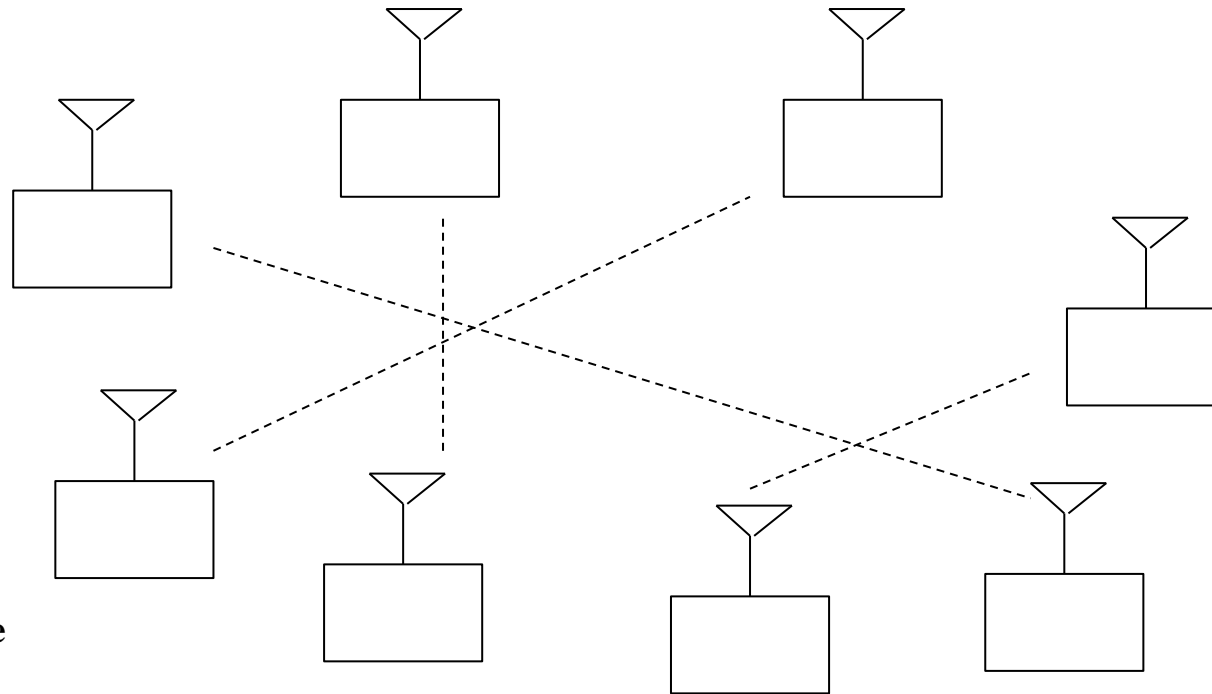


Interference Alignment and Co-Ordinated Multi-Point with 802.11ac-feedback: Testbed Results

Per Zetterberg



Astonishing Result



Cadambe/Jafar, "Interference Alignment and Degrees of Freedom of the K-User Interference Channel", IEEE Trans, Information Theory 2008.

K-transmitters and K-receivers, K-links:
K/2 simultaneous interference-free links.
Requires coding over multiple channel realizations.
Global channel knowledge required.

Channel extension (Cadambe/Jafar)

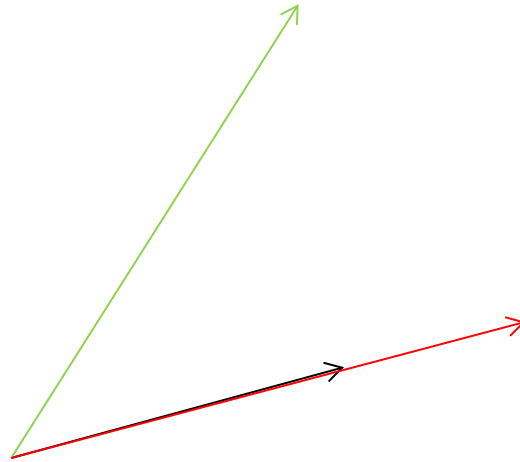
$$\bar{\mathbf{Y}}^{[i]} = \bar{\mathbf{H}}^{[i1]} \bar{\mathbf{V}}^{[1]} \mathbf{X}^{[1]} + \bar{\mathbf{H}}^{[i2]} \bar{\mathbf{V}}^{[2]} \mathbf{X}^{[2]} + \bar{\mathbf{H}}^{[i3]} \bar{\mathbf{V}}^{[3]} \mathbf{X}^{[3]} + \bar{\mathbf{Z}}^{[i]}$$

$$\mathbf{H}^{[ij]} = \text{diag} \left(h^{ij} (f_1, t_1), \dots, h^{ij} (f_m, t_m) \right)$$

$$\begin{aligned}
 m &= 2n + 1 \\
 \frac{3n + 1}{2n + 1} &\Rightarrow 1.5
 \end{aligned}$$

