89, feb 1996.
- [80] R. Bonitz and T. Hsia, “Robust dual-arm manipulation of rigid objects via palm grasping - theory and experiments,” in *IEEE International Conference on Robotics and Automation*, 1996, pp. 22–28.
- [81] V. Lippiello, F. Ruggiero, and L. Villani, “Inverse kinematics for object manipulation with redundant multi-fingered robotic hands,” 2009.
- [82] J.-H. Bae, S. Arimoto, R. Ozawa, M. Sekimoto, and M. Yoshida, “A unified control scheme for a whole robotic arm-fingers system in grasping and manipulation,” in *IEEE International Conference on Robotics and Automation*, may 2006, pp. 2131–2136.

- [83] S. Arimoto, Z. Doulgeri, P. T. A. Nguyen, and J. Fasoulas, “Stable pinching by a pair of robot fingers with soft tips under the effect of gravity,” *Robotica*, vol. 20, no. 03, pp. 241–249, 2002.
- [84] Z. Doulgeri and J. Fasoulas, “Grasping control of rolling manipulations with deformable fingertips,” *IEEE/ASME Transactions on Mechatronics*, vol. 8, no. 2, pp. 283–286, june 2003.
- [85] Y. Kume, Y. Hirata, and K. Kosuge, “Coordinated motion control of multiple mobile manipulators handling a single object without using force/torque sensors,” in *IEEE/RSJ International Conference on Intelligent Robots and Systems*, 2007, pp. 4077–4082.
- [86] D. Sun and J. Mills, “Adaptive synchronized control for coordination of multirobot assembly tasks,” *IEEE Transactions on Robotics and Automation*, vol. 18, no. 4, pp. 498–510, aug 2002.
- [87] K.-Y. Lian, C.-S. Chiu, and P. Liu, “Semi-decentralized adaptive fuzzy control for cooperative multirobot systems with h infin; motion/internal force tracking performance,” *IEEE Transactions on Systems, Man, and Cybernetics, Part B: Cybernetics,*, vol. 32, no. 3, pp. 269–280, jun 2002.
- [88] B. Adorno, P. Fraitse, and S. Druon, “Dual position control strategies using the cooperative dual task-space framework,” in *IEEE/RSJ International Conference on Intelligent Robots and Systems*, oct. 2010, pp. 3955–3960.
- [89] H. Tanner, S. Loizou, and K. Kyriakopoulos, “Nonholonomic navigation and control of cooperating mobile manipulators,” *IEEE Transactions on Robotics and Automation*, vol. 19, no. 1, pp. 53–64, feb 2003.
- [90] R. Kelly, R. Carelli, O. Nasisi, B. Kuchen, and F. Reyes, “Stable visual servoing of camera-in-hand robotic systems,” *IEEE/ASME Transactions on Mechatronics*, vol. 5, no. 1, pp. 39–48, mar 2000.
- [91] P. Dauchez, P. Fraitse, and F. Pierrot, “A vision/position/force control approach for performing assembly tasks with a humanoid robot,” in *IEEE International Conference on Humanoid Robots*, dec. 2005, pp. 277–282.
- [92] V. Lippiello, B. Siciliano, and L. Villani, “An experimental setup for visual servoing applications on an industrial robotic cell,” in *IEEE/ASME International Conference on Advanced Intelligent Mechatronics*, july 2005, pp. 1431–1436.
- [93] V. Lippiello, L. Villani, and B. Siciliano, “An open architecture for sensory feedback control of a dual-arm industrial robotic cell,” *Industrial Robot: An International Journal*, vol. 34, pp. 46–53, 2007.

- [94] E. Zereik, A. Sorbara, G. Casalino, and F. Didot, “Autonomous dual-arm mobile manipulator crew assistant for surface operations: Force/vision-guided grasping,” in *International Conference on Recent Advances in Space Technologies*, june 2009, pp. 710–715.
- [95] J. Maitin-Shepard, M. Cusumano-Towner, J. Lei, and P. Abbeel, “Cloth grasp point detection based on multiple-view geometric cues with application to robotic towel folding,” in *IEEE International Conference on Robotics and Automation*, may 2010, pp. 2308–2315.
- [96] W.-C. Chang and V.-T. Nguyen, “Control of cooperative dual-arm mobile robots in a vision-based intelligent space,” in *International Conference on Climbing and Walking Robots and the Support Technologies for Mobile Machines*, 2010, pp. 296–304.
