

# Sorting algorithms

Johan Montelius

KTH

HT22

# selection sort

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- few write operations
- useful when iteratively searching for the smallest elements

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# merge sort

```
private static void sort(int[] org, int[] aux, int lo, int hi) {
    if (lo != hi) {
        int mid = lo + (hi-lo)/2;
        sort(org, aux, lo, mid);
        sort(org, aux, mid+1, hi);
        merge(org, aux, lo, mid, hi);
    }
}
```

# merge sort work

# merge sort work

6 2 5 4 7 1 3 0

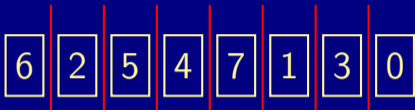
# merge sort work

6 2 5 4 | 7 1 3 0

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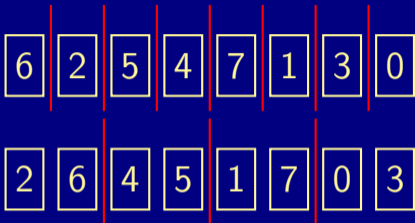


# merge sort work

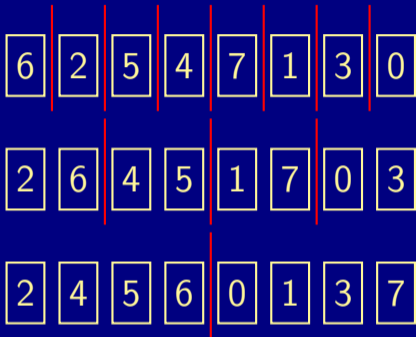




# merge sort work



# merge sort work



# merge sort work

6	2	5	4	7	1	3	0
---	---	---	---	---	---	---	---

2	6	4	5	1	7	0	3
---	---	---	---	---	---	---	---

2	4	5	6	0	1	3	7
---	---	---	---	---	---	---	---

0	1	2	3	4	5	6	7
---	---	---	---	---	---	---	---

# merge sort work

6 | 2 | 5 | 4 | 7 | 1 | 3 | 0

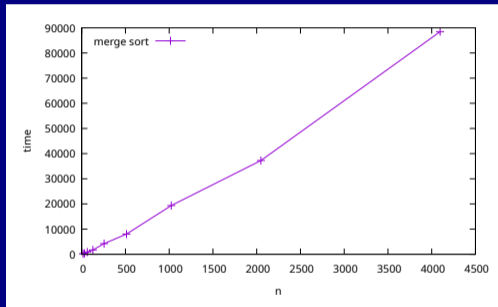
2 | 6 | 4 | 5 | 1 | 7 | 0 | 3

2 | 4 | 5 | 6 | 0 | 1 | 3 | 7

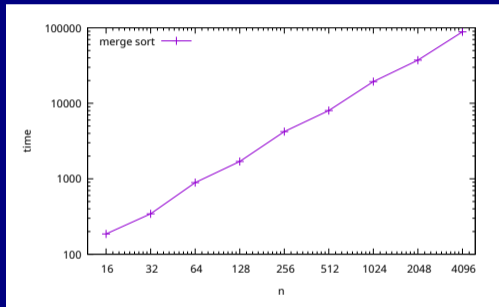
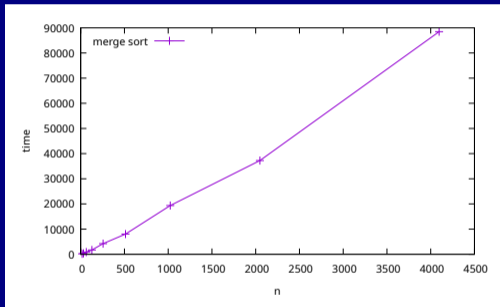
0 | 1 | 2 | 3 | 4 | 5 | 6 | 7

*merge sort executes in  $O(n \times \lg(n))$*

# benchmark



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$n$	$t$	$t/n$
16	186	11.6
32	343	10.7
64	889	13.9
128	1695	13.2
256	4217	16.5
512	8018	15.7
1024	19358	18.9
2048	37242	18.2
4096	88452	21.6

