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Spectral Efficiency and Fairness Maximization in Full-Duplex Cellular Networks

José Mairton B. da Silva Jr.

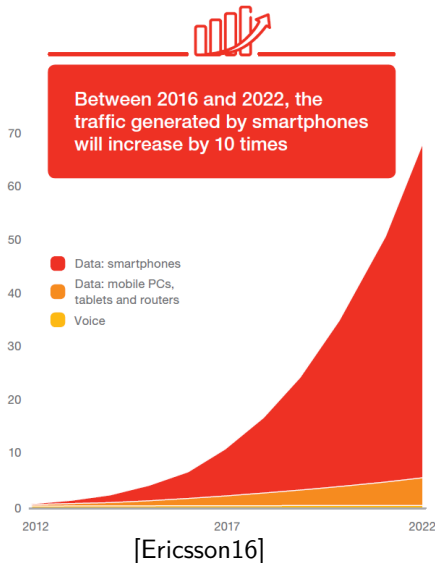
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Need for higher rates in 5G

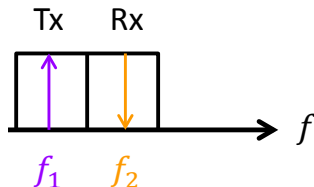
Global mobile traffic (ExaBytes per month)



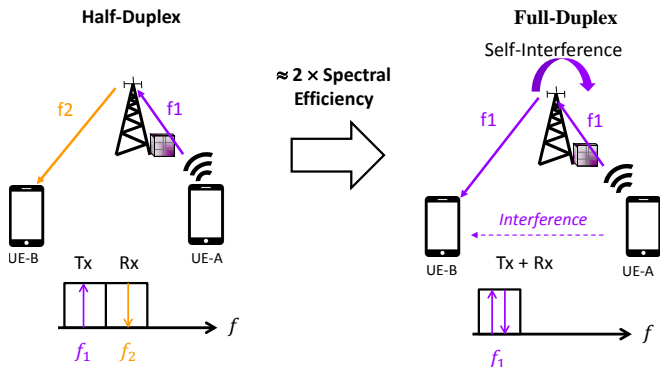
How to meet this demand?

- ↑ antennas at the base station → massive MIMO
- ↑ spectrum → mmWave
- ↑ cells → densification
- ↑ spectral efficient? → **evolve** half-duplex (HD)

Half-Duplex



Half-duplex versus Full-duplex

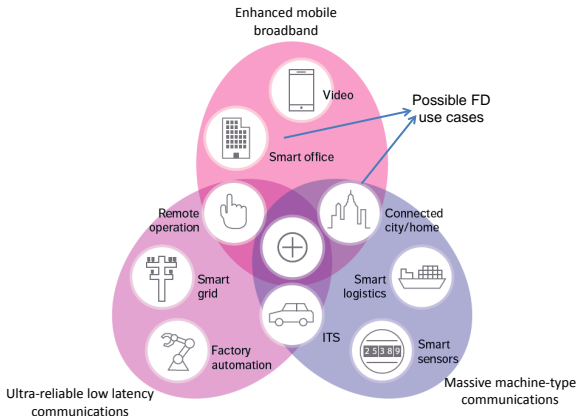


Why half-duplex so far? [Goldsmith05]

“It is generally not possible for radios to receive and transmit on the same frequency band due to the **interference** that results.”

- Recent advances on self-interference (SI) [Bharadia,SIGCOMM13] → **full-duplex is possible**

The role of full-duplex in 5G

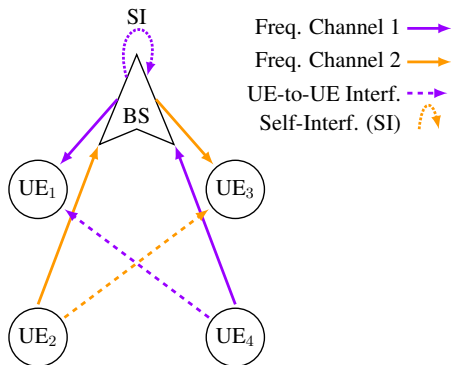


[Ericsson17]

- Full-duplex suitable for short distance + small cells

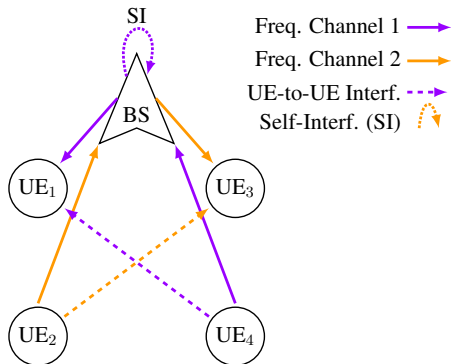
1. Overview of FD cellular networks & main contributions
2. Spectral efficiency maximization
3. Fairness maximization
4. Concluding remarks

1. Overview of FD cellular networks & main contributions
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Benefits

- Spectral efficiency: $\sim 2\times$
- Medium access layer: hidden terminal, collision avoidance, reduced end-to-end delay...