- [97] J. Zhou and Y. Yu, “Coordination control of dual-arm modular robot based on position feedback using Optotrak3020,” *Industrial Robot: An International Journal*, vol. 38, no. 2, pp. 172–185, 2011.
- [98] K. Huebner, K. Welke, M. Przybylski, N. Vahrenkamp, T. Asfour, D. Kragic, and R. Dillmann, “Grasping known objects with humanoid robots: A box-based approach,” in *International Conference on Advanced Robotics*, june 2009, pp. 1–6.
- [99] N. Vahrenkamp, C. Boge, K. Welke, T. Asfour, J. Walter, and R. Dillmann, “Visual servoing for dual arm motions on a humanoid robot,” in *IEEE International Conference on Humanoid Robots*, 2009, pp. 208–214.
- [100] K. S. M. Sahari, S. H., K. Y., and M. Hikizu, “Edge tracing manipulation of clothes based on different gripper types,” *Journal of Computer Science*, vol. 6, no. 8, pp. 872–878, 2010.
- [101] R. Platt, R. Burrige, M. Diftler, J. Graf, M. Goza, E. Huber, and O. Brock, “Humanoid mobile manipulation using controller refinement,” in *IEEE International Conference on Humanoid Robots*, 2006, pp. 94–101.
- [102] S. Schaal, S. Kotosaka, and D. Sternad, “Nonlinear dynamical systems as movement primitives,” in *IEEE International Conference on Humanoid Robotics*, 2000.
- [103] R. Zollner, T. Asfour, and R. Dillmann, “Programming by demonstration: dual-arm manipulation tasks for humanoid robots,” in *IEEE/RSJ International Conference on Intelligent Robots and Systems*, vol. 1, sept.-2 oct. 2004, pp. 479 – 484 vol.1.
- [104] S. Calinon, F. D’halluin, E. Sauser, D. Caldwell, and A. Billard, “Learning and reproduction of gestures by imitation,” *IEEE Robotics Automation Magazine*, vol. 17, no. 2, pp. 44 –54, june 2010.

- [105] E. Gribovskaya and A. Billard, “Combining dynamical systems control and programming by demonstration for teaching discrete bimanual coordination tasks to a humanoid robot,” in *IEEE/ACM International Conference on Human-Robot Interaction*, 2008.
- [106] Y. Koga and J.-C. Latombe, “Experiments in dual-arm manipulation planning,” in *IEEE International Conference on Robotics and Automation*, may 1992, pp. 2238 –2245 vol.3.
- [107] Y. Koga and J.-C. Latombe, “On multi-arm manipulation planning,” in *IEEE International Conference on Robotics and Automation*, may 1994, pp. 945 –952 vol.2.
- [108] J. Barraquand and P. Ferbach, “A penalty function method for constrained motion planning,” in *IEEE International Conference on Robotics and Automation*, may 1994, pp. 1235 –1242 vol.2.
- [109] S. K. Agrawal and S. Shirumalla, “Planning motions of a dual-arm free-floating manipulator keeping the base inertially fixed,” *Mechanism and Machine Theory*, vol. 30, no. 1, pp. 59 – 70, 1995.
- [110] S. M. LaValle, “Planning algorithms,” 2004.
- [111] Z. Bien and J. Lee, “A minimum-time trajectory planning method for two robots,” *IEEE Transactions on Robotics and Automation*, vol. 8, no. 3, pp. 414 –418, jun 1992.
- [112] K. Shin and Q. Zheng, “Minimum-time collision-free trajectory planning for dual-robot systems,” *IEEE Transactions on Robotics and Automation*, vol. 8, no. 5, pp. 641 –644, oct 1992.
- [113] U. Sezgin, L. D. Seneviratne, and S. W. E. Earles, “Redundancy utilization for obstacle avoidance of planar robot manipulators,” in *Proceedings of the Institution of Mechanical Engineers*, 1997.
- [114] U. Sezgin, L. D. Seneviratne, and S. W. E. Earles, “Collision avoidance in multiple-redundant manipulators,” *International Journal of Robotic Research*, vol. 16, pp. 714–724, October 1997.
- [115] S. M. LaValle, “Rapidly-exploring random trees: A new tool for path planning,” Computer Science Dept., Iowa State University, Tech. Rep. TR 98-11, oct. October 1998.