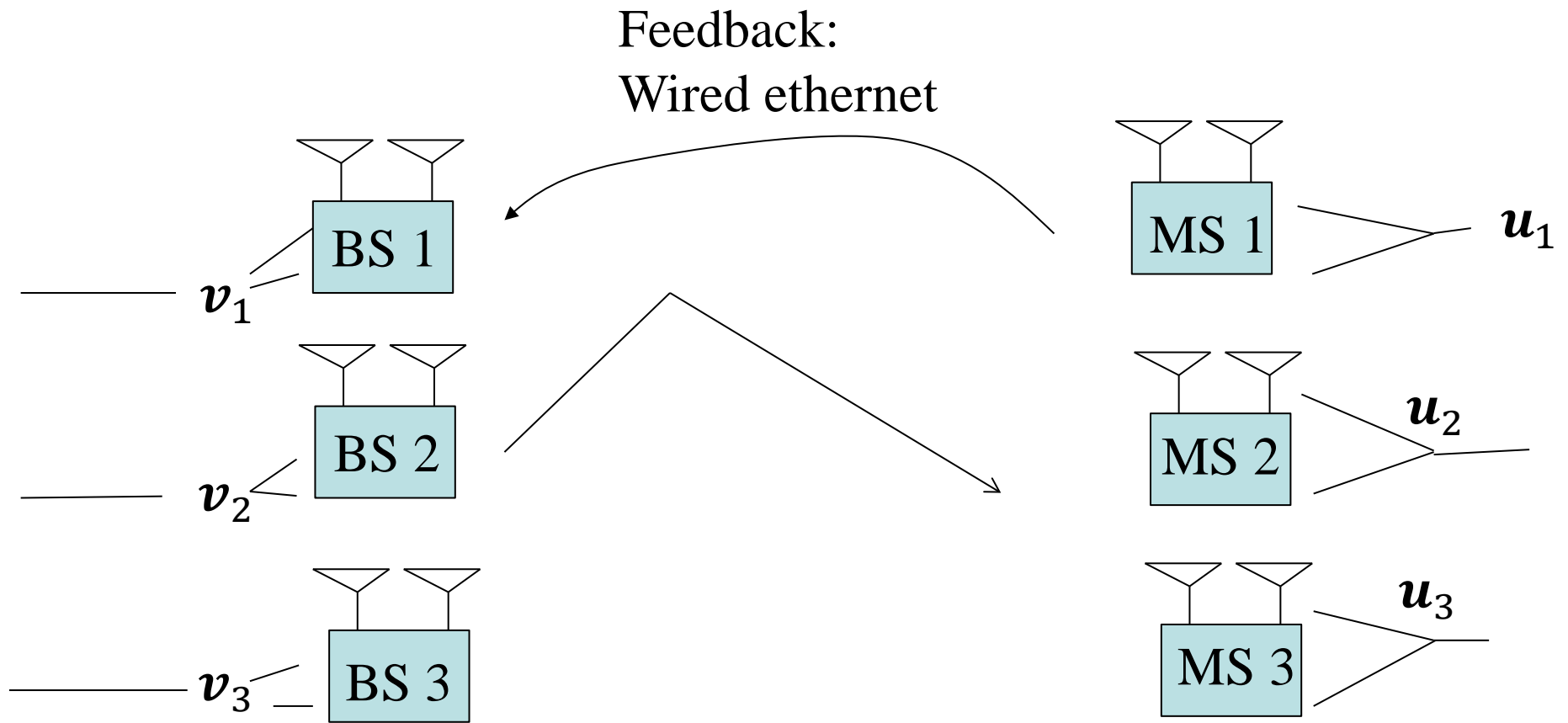

 Channel extended MIMO channel (my wording)

The "alignment"



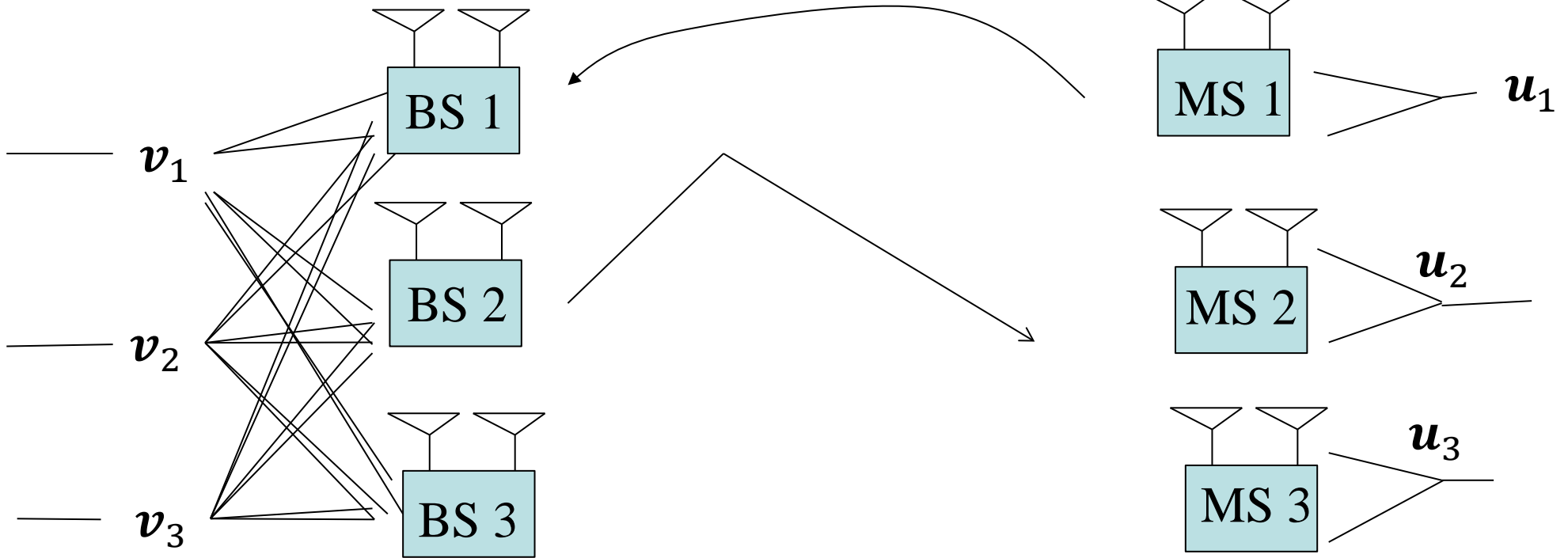
$$\mathbf{y} = \mathbf{w}^{\mathbf{H}} (\mathbf{x}_D + \mathbf{x}_1 + \dots + \mathbf{x}_N) = \mathbf{w}^{\mathbf{H}} \mathbf{x}_D$$

Implementation IA



Implementation: CoMP

Feedback:
Wired ethernet



Beamformer

$$\text{SNIR}_k = \frac{\left| \mathbf{u}_k^* \mathbf{H}_{k,k} \mathbf{v}_k \right|^2}{\sum_{n \neq k} \left| \mathbf{u}_k^* \mathbf{H}_{k,n} \mathbf{v}_n \right|^2 + \tilde{\sigma}^2}$$

"Approaching the Capacity of Wireless Networks through Distributed Interference Alignment", by Krishna Gomadam, Viveck R. Cadambe and Syed A. Jafar.

$$\tilde{\sigma}^2 = \max \left(\sigma_N^2, 0.001 \sum_n \left| \mathbf{H}_{k,n} \right|^2 \right)$$

Beamformer initialization CoMP

$$\mathbf{H}_1 = [\mathbf{H}_{11}, \mathbf{H}_{12}, \mathbf{H}_{13}] = \mathbf{U}_1 \mathbf{S}_1 \mathbf{V}_1^H$$

$$\mathbf{H}_2 = [\mathbf{H}_{21}, \mathbf{H}_{22}, \mathbf{H}_{23}] = \mathbf{U}_2 \mathbf{S}_2 \mathbf{V}_2^H$$