Challenges

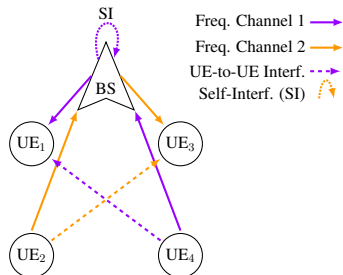
- Severe SI
- UE-to-UE interference
- Mitigate both interferences → user-frequency channel assignment and power allocation





Need of distributed schemes

- Processing burden at the BS is high [Osseiran, COMMAG14]
 - Dense deployment of user
 - New SI cancellation mechanisms
 - Radio resource management

Lack of fair and efficient cross-layer procedures

- How to mitigate UE-to-UE interference and assess fairness?
 - Pairing → uplink to downlink users (flat fading)
 - Assignment → uplink/downlink users to frequency channel (frequency selective fading)
 - Power allocation → mitigate interference
 - Fairness → (weighted sum + min) spectral efficiency maximization



Freq. Channel 1 
Freq. Channel 2 
UE-to-UE Interf. 
Self-Interf. (SI) 

$$\text{maximize}_{\mathbf{X}, \mathbf{p}^u, \mathbf{p}^d} f_0(\mathbf{X}, \mathbf{p}^u, \mathbf{p}^d)$$

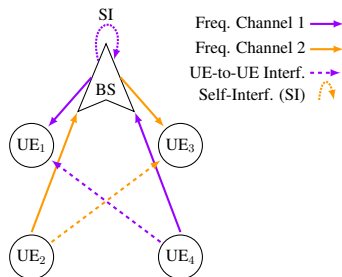
$$\text{subject to } \mathbf{f}_m(\mathbf{X}, \mathbf{p}^u, \mathbf{p}^d) \leq \mathbf{b}_m, \forall m \in \mathcal{M},$$
$$\mathbf{h}_n(\mathbf{X}) \leq \mathbf{c}_n, \forall n \in \mathcal{N},$$
$$\mathbf{X} \in \{0, 1\}^S.$$

Optimization Variables

- Assignment matrix $\rightarrow \mathbf{X} \in \{0, 1\}^S, S = I \times J$

$$x_{ij} = \begin{cases} 1, & \text{if uplink UE}_i \text{ is paired with downlink UE}_j, \\ 0, & \text{otherwise.} \end{cases}$$

- Transmitting powers $\rightarrow \mathbf{p}^u, \mathbf{p}^d$



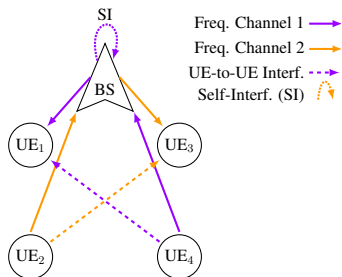
$$\begin{aligned}
 & \text{maximize} && f_0(\mathbf{X}, \mathbf{p}^u, \mathbf{p}^d) \\
 & \mathbf{X}, \mathbf{p}^u, \mathbf{p}^d \\
 & \text{subject to} && \mathbf{f}_m(\mathbf{X}, \mathbf{p}^u, \mathbf{p}^d) \leq \mathbf{b}_m, \quad \forall m \in \mathcal{M}, \\
 & && \mathbf{h}_n(\mathbf{X}) \leq \mathbf{c}_n, \quad \forall n \in \mathcal{N}, \\
 & && \mathbf{X} \in \{0, 1\}^S.
 \end{aligned}$$





Optimization Variables

- Assignment matrix **frequency selective fading** $\rightarrow \mathbf{X} \in \{0, 1\}^S$,
 $S = I \times J \times F$

$$x_{ijf} = \begin{cases} 1, & \text{if uplink UE}_i \text{ is paired with downlink UE}_j \text{ on freq. } f, \\ 0, & \text{otherwise.} \end{cases}$$

- Transmitting powers $\rightarrow \mathbf{p}^u, \mathbf{p}^d$



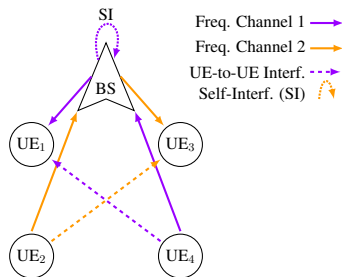
Freq. Channel 1 
Freq. Channel 2 
UE-to-UE Interf. 
Self-Interf. (SI) 

$$\text{maximize}_{\mathbf{X}, \mathbf{p}^u, \mathbf{p}^d} f_0(\mathbf{X}, \mathbf{p}^u, \mathbf{p}^d)$$

$$\text{subject to } \mathbf{f}_m(\mathbf{X}, \mathbf{p}^u, \mathbf{p}^d) \leq \mathbf{b}_m, \forall m \in \mathcal{M},$$
$$\mathbf{h}_n(\mathbf{X}) \leq \mathbf{c}_n, \forall n \in \mathcal{N},$$
$$\mathbf{X} \in \{0, 1\}^S.$$

Objective function $f_0(\mathbf{X}, \mathbf{p}^u, \mathbf{p}^d)$

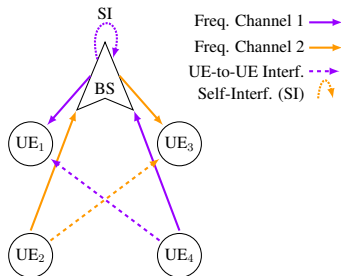
- Sum spectral efficiency \rightarrow sum rate over a given bandwidth
- Fairness \rightarrow worst users should also benefit
- Spectral efficiency + fairness \rightarrow improve the system + the worst users



$$\begin{aligned} & \text{maximize} && f_0(\mathbf{X}, \mathbf{p}^u, \mathbf{p}^d) \\ & \mathbf{X}, \mathbf{p}^u, \mathbf{p}^d \\ & \text{subject to} && \mathbf{f}_m(\mathbf{X}, \mathbf{p}^u, \mathbf{p}^d) \leq \mathbf{b}_m, \forall m \in \mathcal{M}, \\ & && \mathbf{h}_n(\mathbf{X}) \leq \mathbf{c}_n, \forall n \in \mathcal{N}, \\ & && \mathbf{X} \in \{0, 1\}^S. \end{aligned}$$