- [116] J. Barraquand and J.-C. Latombe, “Robot Motion Planning: A Distributed Representation Approach,” Stanford University, Tech. Rep., May 1989.
- [117] S. Lee, “Dual redundant arm configuration optimization with task-oriented dual arm manipulability,” *IEEE Transactions on Robotics and Automation*, vol. 5, no. 1, pp. 78 –97, feb 1989.

- [118] H. Liu and J. Dai, “Manipulation analysis of carton-folding task by using ggps and ccps,” in *IEEE International Symposium on Intelligent Control*, 2002, pp. 637 – 641.
- [119] N. Vahrenkamp, M. Do, T. Asfour, and R. Dillmann, “Integrated grasp and motion planning,” in *IEEE International Conference on Robotics and Automation*, may 2010, pp. 2883 –2888.
- [120] M. Gienger, M. Toussaint, and C. Goerick, “Task maps in humanoid robot manipulation,” in *IEEE/RSJ International Conference on Intelligent Robots and Systems*, sept. 2008, pp. 2758 –2764.
- [121] M. Toussaint and C. Goerick, “Probabilistic inference for structured planning in robotics,” in *IEEE/RSJ International Conference on Intelligent Robots and Systems*, 29 2007-nov. 2 2007, pp. 3068 –3073.
- [122] J. van den Berg, S. Miller, K. Goldberg, and P. Abbeel, “Gravity-based robotic cloth folding,” in *Algorithmic Foundations of Robotics IX*, ser. Springer Tracts in Advanced Robotics, D. Hsu, V. Isler, J.-C. Latombe, and M. Lin, Eds. Springer Berlin / Heidelberg, 2011, vol. 68, pp. 409–424.
- [123] M. Beetz, U. Klank, A. Maldonado, D. Pangercic, and T. Ruhr, “Robotic roommates making pancakes — look into perception-manipulation loop,” in *IEEE International Conference on Robotics and Automation*, 2011.
- [124] K. Salleh, H. Seki, Y. Kamiya, and M. Hikizu, “Inchworm robot grippers in clothes manipulation - optimizing the tracing algorithm,” in *International Conference on Intelligent and Advanced Systems*, 2007, pp. 1051–1055.
- [125] T. Asfour, K. Regenstein, P. Azad, J. Schroder, A. Bierbaum, N. Vahrenkamp, and R. Dillmann, “ARMAR-III: An integrated humanoid platform for sensory-motor control,” in *IEEE International Conference on Humanoid Robots*, dec. 2006, pp. 169 –175.
- [126] H. Iwata and S. Sugano, “Design of human symbiotic robot twenty-one,” in *IEEE International Conference on Robotics and Automation*, 2009, pp. 3294–3300.
- [127] K. Hamajima and M. Kakikura, “Planning strategy for task of unfolding clothes,” *Robotics and Autonomous Systems*, vol. 32, pp. 145–152, 2000.
- [128] J. Stückler and S. S. Behnke, “Following human guidance to cooperatively carry a large object,” in *IEEE International Conference on Humanoid Robots*, oct 2011.
- [129] S. Hata, T. Hiroyasu, J. Hayashi, H. Hojoh, and T. Hamada, “Robot system for cloth handling,” in *34th Annual Conference of IEEE Industrial Electronics*, nov. 2008, pp. 3449–3454.

- [130] J. Takamatsu, K. Ogawara, H. Kimura, and K. Ikeuchi, “Recognizing assembly tasks through human demonstration,” *International Journal of Robotics Research*, vol. 26, pp. 641–659, July 2007.
- [131] Y. F. Zheng and M. Z. Chen, “Trajectory planning for two manipulators to deform flexible beams,” *Robotics and Autonomous Systems*, vol. 12, no. 1-2, pp. 55 – 67, 1994, special Issue Parallel and Multi-Arm Robotic Systems.
- [132] Y. Yamada, S. Nagamatsu, and Y. Sato, “Development of multi-arm robots for automobile assembly,” in *IEEE International Conference on Robotics and Automation*, vol. 3, may 1995, pp. 2224 –2229 vol.3.
- [133] H. Liu and J. Dai, “An approach to carton-folding trajectory planning using dual robotic fingers,” *Robotics and Autonomous Systems*, vol. 42, no. 1, pp. 47 – 63, 2003.