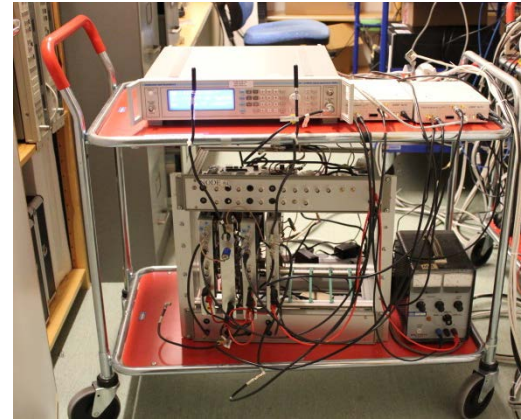
$$\mathbf{H}_3 = [\mathbf{H}_{31}, \mathbf{H}_{32}, \mathbf{H}_{33}] = \mathbf{U}_3 \mathbf{S}_3 \mathbf{V}_3^H$$

$$\tilde{\mathbf{V}} = [\mathbf{V}_1(:,1) \quad \mathbf{V}_2(:,1) \quad \mathbf{V}_3(:,1)]$$

$$\mathbf{W} = \tilde{\mathbf{V}} (\tilde{\mathbf{V}}^H \tilde{\mathbf{V}})^{-1}$$

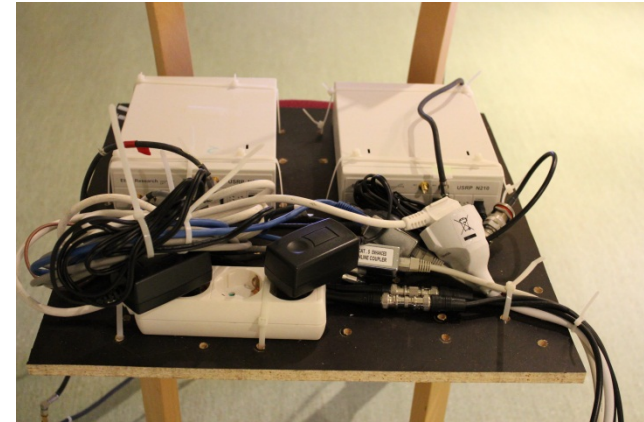
The testbed

3MS

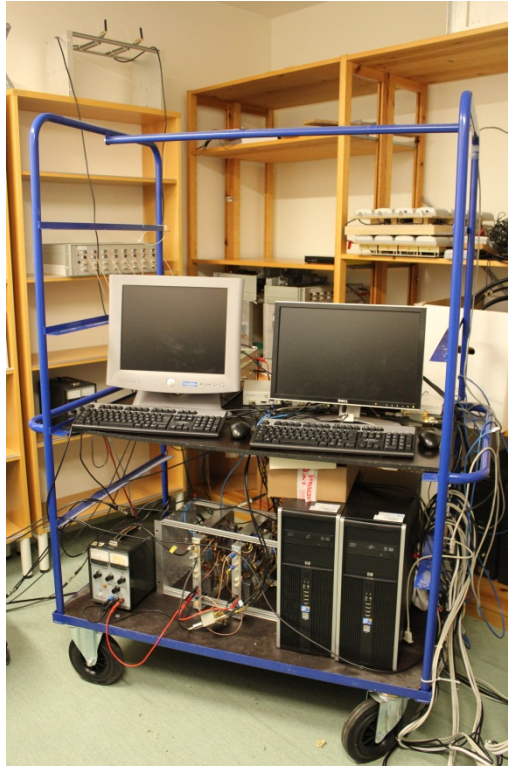


10m

3BS



10m



$P=10\text{dBm}$
 $NF=10-11\text{dB}$

IEEE 802.11ac feedback

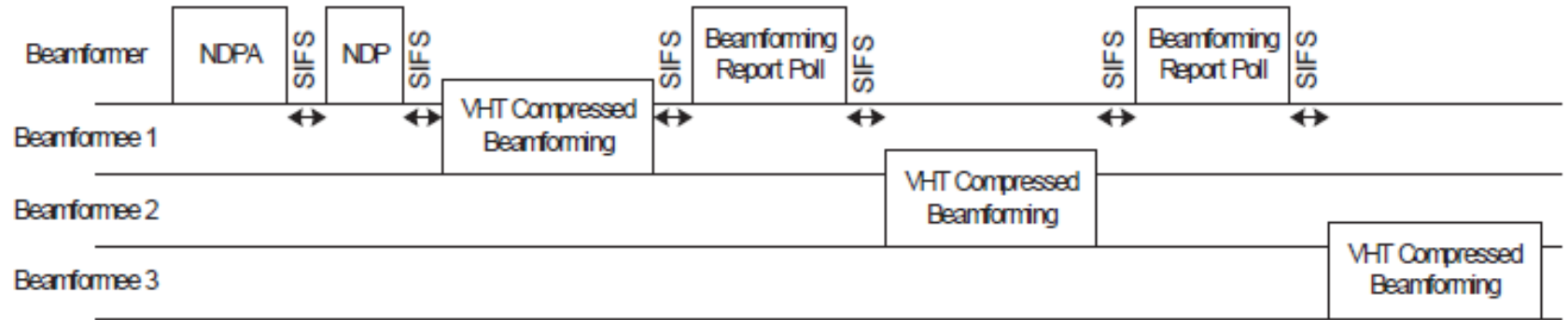


Figure 9-41b—Sounding protocol with more than one beamformee

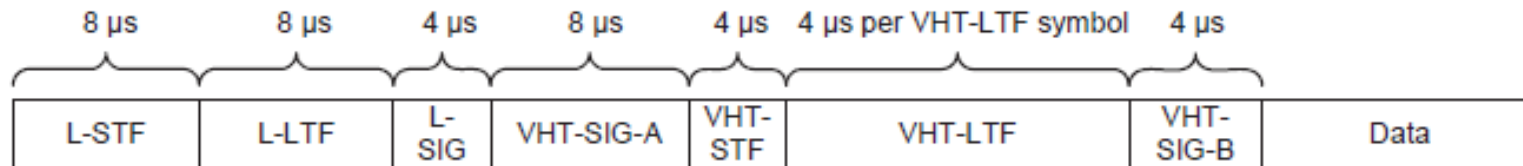


Figure 22-2—VHT PPDU format

Training symbols
One per antenna

IEEE 802.11ac feedback, contd.

$$\mathbf{H} = \mathbf{U} \mathbf{S} \mathbf{V}^H$$

$$\mathbf{V} = \left[\prod_{i=1}^{N_r} \left[D_i \left(1_{i-1} e^{j\phi_{i,i}}, \dots, e^{j\phi_{N_r,1,i}}, 1 \right) \prod_{l=i+1}^{N_r} G_l^T(\psi_l) \right] \tilde{\mathbf{I}}_{N_r \times N_c} \right]$$

Number of phis and psis : $N_c N_r - N_c^2 / 2 - N_c / 2$

Range $0, 2\pi$

Range $0, \pi / 2$

Quantization bits = 7 or 9

Quantization bits 5 or 7

The whole 6×2 matrix is treated by the three MSs.