Constraint function $\mathbf{f}_m(\mathbf{X}, \mathbf{p}^u, \mathbf{p}^d)$

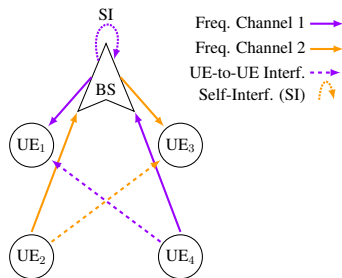
- Minimum quality of service requirements $\rightarrow \mathbf{f}_m(\mathbf{X}, \mathbf{p}^u, \mathbf{p}^d) \rightarrow$ Non-convex
- Maximum transmitting power $\rightarrow \mathbf{f}_m(\mathbf{p}^u, \mathbf{p}^d) \rightarrow$ Convex



$$\begin{aligned} & \text{maximize} && f_0(\mathbf{X}, \mathbf{p}^u, \mathbf{p}^d) \\ & \mathbf{X}, \mathbf{p}^u, \mathbf{p}^d \\ \text{subject to} &&& \mathbf{f}_m(\mathbf{X}, \mathbf{p}^u, \mathbf{p}^d) \leq \mathbf{b}_m, \quad \forall m \in \mathcal{M}, \\ &&& \mathbf{h}_n(\mathbf{X}) \leq \mathbf{c}_n, \quad \forall n \in \mathcal{N}, \\ &&& \mathbf{X} \in \{0, 1\}^S. \end{aligned}$$

Constraint function $\mathbf{h}_n(\mathbf{X})$

- Binary constraints \rightarrow orthogonality of UL/DL users and frequency channels
- Linear constraints



$$\begin{aligned} & \text{maximize} && f_0(\mathbf{X}, \mathbf{p}^u, \mathbf{p}^d) \\ & \mathbf{X}, \mathbf{p}^u, \mathbf{p}^d \\ \text{subject to} &&& \mathbf{f}_m(\mathbf{X}, \mathbf{p}^u, \mathbf{p}^d) \leq \mathbf{b}_m, \quad \forall m \in \mathcal{M}, \\ &&& \mathbf{h}_n(\mathbf{X}) \leq \mathbf{c}_n, \quad \forall n \in \mathcal{N}, \\ &&& \mathbf{X} \in \{0, 1\}^S. \end{aligned}$$

How difficult is this problem?

- Mixed integer nonlinear programming (MINLP) problem \rightarrow difficult to solve
- Some cases of $\mathbf{X} \rightarrow$ NP-hard \rightarrow **no polynomial-time solution known**

Spectral efficiency maximization

- [C1] José Mairton B. da Silva Jr., Y. Xu, G. Fodor, C. Fischione, "Distributed Spectral Efficiency Maximization in Full-Duplex Cellular Networks", in *Proc. IEEE International Conference on Communications (ICC'16)*, May 2016.
- [J1] José Mairton B. da Silva Jr., G. Fodor, C. Fischione, "Fast-Lipschitz Power Control and User-Frequency Assignment in Full-Duplex Cellular Networks," submitted to *IEEE Transactions on Wireless Communications*, February 2017.

Fairness maximization

- [J2] José Mairton B. da Silva Jr., G. Fodor, C. Fischione, "Spectral Efficient and Fair User Pairing for Full-Duplex Communication in Cellular Networks", *IEEE Transactions on Wireless Communications*, Vol. 15, No. 11, pp. 7578-7593, Nov. 2016.
- [C2] José Mairton B. da Silva Jr., G. Fodor, C. Fischione, "On the Spectral Efficiency and Fairness in Full-Duplex Cellular Networks", in *Proc. IEEE International Conference on Communications (ICC'17)*, May 2017, accepted.

	[C1]	[J1]	[J2]	[C2]
User Pairing	✓	✓	✓	✓
Freq. Assignment	-	✓	✓	-
Power Alloc./Control	✓	✓	✓	✓
Distributed	✓	✓	-	-
Objective	Sum SE	Sum SE	Minimum SE	Sum SE + Minimum SE

Spectral efficiency maximization

- Distributed mechanisms for FD cellular networks
 - Auction algorithm [C1] → resource pairing
 - Power control [J1] → SINR and power settings
- SI or UE-to-UE interference → different roles for power allocation and assignment
- Spectral efficiency gains over HD
 - Realistic system simulations → **Yes, + energy savings!**

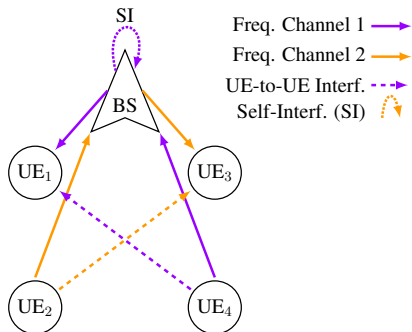
	[C1]	[J1]	[J2]	[C2]
User Pairing	✓	✓	✓	✓
Freq. Assignment	-	✓	✓	-
Power Alloc./Control	✓	✓	✓	✓
Distributed	✓	✓	-	-
Objective	Sum SE	Sum SE	Minimum SE	Sum SE + Minimum SE