- [134] R. Suda, K. Kosuge, and H. Kakuya, “Object-impedance-based cooperative handling of object by mobile robot helper and human using visual and force information,” in *IEEE/ASME International Conference on Advanced Intelligent Mechatronics*, vol. 1, july 2003, pp. 592–597.
- [135] S. Kock, T. Vittor, B. Matthias, H. Jerregard, M. Kallman, I. Lundberg, R. Mellander, and M. Hedelind, “Robot concept for scalable, flexible assembly automation: A technology study on a harmless dual-armed robot,” in *IEEE International Symposium on Assembly and Manufacturing*, may 2011, pp. 1–5.
- [136] J. R. Wilson, “Robonaut: The next generation,” *Aerospace America*, vol. 48, no. 8, pp. 26–31, Sep 2010.
- [137] T. Haidegger, “Advanced robotic arms in space,” in *55th International Astronautical Congress*, 2004.
- [138] P. Deegan, B. Thibodeau, and R. Grupen, “Designing a self-stabilizing robot for dynamic mobile manipulation,” in *Robotics: Science and Systems - Workshop on Manipulation for Human Environments*, Philadelphia, Pennsylvania, Aug 2006.
- [139] C. Ott, O. Eiberger, W. Friedl, B. Bauml, U. Hillenbrand, C. Borst, A. Albu-Schäffer, B. Brunner, H. Hirschmüller, S. Kielhöfer, R. Konietschke, M. Suppa, T. Wimböck, F. Zacharias, and G. Hirzinger, “A humanoid two-arm system for dexterous manipulation,” in *6th IEEE-RAS International Conference on Humanoid Robots*, dec. 2006, pp. 276–283.
- [140] J. Lemburg, J. de Gea Fernandez, M. Eich, D. Mronga, P. Kampmann, A. Vogt, A. Aggarwal, Y. Shi, and F. Kirchner, “AILA - design of an autonomous mobile dual-arm robot,” in *IEEE International Conference on Robotics and Automation*, Shanghai, China, 2011, pp. 5147–5153.

- [141] “<http://ias.cs.tum.edu/research-areas/robots/tum-robot>,” Retrieved on July 22, 2011.
- [142] T. Chen and C. Kemp, “A direct physical interface for navigation and positioning of a robotic nursing assistant,” *Advanced Robotics*, vol. 25, no. 5, pp. 605–627, 2011.
- [143] M. Hirose and T. Takenaka, “Development of humanoid robot asimo,” *Honda R&D Tech Rev*, vol. 13, no. 1, pp. 1–6, 2001.
- [144] K. Kaneko, F. Kanehiro, S. Kajita, K. Yokoyama, K. Akachi, T. Kawasaki, S. Ota, and T. Isozumi, “Design of prototype humanoid robotics platform for hrp,” in *IEEE/RSJ International Conference on Intelligent Robots and Systems*, vol. 3, 2002, pp. 2431 – 2436 vol.3.
- [145] J. K. Lee, B. S. Park, H. J. Lee, K. Kim, and H. D. Kim, “Development of a control system for master-slave operation,” in *International Conference on Control, Automation and Systems*, Oct 2010.
- [146] T. Mukai, S. Hirano, H. Nakashima, Y. Kato, Y. Sakaida, S. Guo, and S. Hosoe, “Development of a nursing-care assistant robot riba that can lift a human in its arms,” in *IEEE/RSJ International Conference on Intelligent Robots and Systems*, oct. 2010, pp. 5996 –6001.
- [147] S. Han, J. Choi, K. Son, M. Lee, J. Lee, and M. Lee, “A study on feature-based visual servoing control of eight axes-dual arm robot by utilizing redundant feature,” in *IEEE International Conference on Robotics and Automation*, vol. 3, 2001, pp. 2622–2627.
- [148] Y. Kim, S. Fan, S. Han, and H. Go, “Image-based visual feedback control of a dual-arm robot,” in *IEEE International Symposium on Industrial Electronics*, vol. 3, 2001, pp. 1603–1608.
- [149] W.-S. Lee, S.-B. Oh, D.-J. Cha, J.-B. Lee, S.-H. Han, and D.-J. Park, “A study on robust feedback control for dual-arm robot system,” in *International Conference on Control, Automation and Systems*, oct. 2007, pp. 2299–2303.