Frequency granularity

Channel Width	N_g	N_s	Subcarriers for which Compressed Feedback Beamforming Matrix subfield is sent: $scidx(0), scidx(1), \dots, scidx(N_s-1)$
20 MHz	1	52	-28, -27, -26, -25, -24, -23, -22, -20, -19, -18, -17, -16, -15, -14, -13, -12, -11, -10, -9, -8, -6, -5, -4, -3, -2, -1, 1, 2, 3, 4, 5, 6, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 22, 23, 24, 25, 26, 27, 28 NOTE—Pilot subcarriers ($\pm 21, \pm 7$) and DC subcarrier (0) are skipped
	2	30	-28, -26, -24, -22, -20, -18, -16, -14, -12, -10, -8, -6, -4, -2, -1, 1, 2, 4, 6, 8, 10, 12, 14, 16, 18, 20, 22, 24, 26, 28
	4	16	-28, -24, -20, -16, -12, -8, -4, -1, 1, 4, 8, 12, 16, 20, 24, 28

Our implementation:

14MHz	1	38	-19, -18, -17, -16, -15, -14, -13, -12, -11, -10, -9, -8, -6, -5, -4, -3, -2, -1, 1, 2, 3, 4, 5, 6, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19
	2	20	-18, -16, -14, -12, -10, -8, -6, -4, -2, -1, 1, 2, 4, 6, 8, 10, 12, 14, 16, 18
	4	8	-12, -8, -4, -1, 1, 4, 8, 12
	8	6	-16, -8, -1, 1, 8, 16
	16	4	-16, -1, 1, 16

SNR feedback

$$\Delta SNR_{k,i} = \begin{cases} \min(\text{round}(10\log_{10}\left(\frac{\|H_k V_{k,i}\|^2}{N}\right) - \overline{SNR}_i), 7), & \text{if } 10\log_{10}\left(\frac{\|H_k V_{k,i}\|^2}{N}\right) \geq \overline{SNR}_i \\ \min(\text{round}(10\log_{10}\left(\frac{\|H_k V_{k,i}\|^2}{N}\right) - \overline{SNR}_i), -8), & \text{otherwise} \end{cases}$$

Channel Width	Ng	Ns'	Subcarriers for which the Delta SNR subfield is sent: $scidx(0), scidx(1), \dots, scidx(Ns'-1)$
20 MHz	1	30	-28, -26, -24, -22, -20, -18, -16, -14, -12, -10, -8, -6, -4, -2, -1, 1, 2, 4, 6, 8, 10, 12, 14, 16, 18, 20, 22, 24, 26, 28
	2	16	-28, -24, -20, -16, -12, -8, -4, -1, 1, 4, 8, 12, 16, 20, 24, 28
	4	10	-28, -20, -12, -4, -1, 1, 4, 12, 20, 28

14MHz	1	20	-18, -16, -14, -12, -10, -8, -6, -4, -2, -1, 1, 2, 4, 6, 8, 10, 12, 14, 16, 18";
	2	10	-16, -12, -8, -4, -1, 1, 4, 8, 12, 16
	4	8	12, -8, -4, -1, 1, 4, 8, 12
	8	4	-8, -1, 1, 8
	16	2	-16, 16

Interpolate between subcarriers

Reuse V on adjacent subcarriers.

Interpolate SNR values

Reconstruct H as:

$$H = \text{diag}(\text{SNR}_0, \text{SNR}_1) * V.$$

Overhead

- The three short frames $\approx 2*60\mu\text{s} + \text{num_users}*60\mu\text{s}$
- Gaps = 2 SIFS + num_users SIFS
- Number of feedback bits per V matrix = $(N_c N_r - N_c^2 / -N_c)$
(7+9)
- Number of feedback for SNR $\text{num_users} * 8 * \text{SNR}_s * N_r$