# benchmark

$n$	$t$	$t/n$	$t/(n \times \log(n))$
16	186	11.6	4.2
32	343	10.7	3.1
64	889	13.9	3.3
128	1695	13.2	2.7
256	4217	16.5	3.0
512	8018	15.7	2.5
1024	19358	18.9	2.7
2048	37242	18.2	2.4
4096	88452	21.6	2.6



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- an  $O(n \times \lg(n))$  algorithm
- requires additional space (could be avoided but complicated)
- robust i.e. no worst case scenarios

# quick sort

Merge sort divides the array on the way down and sorts it on the way up.

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Merge sort divides the array on the way down and sorts it on the way up.

Quick sort sorts the array on the way down and assemble it on the way up.

# quick sort

# quick sort





# quick sort

pivot



7	11	5	9	1	2	10	3	6	8	4	0
---	----	---	---	---	---	----	---	---	---	---	---

# quick sort

pivot



i

# quick sort

pivot



i



j

# quick sort

pivot



↑  
i

↑  
j

# quick sort

pivot  
↓



↑  
i

↑  
j

# quick sort

pivot



↑  
i

↑  
j

# quick sort

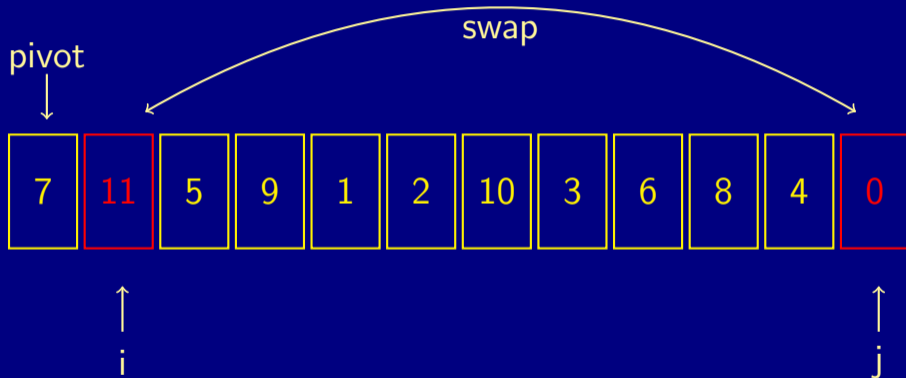
pivot



↑  
i

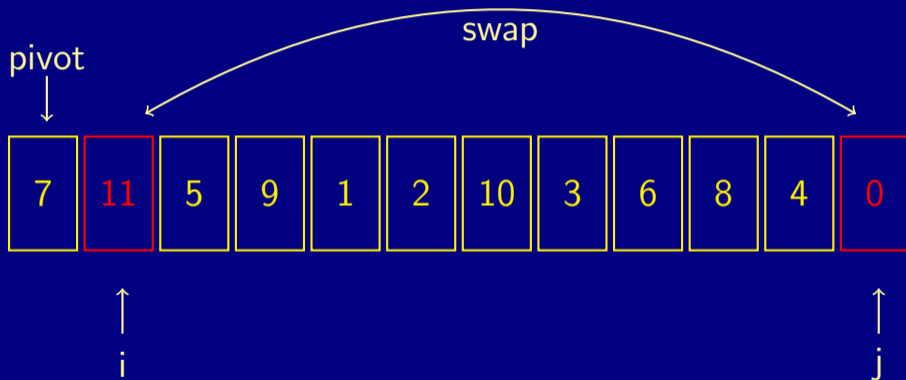
↑  
j

# quick sort





# quick sort



# quick sort

pivot  
↓



↑  
i

↑  
j

# quick sort

pivot  
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pivot  
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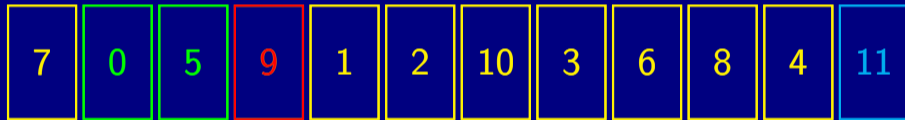