Fairness maximization

- Role of assignment and power allocation in fairness
 - Assignment and power allocation → used jointly and should not be split
- Weights to increase fairness [C2] → not necessary if multi-objective optimization
- Fairness gains over simple FD solutions [J2,C2]
 - Realistic system simulations → **Yes, + user connectivity!**

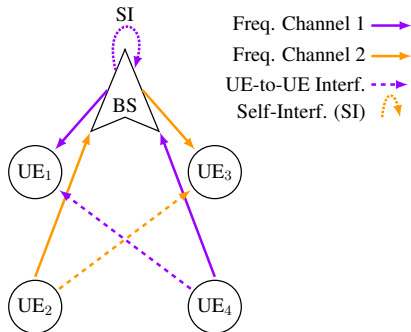
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System Model (1/3)



	[C1]	[J1]	[J2]	[C2]
User Pairing	✓	✓	✓	✓
Freq. Assignment	-	✓	✓	-
Power Alloc./Control	✓	✓	✓	✓
Distributed	✓	✓	-	-
Objective	Sum SE	Sum SE	Minimum SE	Sum SE + Minimum SE

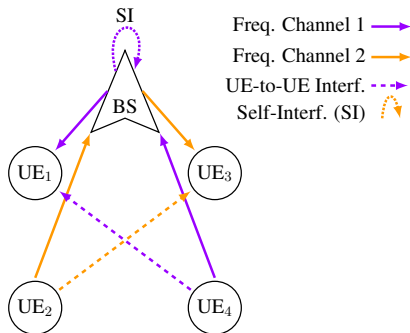
System Model (2/3)



- Single-cell cellular system \rightarrow only BS is FD-capable
- # UL users $\rightarrow I$; # DL users $\rightarrow J$; # Frequency channels $\rightarrow F$
- Path gain with flat fading $\rightarrow G_{ib}, G_{bj}, G_{ij}$
- SI cancellation coefficient $\rightarrow \beta$ **fixed**
- Assignment matrix with flat fading $\rightarrow \mathbf{X} \in \{0, 1\}^{I \times J}$

$$x_{ij} = \begin{cases} 1, & \text{if the UL } UE_i \text{ is paired with the DL } UE_j, \\ 0, & \text{otherwise.} \end{cases}$$

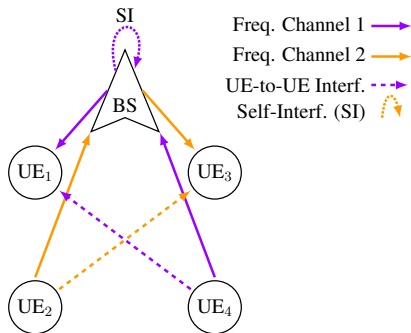
System Model (2/3)



- Single-cell cellular system \rightarrow only BS is FD-capable
- # UL users $\rightarrow I$; # DL users $\rightarrow J$; # Frequency channels $\rightarrow F$
- Path gain for frequency selective fading $\rightarrow G_{ibf}, G_{bjf}, G_{ijf}$
- SI cancellation coefficient $\rightarrow \beta$ fixed
- Assignment matrix freq. selective fading $\rightarrow \mathbf{X} \in \{0, 1\}^{I \times J \times F}$

$$x_{ijf} = \begin{cases} 1, & \text{if the UL UE}_i \text{ is paired with the DL UE}_j \text{ on freq. } f, \\ 0, & \text{otherwise.} \end{cases}$$

System Model (3/3)

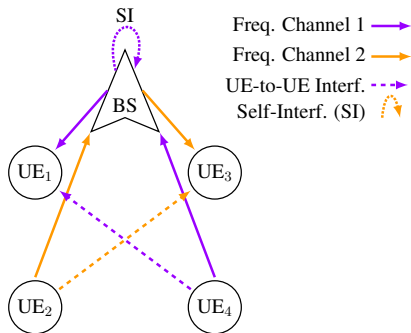


- Power vectors $\rightarrow \mathbf{p}^u = [P_1^u \dots P_I^u]$, $\mathbf{p}^d = [P_1^d \dots P_J^d]$
- Signal-to-interference noise ratio (SINR)

$$\gamma_i^u = \frac{P_i^u G_{ib}}{\sigma^2 + \sum_{j=1}^J x_{ij} P_j^d \beta}, \quad \gamma_j^d = \frac{P_j^d G_{bj}}{\sigma^2 + \sum_{i=1}^I x_{ij} P_i^u G_{ij}}.$$

- Achievable spectral efficiency

$$C_i^u = \log_2(1 + \gamma_i^u), \quad C_j^d = \log_2(1 + \gamma_j^d).$$



- Power vectors $\rightarrow \mathbf{p}^u = [P_1^u \dots P_I^u]$, $\mathbf{p}^d = [P_1^d \dots P_J^d]$
- Signal-to-interference noise ratio (SINR)

$$\gamma_{if}^u = \frac{P_i^u G_{ibf}}{\sigma^2 + \sum_{j=1}^J x_{ijf} P_j^d \beta}, \quad \gamma_{jf}^d = \frac{P_j^d G_{bjf}}{\sigma^2 + \sum_{i=1}^I x_{ijf} P_i^u G_{ijf}}.$$

- Achievable spectral efficiency

$$C_i^u = \sum_{f=1}^F \log_2(1 + \gamma_{if}^u), \quad C_j^d = \sum_{f=1}^F \log_2(1 + \gamma_{jf}^d).$$