Feedback time in our case $\approx 350\mu\text{s} + 1065\mu\text{s} / (N_g * R)$

$N_g = 4, R = 2 \Rightarrow 500\mu\text{s}$

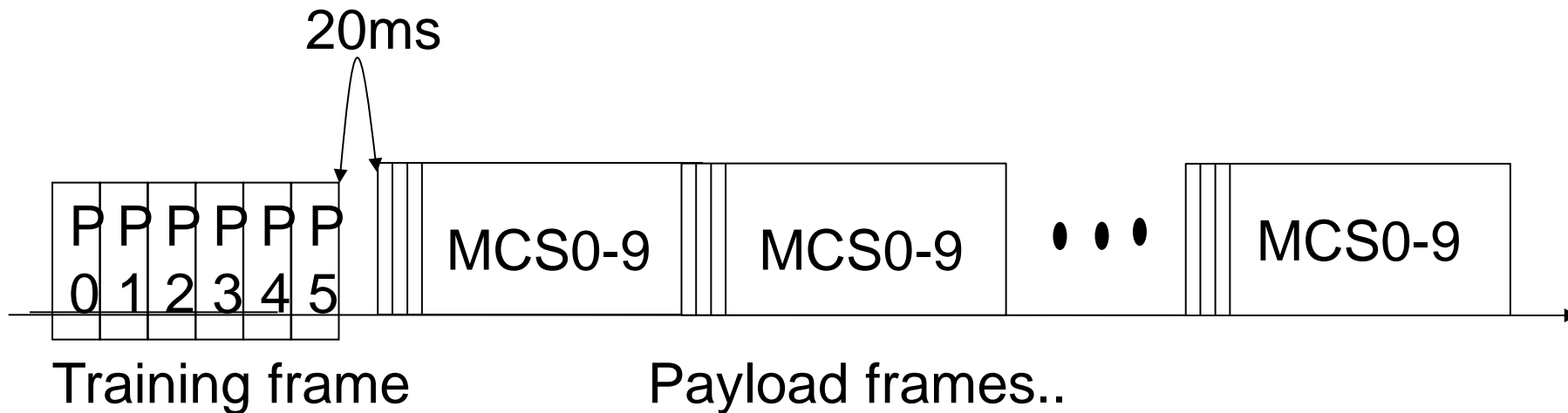
With update interval : 20ms

\Rightarrow Overhead 2.5%

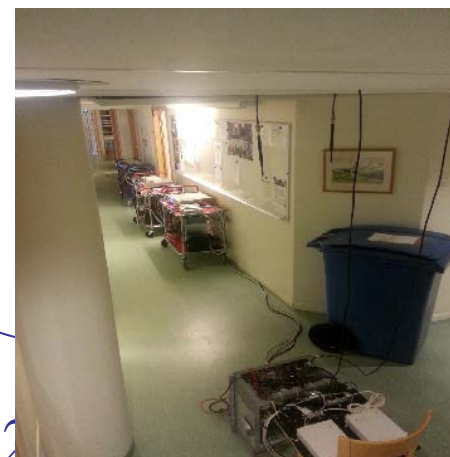
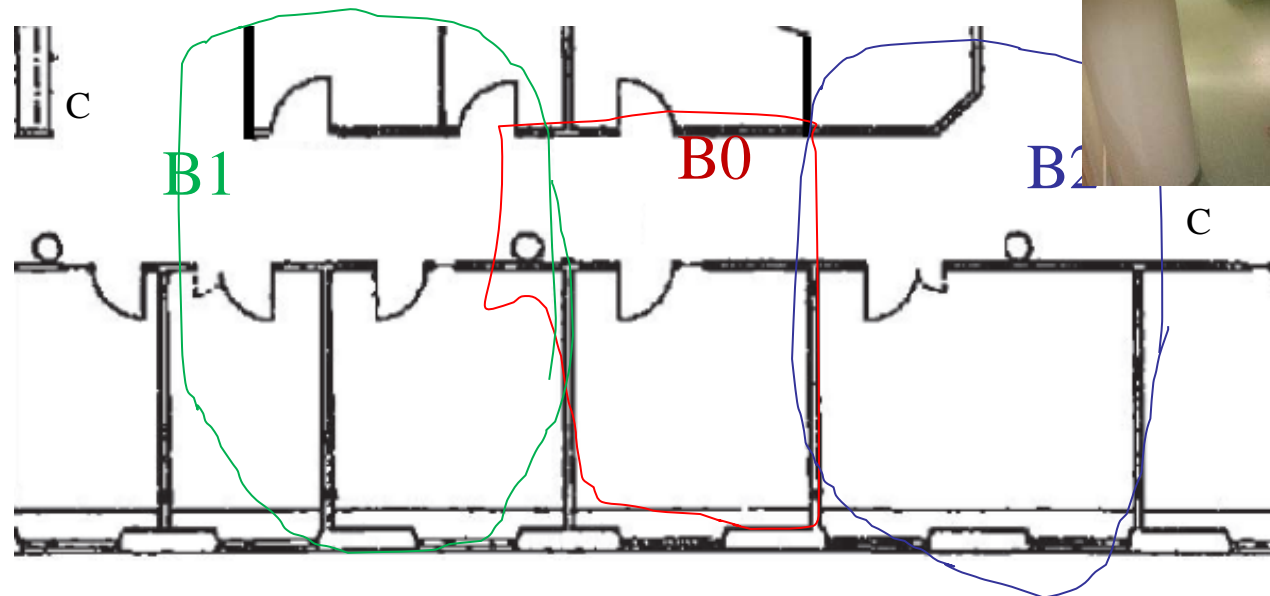
Based on: *Improved MU-MIMO Performance for Future 802.11 Systems Using Differential Feedback*, Ron Porat

Our implementation

1. BS1 sends P0,P1
2. BS2 sends P2,P3
3. BS3 sends P4,P5
4. MS1-MS3 sends compressed V matrix to BS1.
5. BS1 un-compresses calculates all beamformers using max SINR on 38subcarriers.
6. Each BS sends beamformed frames.
7. MSs saves all data.
8. Post-processing of received signals.