- [150] H. Li, Q. Huang, Q. Dong, C. Li, Y. He, Z. Jiang, Y. Li, P. Lv, L. Xie, X. Chen, and K. Li, “Design for a dual-arm space robot,” in *CISM Symposium on Robot Design, Dynamics and Control*, ser. CISM International Centre for Mechanical Sciences, G. Maier, F. G. Rammerstorfer, J. Salençon, B. Schrefler, P. Serafini, V. Parenti Castelli, and W. Schiehlen, Eds. Springer Vienna, 2010, vol. 524, pp. 191–198.
- [151] R. M. Murray, S. S. Sastry, and L. Zexiang, *A Mathematical Introduction to Robotic Manipulation*, 1st ed. Boca Raton, FL, USA: CRC Press, Inc., 1994.

- [152] P. Chiacchio and S. Chiaverini, *Complex Robotic Systems*, 1st ed. Secaucus, NJ, USA: Springer-Verlag New York, Inc., 1998.
- [153] A. Bicchi, “Hands for dexterous manipulation and robust grasping: a difficult road toward simplicity,” *IEEE Transactions on Robotics and Automation*, vol. 16, no. 6, pp. 652–662, 2000.
- [154] A. Bicchi and V. Kumar, “Robotic grasping and manipulation,” in *Lecture Notes in Control and Information Sciences*, S. Nicosia, B. Siciliano, A. Bicchi, and P. Valigi, Eds., vol. 270. Springer Berlin Heidelberg, 2001, pp. 55–74.
- [155] M. Mason and J. Salisbury, Eds., *Robot hands and the mechanics of manipulation*. Cambridge, MA, USA: MIT Press, 1985.
- [156] A. Okamura, N. Smaby, and M. Cutkosky, “An overview of dexterous manipulation,” in *IEEE International Conference on Robotics and Automation*, 2000, pp. 255–262 vol.1.
- [157] A. Bicchi and V. Kumar, “Robotic grasping and contact: a review,” in *IEEE International Conference on Robotics and Automation*, 2000, pp. 348–353 vol.1.
- [158] T. Wimböck, C. Ott, A. Albu-Schäffer, and G. Hirzinger, “Comparison of object-level grasp controllers for dynamic dexterous manipulation,” *The International Journal of Robotics Research*, vol. 31, no. 1, pp. 3–23, 2012.
- [159] K. Shimoga, “Robot grasp synthesis algorithms: A survey,” *The International Journal of Robotics Research*, vol. 15, no. 3, pp. 230–266, 1996.
- [160] S. F. F. Gibson and B. Mirtich, “A survey of deformable modeling in computer graphics,” Tech. Rep., 1997.
- [161] D. J. Balkcom, “Robotic origami folding,” *The International Journal of Robotics Research*, vol. 27, no. 5, pp. 613–627, 2008.
- [162] L. Lu and S. Akella, “Folding cartons with fixtures: a motion planning approach,” *IEEE Transactions on Robotics and Automation*, vol. 16, no. 4, pp. 346–356, Aug. 2000.
- [163] W.-H. Zhu, “On adaptive synchronization control of coordinated multi-robots with flexible/rigid constraints,” *IEEE Transactions on Robotics*, vol. 21, no. 3, pp. 520 – 525, june 2005.
- [164] S. Hutchinson, G. D. Hager, and P. I. Corke, “A tutorial on visual servo control,” *IEEE Transactions on Robotics and Automation*, vol. 12, no. 5, pp. 651–670, 1996.
- [165] F. Chaumette and S. Hutchinson, “Visual servo control. I. Basic approaches,” *IEEE Robotics Automation Magazine*, vol. 13, no. 4, pp. 82–90, 2006.

- [166] F. Chaumette and S. Hutchinson, “Visual servo control. II. Advanced approaches,” *IEEE Robotics Automation Magazine*, vol. 14, no. 1, pp. 109–118, 2007.
- [167] N. Vahrenkamp, D. Berenson, T. Asfour, J. Kuffner, and R. Dillmann, “Humanoid motion planning for dual-arm manipulation and re-grasping tasks,” in *IEEE/RSJ International Conference on Intelligent Robots and Systems*, oct. 2009, pp. 2464–2470.
- [168] S. Calinon and A. Billard, “Stochastic gesture production and recognition model for a humanoid robot,” in *IEEE/RSJ International Conference on Intelligent Robots and Systems*, 2003, pp. 2769–2774.