↑  
i

↑  
j

# quick sort

pivot  
↓



↑  
i

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j

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pivot  
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↑  
i

↑  
j

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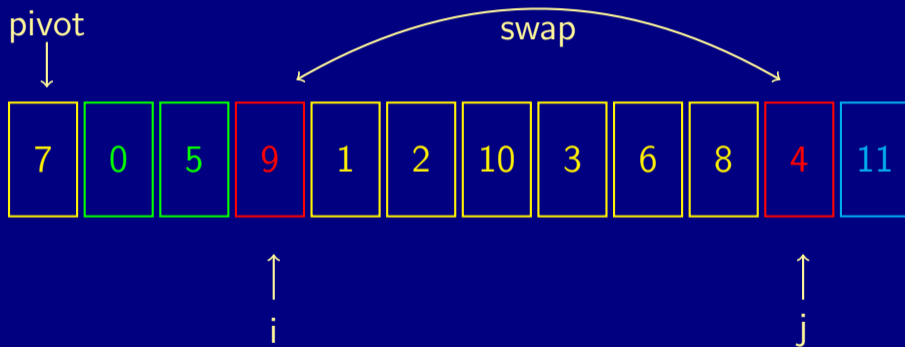
pivot  
↓



↑  
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↑  
i

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j

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↑  
i

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↑  
i

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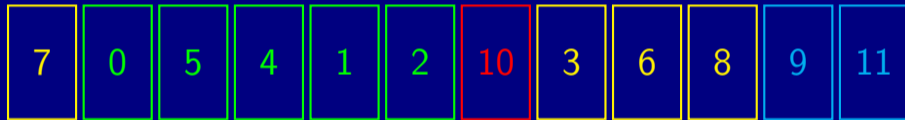


↑  
i

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j

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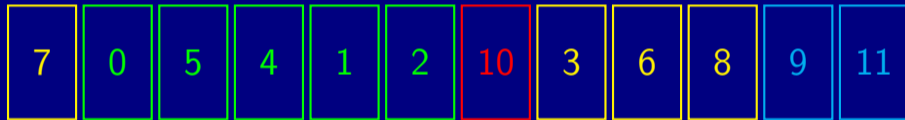


↑  
i

↑  
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pivot  
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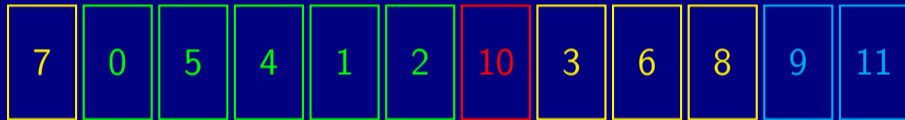


↑  
i

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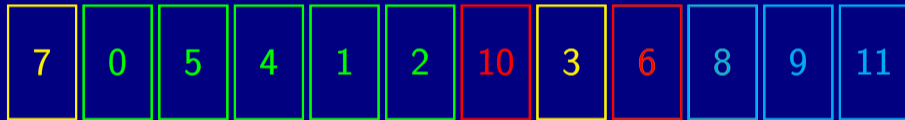
# quick sort

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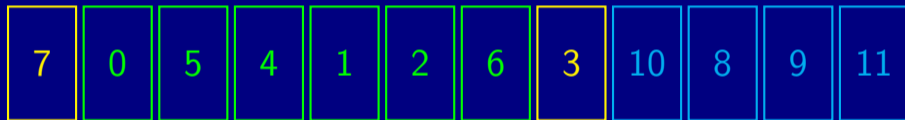
↑  
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↑  
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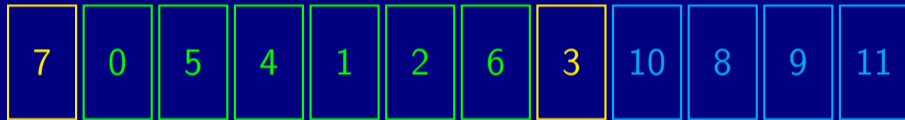
# quick sort

pivot  
↓



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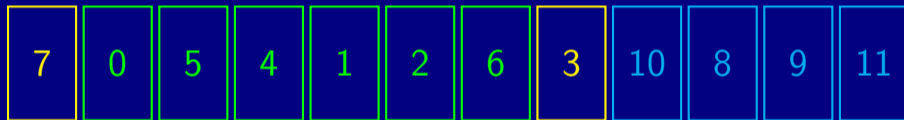