- Joint assignment and spectral efficiency maximization (JASEM)

$$\underset{\mathbf{X}, \mathbf{P}^u, \mathbf{P}^d}{\text{maximize}} \quad \sum_{i=1}^I C_i^u + \sum_{j=1}^J C_j^d \quad (\text{Objective})$$

$$\text{subject to} \quad P_i^u \leq P_{\max}^u, \quad \forall i, \quad (\text{Maximum Tx. power UL})$$

$$P_j^d \leq P_{\max}^d, \quad \forall j, \quad (\text{Maximum Tx. power DL})$$

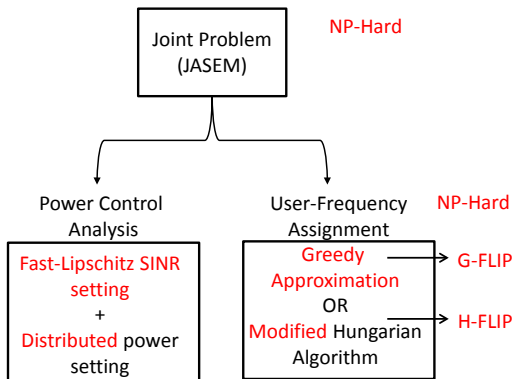
$$\sum_{j=1}^J \sum_{f=1}^F x_{ijf} \leq 1, \quad \forall i, \quad (\text{User orthogonality UL})$$

$$\sum_{i=1}^I \sum_{f=1}^F x_{ijf} \leq 1, \quad \forall j, \quad (\text{User orthogonality DL})$$

$$\sum_{i=1}^I \sum_{j=1}^J x_{ijf} \leq 1, \quad \forall f, \quad (\text{User orthogonality freq.})$$

$$x_{ijf} \in \{0, 1\}, \quad \forall i, j, f. \quad (\text{Binary association})$$

Solution approach for JASEM



- Power control analysis \rightarrow fixed \mathbf{X} and variables $\mathbf{p}^u, \mathbf{p}^d$
 - Power allocation problem \rightarrow vector transformation + hypograph equivalent form
- User-frequency assignment \rightarrow fixed $\mathbf{p}^u, \mathbf{p}^d$ and variable \mathbf{X}
 - NP-Hard \rightarrow greedy approximation

Power allocation problem

$$\begin{aligned} & \underset{\mathbf{p}^u, \mathbf{p}^d}{\text{maximize}} && \sum_{i=1}^I C_i^u + \sum_{j=1}^J C_j^d \\ & \text{subject to} && \mathbf{p}^u, \mathbf{p}^d \in \mathcal{P}. \end{aligned} \quad \longleftrightarrow$$

Power + spectral efficiency problem

$$\begin{aligned} & \underset{\mathbf{p}, \mathbf{t}}{\text{maximize}} && \sum_{k=1}^K t_k \\ & \text{subject to} && t_k \leq \alpha_k \log(1 + \gamma_k(\mathbf{p})), \forall k, \\ & && P_k \leq P_{\max}^{(k)}, \forall k. \end{aligned}$$

Lemma on t_k

The diagonal matrix $\mathbf{T} = [\exp(t_k/\alpha_k) - 1]_k$ of adaptive SINR targets is feasible if and only if

$$\rho(\mathbf{TF}) < 1.$$

- Lemma on $t_k \rightarrow$ **target inequality** for pair (k, l) sharing resource

$$\exp\left(\frac{t_k}{\alpha_k} + \frac{t_l}{\alpha_l}\right) - \exp\left(\frac{t_k}{\alpha_k}\right) - \exp\left(\frac{t_l}{\alpha_l}\right) \leq \epsilon \left(\frac{G_{kb}^u G_{bl}^d}{\beta G_{lk}} - 1 \right).$$

Spectral efficiency target

$$\begin{aligned} & \underset{t_k, t_l}{\text{maximize}} && t_k + t_l \\ & \text{subject to} && \text{(target inequality)}, \longleftrightarrow \\ & && t_k, t_l \geq 0. \end{aligned}$$

Fast-Lipschitz form [Fischione, TAC11]

$$\begin{aligned} & \underset{t_k, t_l}{\text{maximize}} && t_k + t_l \\ & \text{subject to} && t_k \leq t_k - \gamma h(t_k, t_l), \\ & && \mathbf{x} = [t_k \ t_l] \in \mathcal{X}, \end{aligned}$$

Lemma on t_k

If $\frac{\partial h(t_k, t_l)}{\partial t_l} < \frac{\partial h(t_k, t_l)}{\partial t_k}$, and the parameter γ is constrained as $\left(2 \frac{\partial h(t_k, t_l)}{\partial t_k}\right)^{-1} < \gamma < \left(\frac{\partial h(t_k, t_l)}{\partial t_k}\right)^{-1}$, then problem above is Fast-Lipschitz.

Distributed spectral efficiency target + power setting

- $t_k \rightarrow$ Fast-Lipschitz optimization
- $t_l \rightarrow$ use t_k with golden search optimization
- Use t_k, t_l to find P_k, P_l that minimizes $P_k + P_l$
- $\therefore \rightarrow$ Close-to-optimal spectral efficiency + min. sum power

- Axial 3D Assignment problem \rightarrow NP-Hard

$$\underset{\mathbf{x}}{\text{maximize}} \quad \sum_{i=1}^I \sum_{j=1}^J \sum_{f=1}^F \left(C_{if}^u + C_{jf}^d \right) x_{ijf} \quad (\text{Objective})$$

$$\text{subject to} \quad \sum_{j=1}^J \sum_{f=1}^F x_{ijf} = 1, \quad \forall i, \quad (\text{User orthogonality UL})$$