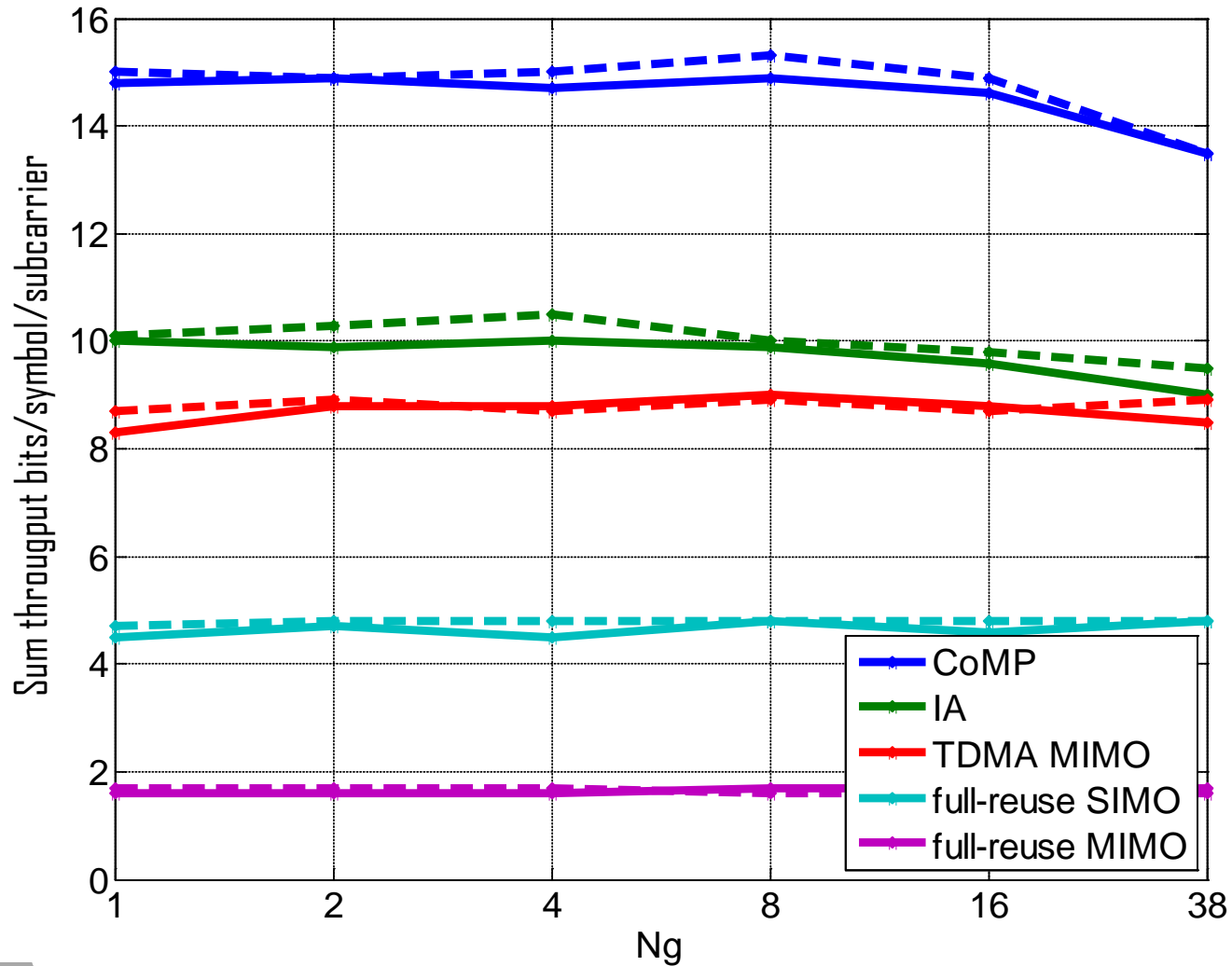


Measurement environment

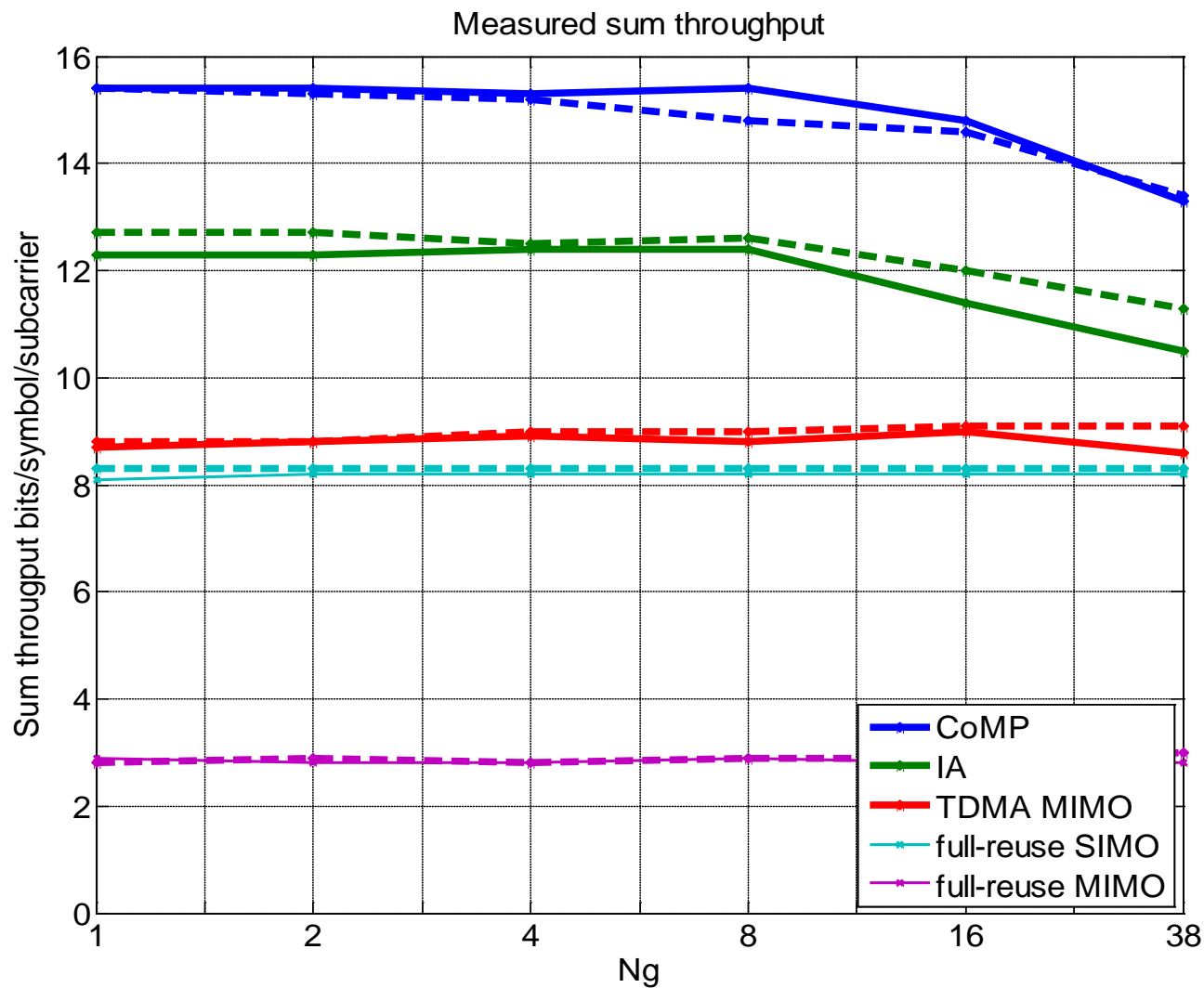


Results LoS (stationary)

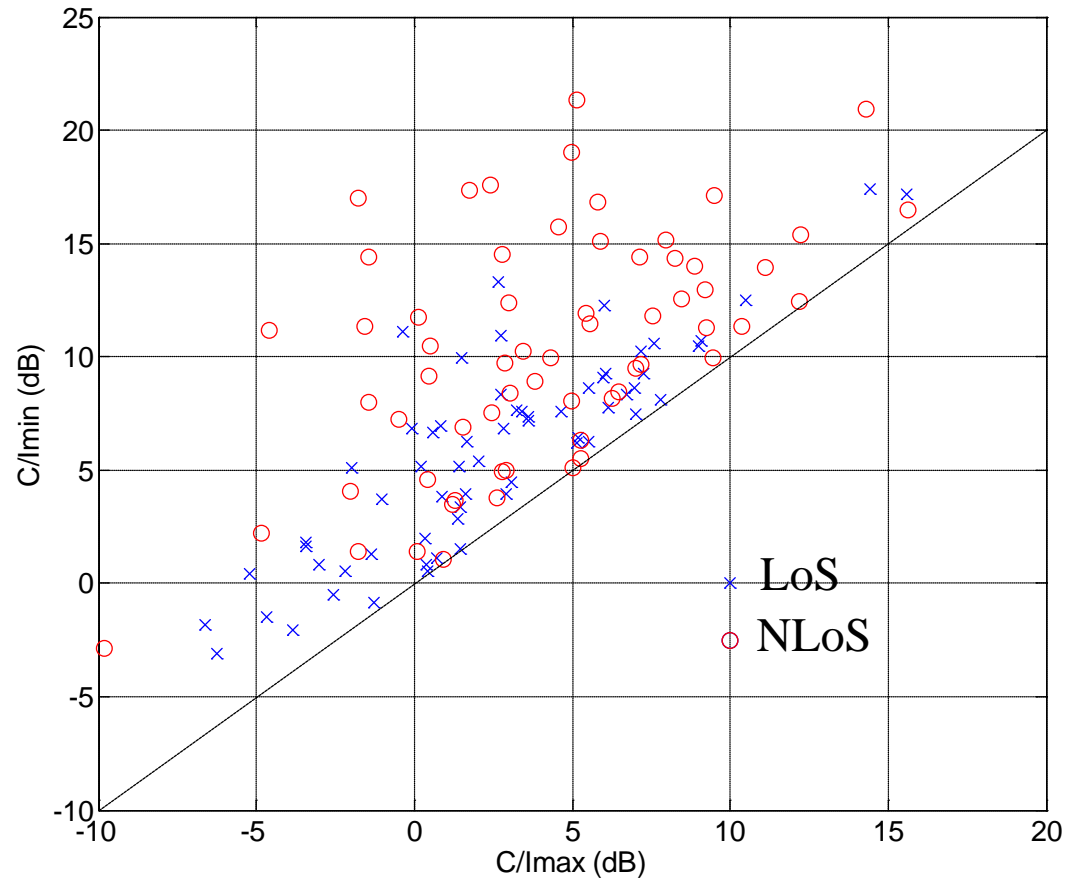
Measured sum throughput



Results NLoS (stationary)