↑  
i

↑  
j

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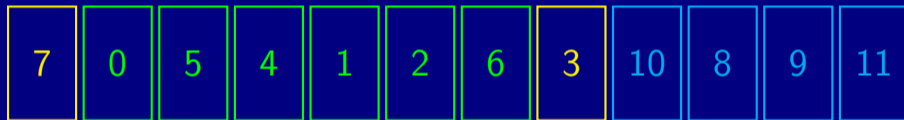
pivot  
↓



↑ ↑  
i j

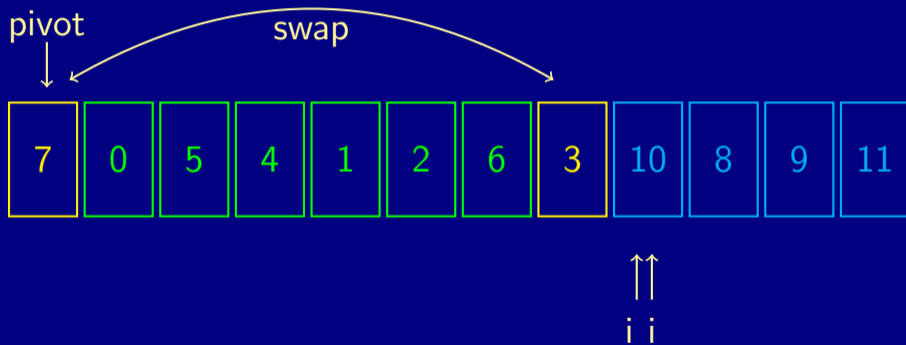
# quick sort

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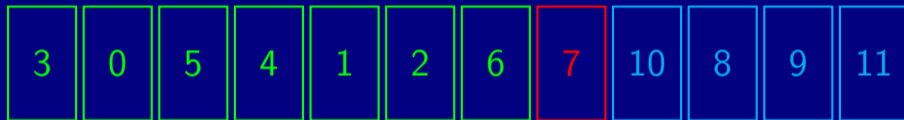


↑    ↑↑  
j    i i

# quick sort



# quick sort



# quick sort work

# quick sort work

3 2 4 5 1 6 0



# quick sort work

3 2 4 5 1 6 0

1 2 0 3 5 6 4

# quick sort work

3 2 4 5 1 6 0

1 2 0 3 5 6 4

0 1 2 3 4 5 6

# quick sort work

3 2 4 5 1 6 0

1 2 0 3 5 6 4

0 1 2 3 4 5 6

0 1 2 3 4 5 6

# quick sort work

3 2 4 5 1 6 0

1 2 0 3 5 6 4

0 1 2 3 4 5 6

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- no additional space

# quick sort

- an  $O(n \times \lg(n))$  algorithm
- no additional space
- worst case scenario if array is sorted -  $O(n^2)$



# stability

A sorting algorithm is *stable* if the given order is preserved when sorting two equal elements.

Why stability matters:

Gustav Bengtsson

Adam Bengtsson

Fredrik Andersson

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# sorting algorithms

stable algorithms

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stable algorithms

- insertion sort

# sorting algorithms

## stable algorithms

- insertion sort
- merge sort

## unstable algorithms



# sorting algorithms

## stable algorithms

- insertion sort
- merge sort

## unstable algorithms

- selection sort

# sorting algorithms

## stable algorithms

- insertion sort
- merge sort

## unstable algorithms

- selection sort
- quick sort