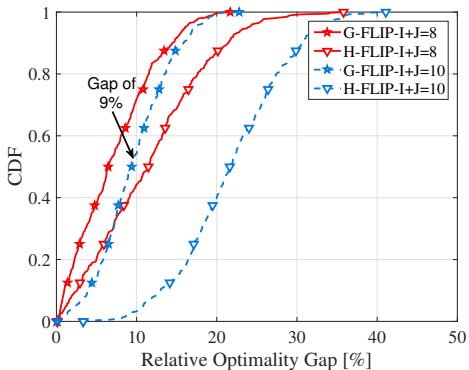
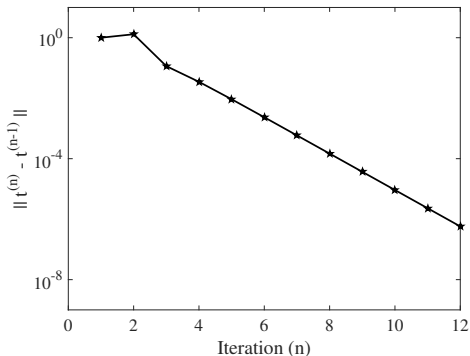
$$\sum_{i=1}^I \sum_{f=1}^F x_{ijf} = 1, \quad \forall j, \quad (\text{User orthogonality DL})$$

$$\sum_{i=1}^I \sum_{j=1}^J x_{ijf} = 1, \quad \forall f, \quad (\text{User orthogonality freq})$$

$$x_{ijf} \in \{0, 1\}, \quad \forall i, j, f, \quad (\text{Binary association})$$

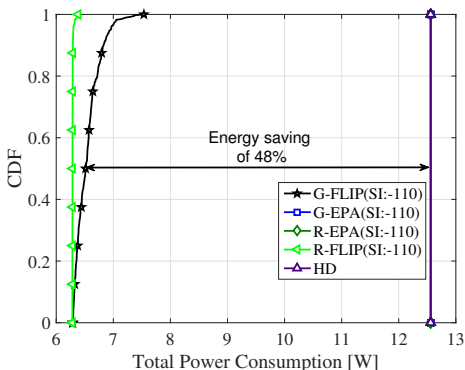
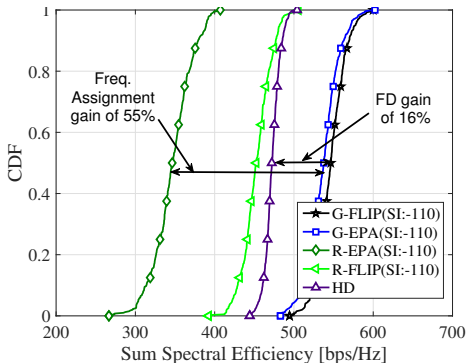
Solution approach

- Start with best pair and continue until all users are paired
- Greedy approximation \rightarrow performance guarantee of $1/3$
- Modified Hungarian algorithm \rightarrow transforms 3D into 2D + Hungarian algorithm



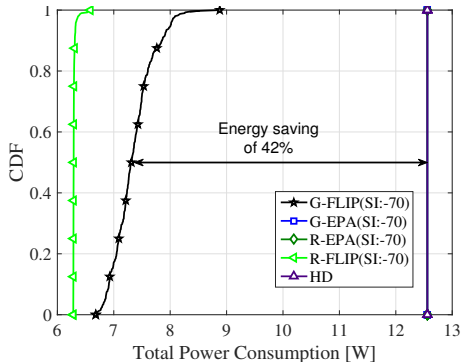
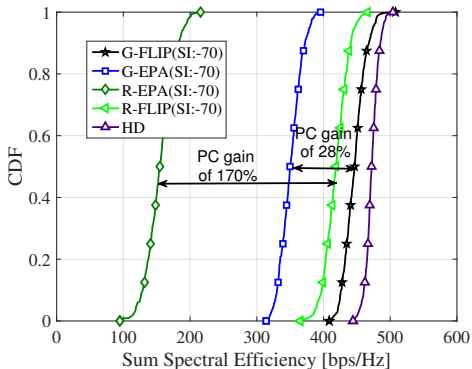
- Convergence with accuracy 10^{-6} in 12 iterations
- G-FLIP \rightarrow close to optimality
- H-FLIP \rightarrow large optimality gap for high number of users

Results for interference-limited regime -25 UL/DL UEs



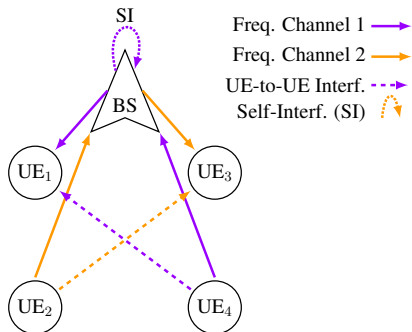
- Most of the gains (G-FLIP & G-EPA) → **greedy assignment**
- Power control (FLIP) + poor assignment (R) → still no gains
- Expected → large gains in **energy efficiency**

Results for SI-limited regime - 25 UL/DL UEs



- Most of the gains (G-FLIP & R-FLIP) → **power control (FLIP)**
- Power control + greedy assignment → still no gains over HD
- Expected → large gains in **energy efficiency**

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	[C1]	[J1]	[J2]	[C2]
User Pairing	✓	✓	✓	✓
Freq. Assignment	-	✓	✓	-
Power Alloc./Control	✓	✓	✓	✓
Distributed	✓	✓	-	-
Objective	Sum SE	Sum SE	Minimum SE	Sum SE + Minimum SE