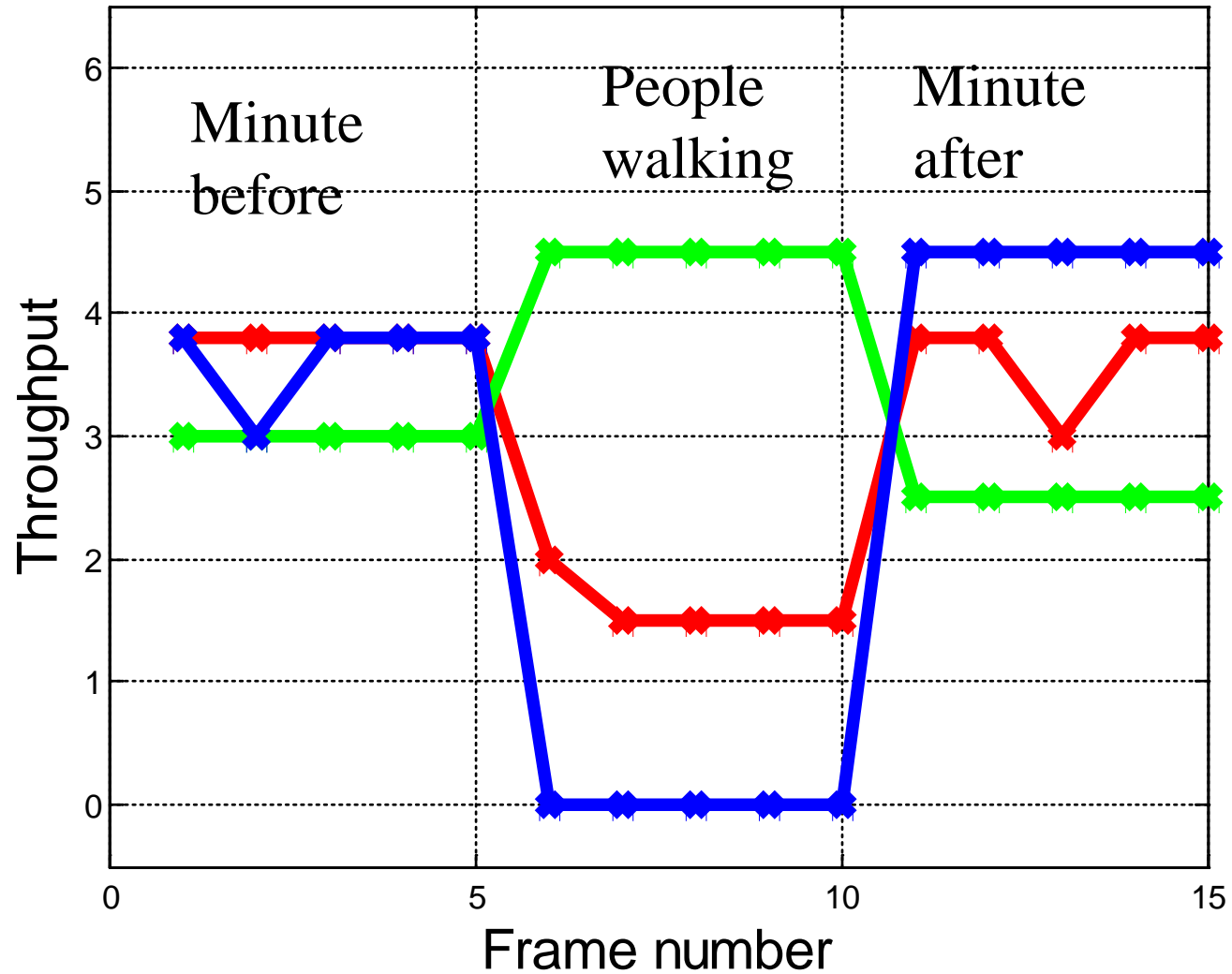
Why is NLoS better for IA?



