## an infinite list

#### Streams

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```
inf = infinity(); [0|inf] = inf.(); [1|inf] = inf.()

def infinity() do
   fn() -> infinity(0) end
end

def infinity(n) do
  [...|...]
end
```

2.07

#### the list of fibonacci

A function that returns an infinite list of Fibonacci numbers.

```
def fib() do
   fn() -> fib(1,1) end
end

def fib(f1, f2) do
   [f1 | fn() -> fib(f2, f1+f2) end]
end
```

## a lazy list from 1 to 10

Let's represent a *range* of integers from 1 to 10 as:

{:range, 1, 10}

Elixir gives us a syntax for this:

1..10

But we will do our own :-)

This is not how Elixir represents it but it's fine for now

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#### sum/1 of a range

### foldl/3 on a range

```
def sum({:range, to, to}) do ... end
def sum({:range, from, to}) do ... + sum({:range, ..., to}) end

def sum(range) do sum(range, 0) end

def sum({:range, to, to}, acc) do ... end
def sum({:range, from, to}, acc) do sum({:range, ..., to}, ...) end
```

How do we fold-left on a range:

$$foldl(\{:range, 1, 5\}, 0, fn(x,a) \rightarrow x + a end)$$

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#### sum/1 of a range

## map/2 on a range

def sum(range) do foldl(range, 0,  $fn(x,acc) \rightarrow x + acc$  end) end

How do we map on a range (let's forget the order):

$$map(\{:range, 1, 5\}, fn(x) \rightarrow x + 1 end)$$

should we return a list of values or .... a modified range?

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#### filter/2 on a range

### take/2 on a range

```
How do we filter a range (again, f*ck the order):
 filter(\{: range, 1, 5\}, fn(x) \rightarrow rem(x,2) == 0 end)
should we return a list of values or ....
```

```
How do we take n elements from a range (order ... not):
```

```
take({:range, 1, 1_000_000}, 5)
```

we don't want to build a list of a million integers

# reduce/3: the goto of all

... we're not done!

```
def sum(r) do
    reduce(r, 0, fn(x,a) \rightarrow x+a end)
  end
Our reduce/3 should work as foldl/3 (left to right, tail recursive).
  def reduce({:range, from , to}, acc, fun) do
    if from <= to do
      reduce({:range, from+1, to}, fun.(from, acc), fun)
    else
      acc
    end
  end
```

## How do we stop in the midle?

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Implement take/2 using reduce by .....

We need to control the reduction.

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#### continue

```
def reduce({:range, from , to}, {:cont, acc}, fun) do
   if from <= to do
     reduce({:range, from+1, to}, fun.(from, acc), fun)
   else
     {:done, acc}
   end
end

def sum(r) do
   reduce(r, {:cont, 0}, fn(x,a) -> {:cont, x+a} end)
end
```

The accumulator is both a value and an instruction to continue.

### suspend in the midle: head and tail

```
:
def reduce(range, {:suspend, acc}, fun) do
    {:suspended, acc, fn(cmd) -> reduce(range, cmd, fun) end}
end

def head(r) do
    reduce(r, {:cont, :na},
    fn (x, _) ->
        {:suspend, x}
    end)
end
```

### stop in the midle

```
:
  def reduce(_, {:halt, acc}, _fun) do
    {:halted, acc}
end

def take(r, n) do
  reduce(r, {:cont, {:sofar, n, [] }},
    fn(x,{:sofar, n, a}) ->
        if n > 0 do
        {:cont, {:sofar, n-1, [x|a]}}
    else
        {:halt, [x|a]}
    end
    end)
end
```

Elixir libraries

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- List: operatates on lists, returns a list or some value.
- Enum: takes an Enumerable as argument, returns a list or value.
- Stream: takes an Enumerable as argument, returns an Enumerable or value.

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A datastructure is Enumerable if it implements the enumerable protocol. Lists and ranges are Enumerable.

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# Summary

- range: representation of a range of integers
- streams: lazy evaluation of sequences