- Joint assignment and fairness maximization (JAFM)

$$\underset{\mathbf{X}^u, \mathbf{X}^d, \mathbf{P}^u, \mathbf{P}^d}{\text{maximize}} \quad \min_{\forall i, j} \{C_i^u, C_j^d\} \quad (\text{Objective})$$

$$\text{subject to} \quad \sum_{f=1}^F \gamma_{if}^u \geq \gamma_{\text{th}}^u, \quad \forall i, \quad (\text{Minimum SINR constraint UL})$$

$$\sum_{f=1}^F \gamma_{jf}^d \geq \gamma_{\text{th}}^d, \quad \forall j, \quad (\text{Minimum SINR constraint DL})$$

$$P_i^u \leq P_{\text{max}}^u, \quad \forall i, \quad (\text{Maximum Tx. power UL})$$

$$P_j^d \leq P_{\text{max}}^d, \quad \forall j, \quad (\text{Maximum Tx. power DL})$$

$$\sum_{i=1}^I x_{if}^u \leq 1, \quad \forall f, \quad (\text{User-frequency orthogonality UL})$$

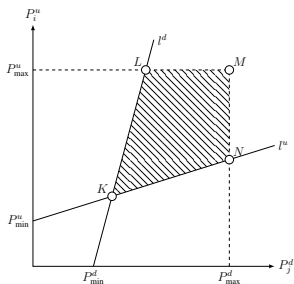
$$\sum_{f=1}^F x_{if}^u \leq 1, \quad \forall i, \quad (\text{Frequency orthogonality in UL})$$

$$\sum_{j=1}^J x_{jf}^d \leq 1, \quad \forall f, \quad (\text{User-frequency orthogonality DL})$$

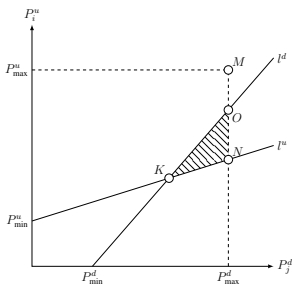
$$\sum_{f=1}^F x_{jf}^d \leq 1, \quad \forall j, \quad (\text{Frequency orthogonality in DL})$$

$$x_{if}^u, x_{jf}^d \in \{0, 1\}, \quad \forall i, j, f. \quad (\text{Binary association})$$

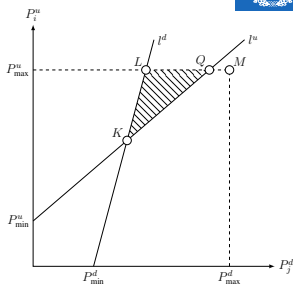
Admissible area



$$\gamma_{iMf}^u > \gamma_{th}^u, \gamma_{jMf}^d \geq \gamma_{th}^d$$



$$\gamma_{iMf}^u > \gamma_{th}^u, \gamma_{jMf}^d < \gamma_{th}^d$$



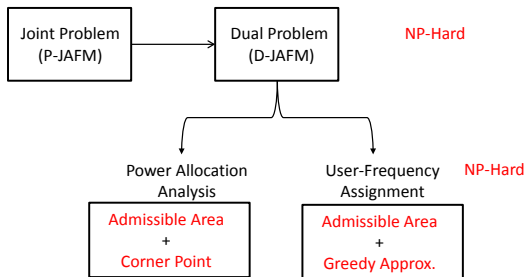
$$\gamma_{iMf}^u \leq \gamma_{th}^u, \gamma_{jMf}^d \geq \gamma_{th}^d$$

Lemma on admissible β

Pair (i, j) on frequency f is an *admissible* if the SI is $\beta \leq \beta_{ijf}^{\max}$

$$\beta_{ijf}^{\max} = \begin{cases} \frac{G_{bjf}(P_{\max}^u G_{ibf} - \gamma_{th}^u \sigma^2)}{\gamma_{th}^u \gamma_{th}^d (P_{\max}^u G_{ijf} + \sigma^2)}, & \text{if } \gamma_{jMf}^d > \gamma_{th}^d, \\ \frac{P_{\max}^d G_{bjf} G_{ibf} - \sigma^2 \gamma_{th}^d (G_{ijf} \gamma_{th}^u + G_{ibf})}{\gamma_{th}^u \gamma_{th}^d P_{\max}^d G_{ijf}}, & \text{if } \gamma_{jMf}^d \leq \gamma_{th}^d. \end{cases}$$

Solution approach for JAFM (1/2)



- Lagrangian duality \rightarrow power allocation + user-frequency assignment
- Power allocation analysis \rightarrow optimal allocation in corner point of admissible area
- User-frequency assignment \rightarrow greedy approximation for users in the admissible area

Solution approach for JAFM (2/2)