Time varying channels

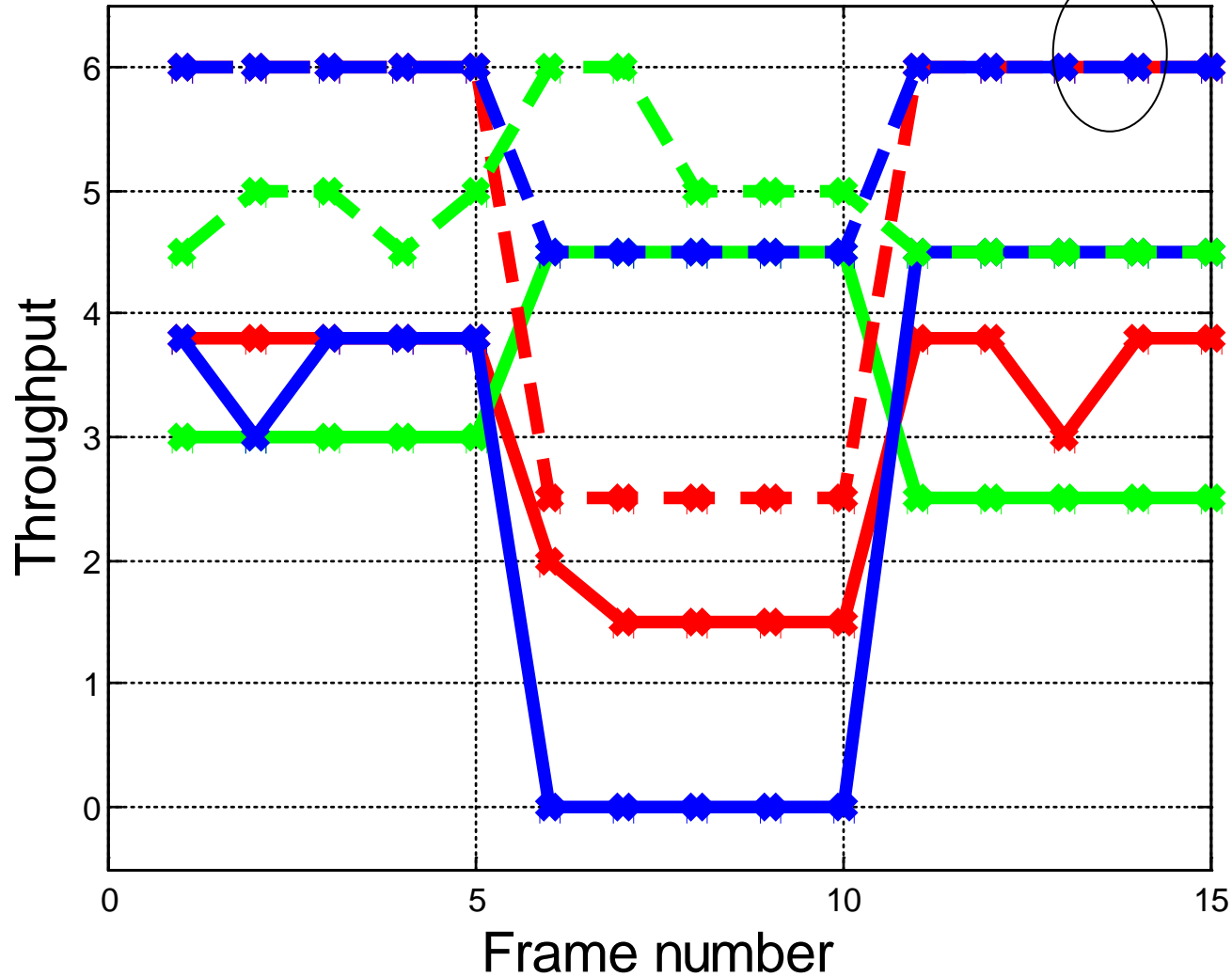


Time varying channels



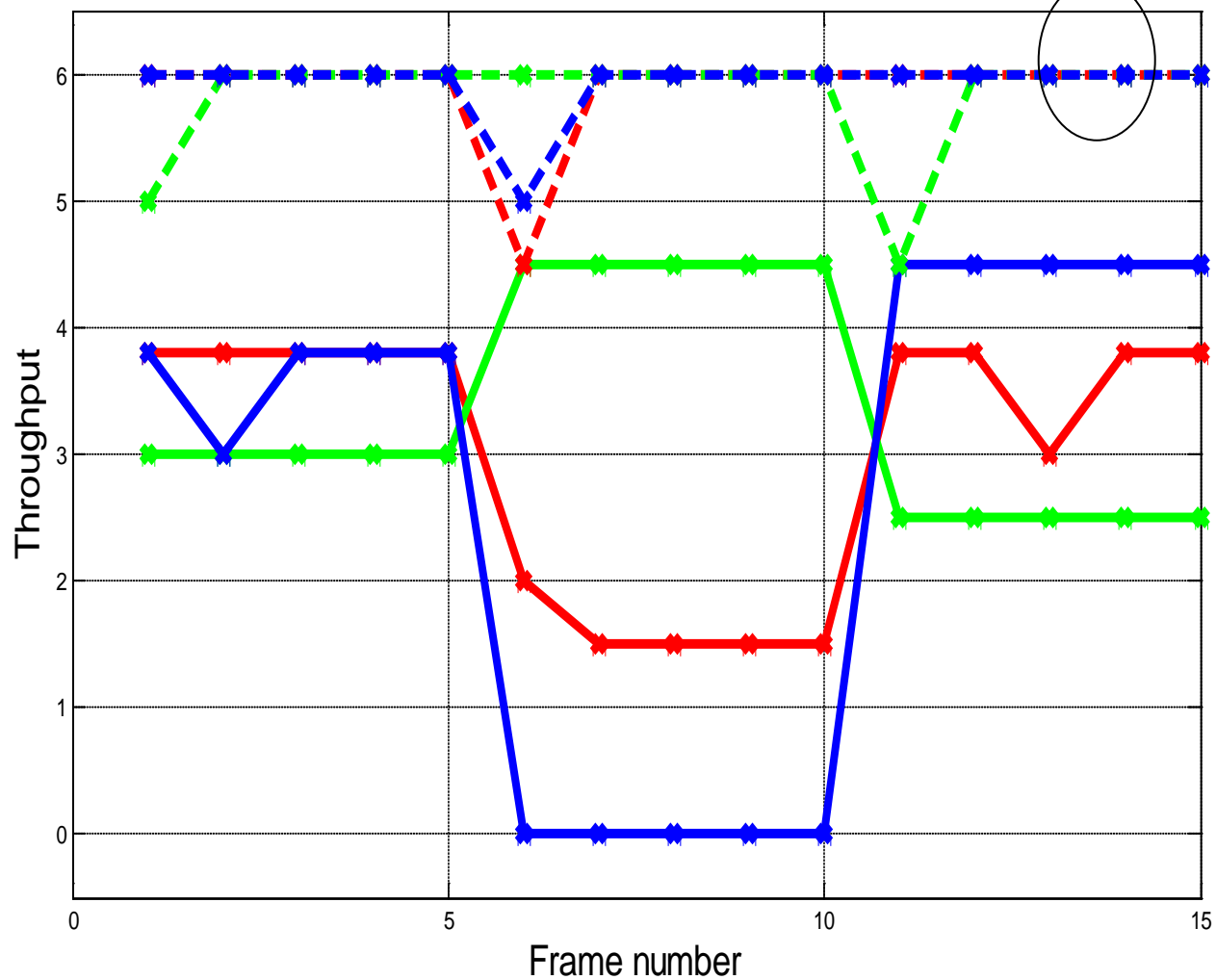
Time varying channels

Simulated on
measured
channels



Time varying channels

0.5ms feedback delay



Conclusion

- IA gives 25% sum throughput gain over SU MIMO on stationary channel (LoS and NLoS averaged)
- CoMP gives 71% gain over SU MIMO.
- All schemes limited by RF impairments.
- Geometry factor important for IA versus MIMO.
- Full reuse SIMO and MIMO worse than SU MIMO.
- Next step: analyzing measurements with time varying channels.

Results versus EVM model

Scheme	Actual performance	Impairment model
IA	11.1	11.7
CoMP	15.2	17.3
SU MIMO	8.9	8.1
FR SIMO	6.5	6.2
FR SIMO	2.3	2.3