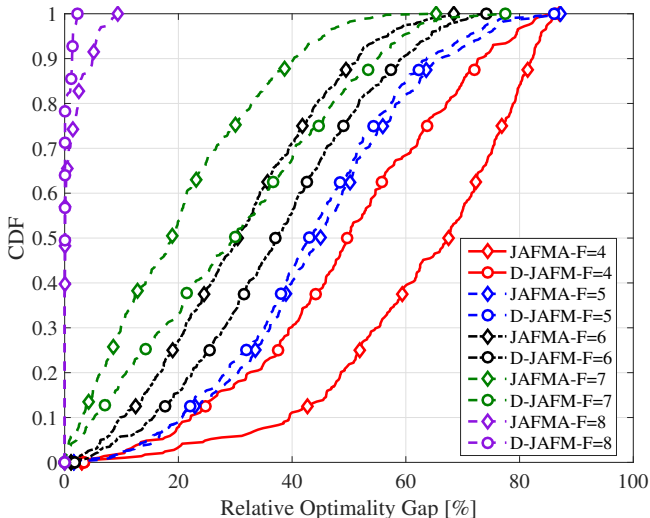
$$\begin{aligned}
 & \underset{\mathbf{x}}{\text{maximize}} && \sum_{i=1}^I \sum_{j=1}^J \sum_{f=1}^F \left(\min\{C_{if}^u, C_{jf}^d\} \right) x_{ijf} && \text{(Objective)} \\
 & \text{subject to} && \sum_{j=1}^J \sum_{f=1}^F x_{ijf} = 1, \forall i, && \text{(User orthogonality UL)} \\
 & && \sum_{i=1}^I \sum_{f=1}^F x_{ijf} = 1, \forall j, && \text{(User orthogonality DL)} \\
 & && \sum_{i=1}^I \sum_{j=1}^J x_{ijf} = 1, \forall f, && \text{(User orthogonality freq)} \\
 & && x_{ijf} \in \{0, 1\}, \forall i, j, f, && \text{(Binary association)}
 \end{aligned}$$

- Start with best admissible pair and continue until all users are paired
- Performance guarantee of 1/3
- Power allocation + greedy approximation \rightarrow JAFMA

JAFMA

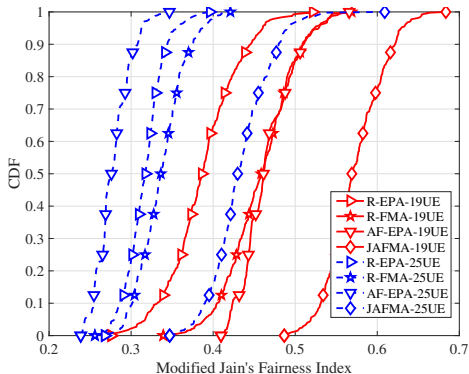
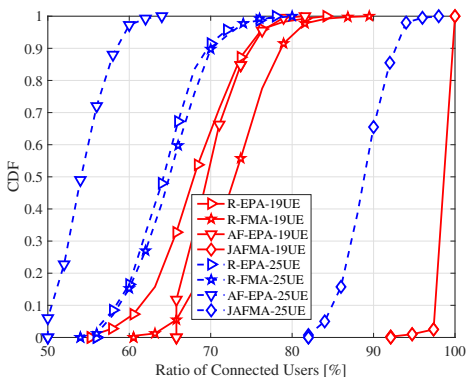
- Duality gap \downarrow as number of frequency channel \uparrow
- JAFMA \rightarrow approximate solution to JAFM

Optimality gap for JAFMA - $\beta = -100\text{dB}$



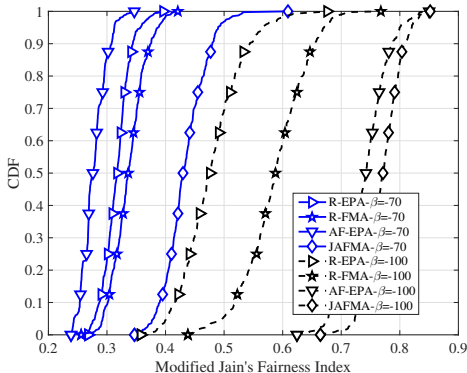
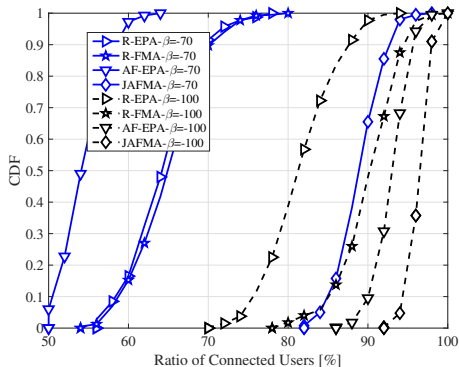
- JAFMA \rightarrow optimality gap decreases with increasing F

Analysis for different users' loads - $\beta = -70\text{dB}$



- JAFMA \rightarrow highest **user connectivity + fairness**
- Greedy assignment (AF) + equal power allocation \rightarrow still no gains
- Optimal power allocation (FMA) + poor assignment \rightarrow still no gains

Analysis for different β - 25 UL/DL UEs



- $\beta = -100$ dB
 - JAFMA \rightarrow gains in **user connectivity + fairness**
 - Split JAFMA \rightarrow still good performance
- $\beta = -70$ dB
 - JAFMA \rightarrow **large** gains in **user connectivity + fairness**
 - Split JAFMA \rightarrow poor performance

1. Overview of FD cellular networks & main contributions
2. Spectral efficiency maximization
3. Fairness maximization
4. Concluding remarks

Sum spectral efficiency maximization

- **Gains** over HD with **distributed solutions**
 - Auction theory + optimal power allocation → **weighted sum spectral efficiency**
 - Fast-Lipschitz optimization + greedy approximation → **spectral and energy efficiency**
- **Different roles** of assignment and power control → interference- or SI-limited regime

Fairness maximization

- **Gains** for **minimum achieved spectral efficiency** + **connectivity**
- Joint solutions + UE-to-UE interference consideration → **higher fairness**
- Multi-objective optimization → **PL weights not necessary**

Some references (1/2)



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Thanks for your attention!



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Spectral Efficiency and Fairness Maximization in Full-Duplex Cellular Networks

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